

# The Impact of Structural Distortions on the Magnetism of Double Perovskites Containing 5d<sup>1</sup> Transition-Metal Ions

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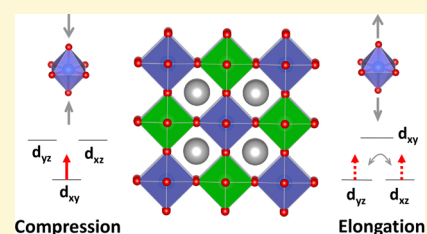


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**ABSTRACT:** Five double perovskites, each containing a transition-metal ion with a 5d<sup>1</sup> configuration, have been studied to better understand the surprising diversity of magnetic ground states seen in these isoelectronic compounds. Ba<sub>2</sub>ZnReO<sub>6</sub> adopts the cubic double perovskite structure and magnetically orders below 16 K, with a canted ferromagnetic structure and a saturated magnetization of ~0.24 μ<sub>B</sub>/Re. X-ray magnetic circular dichroism indicates a substantial orbital moment of approximately 0.4 μ<sub>B</sub>/Re that opposes the spin moment. The structures of Ba<sub>2</sub>NaOsO<sub>6</sub> (canted ferromagnet, T<sub>C</sub> = 7 K) and Ba<sub>2</sub>LiOsO<sub>6</sub> (antiferromagnet, T<sub>N</sub> = 8 K) are reinvestigated using time-of-flight neutron powder diffraction and found to crystallize with the cubic double perovskite structure. No evidence for a structural distortion can be found in either compound down to 10 K. Ba<sub>2</sub>CdReO<sub>6</sub> is also cubic at room temperature but undergoes a structural transition upon cooling below ~180 K to a tetragonal structure with I4/m symmetry that involves compression of the Re–O bonds that are parallel to the c-axis. Sr<sub>2</sub>LiOsO<sub>6</sub> shows a similar tetragonal distortion at room temperature and maintains that structure down to 10 K. Surprisingly, the Os-centered octahedron in Sr<sub>2</sub>LiOsO<sub>6</sub> is distorted in the opposite direction, exhibiting an elongation of the Os–O bonds along the c-axis. Differences in the distortions of the octahedra lead to different magnetic ground states, antiferromagnetic (T<sub>N</sub> = 4 K) for Ba<sub>2</sub>CdReO<sub>6</sub> and spin glass (T<sub>g</sub> = 30 K) for Sr<sub>2</sub>LiOsO<sub>6</sub>. Theoretical modeling shows that the varied magnetic behaviors of double perovskites containing 5d<sup>1</sup> ions are closely tied to crystallographic distortions. These distortions remove the degeneracy of the 5d t<sub>2g</sub> orbitals, leading to changes in orbital occupation that ultimately determine which of the several competing magnetic ground states is favored.



## INTRODUCTION

Double perovskites with the general formula A<sub>2</sub>MM'O<sub>6</sub>, where A and M are diamagnetic ions and M' is a 5d ion, are an intriguing playground for studying magnetism. Two key features—strong spin–orbit coupling and a relatively large radial extension from the nucleus—differentiate 5d orbitals from their 3d counterparts. The former alters the interplay of spin, orbital, charge, and lattice degrees of freedom, while the latter leads to larger hybridization with oxygen, which impacts the strength of competing superexchange interactions and the tendency toward orbital ordering.

Among double perovskites containing M' cations with either a 5d<sup>2</sup> or 5d<sup>3</sup> electron configuration, antiferromagnetic ground states dominate, although recently, three double perovskites containing the 5d<sup>2</sup> ion Os<sup>6+</sup> were reported to adopt octupolar ordering rather than conventional long-range ordering of magnetic dipole moments.<sup>1</sup> In contrast, double perovskites containing 5d<sup>1</sup> ions show a diverse array of ground states (see Figure 1). Previous studies of Ba<sub>2</sub>NaOsO<sub>6</sub>,<sup>2–4</sup> Ba<sub>2</sub>MgReO<sub>6</sub>,<sup>5,6</sup> Ba<sub>2</sub>ZnReO<sub>6</sub>,<sup>5</sup> and Ba<sub>2</sub>CdReO<sub>6</sub><sup>7</sup> report a hysteresis loop at a low temperature with a saturated moment of ~0.2 μ<sub>B</sub> per formula unit. Single-crystal magnetization measurements in combination with either nuclear magnetic resonance (NMR)<sup>8</sup>

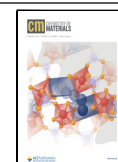
or resonant X-ray scattering studies<sup>9</sup> indicate that the magnetic structures of Ba<sub>2</sub>MgReO<sub>6</sub> and Ba<sub>2</sub>NaOsO<sub>6</sub> contain ferromagnetic (001) layers that are strongly canted with respect to the neighboring (001) layers. This structure might best be described as intermediate between a collinear ferromagnetic structure and a type I antiferromagnetic structure, as illustrated in Figure 1d. Hereafter, we refer to this as a canted ferromagnetic structure. Ba<sub>2</sub>ZnReO<sub>6</sub> and Ba<sub>2</sub>CdReO<sub>6</sub> are assumed to adopt similar structures, but magnetization measurements on powder samples are not sufficient to unambiguously differentiate this structure from the simpler ferromagnetic ground state.

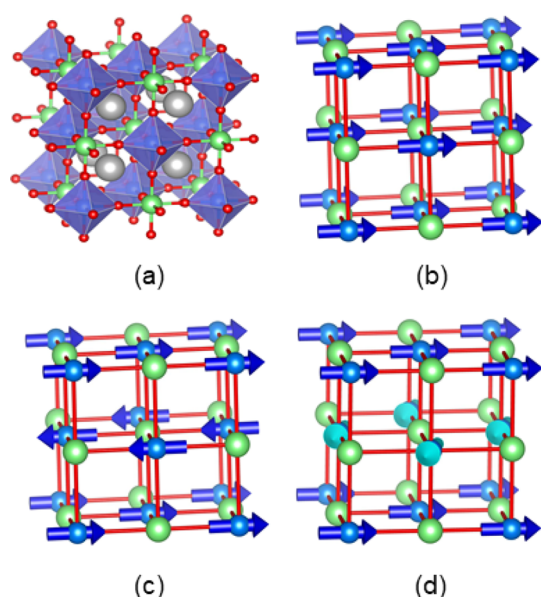
Not all 5d<sup>1</sup> double perovskites adopt the canted ferromagnetic structure of Figure 1d. For reasons that are not well understood, the isoelectronic and isostructural Ba<sub>2</sub>LiOsO<sub>6</sub> adopts an antiferromagnetic ground state (T<sub>N</sub> =

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**Figure 1.** (a)  $A_2MM'O_6$  cubic double perovskite structure emphasizing the  $M'O_6$  octahedra. Magnetic structures of double perovskites that are (b) ferromagnetic, (c) type I antiferromagnetic, and (d) canted ferromagnetic.

8 K) and has been shown to exhibit a spin-flop transition to a ferromagnetic state in magnetic fields greater than 5.5 T.<sup>2,4</sup> A recent study on single crystals of the tetragonally distorted  $Sr_2MgReO_6$  revealed a type I antiferromagnetic state below  $T_N = 55$  K. Earlier studies on polycrystalline samples of the same compound presented strong evidence for spin glass behavior at a low temperature.<sup>10–13</sup> This suggests that the presence of defects or subtle compositional variations may be enough to stabilize a different magnetic ground state.

A theoretical study of nominally cubic  $5d^1$  double perovskites using a model Hamiltonian approach was initiated by Chen et al.<sup>14</sup> and later extended by Svoboda et al.<sup>15</sup> In these studies, two separate phase transitions are found: orbital order (equivalent to quadrupolar order) that sets in at a higher temperature,  $T_o$ , and magnetic ordering that occurs at a lower temperature,  $T_c$ . This can account for several observed anomalies such as the recovery of only  $R \cdot \ln 2$  (and not  $R \cdot \ln 4$ ) entropy at the magnetic  $T_c$  in  $Ba_2NaOsO_6$  and  $Ba_2MgReO_6$  and the deviations from the Curie–Weiss susceptibility above  $T_c$ . This analysis also shows that the electronically induced orbital ordering naturally leads to a canted ferromagnetic ground state for a large part of parameter space.<sup>14,15</sup> It was also qualitatively argued<sup>15</sup> that the orbital order should lead to a very small lattice distortion, which was difficult to observe directly until the publication of high-resolution, single-crystal diffraction studies of  $Ba_2MgReO_6$ .<sup>6,9</sup>

In this study, we take a careful look at the role of structural distortions on the magnetism of double perovskites containing  $5d^1$  ions by studying five compositions:  $Ba_2NaOsO_6$ ,  $Ba_2LiOsO_6$ ,  $Ba_2ZnReO_6$ ,  $Ba_2CdReO_6$ , and  $Sr_2LiOsO_6$ . We find that the latter two compounds undergo tetragonal distortions at temperatures well above the magnetic ordering/freezing temperature, and these distortions have significant implications for the magnetism. Theoretical modeling is used to understand how changes in energy levels and occupation of the  $5d$  orbitals that accompany these structural distortions

impact the delicate balance between competing magnetic ground states.

## EXPERIMENTAL SECTION

Polycrystalline samples were prepared by solid-state methods. Reagents included BaO (Sigma-Aldrich, 99.99% metals basis), SrO (Sigma-Aldrich, 99.9% trace metals basis), Os powder (Sigma-Aldrich, 99.9% trace metals basis),  $ReO_3$  (Alfa Aesar, 99.9% trace metals basis), ZnO (Alfa Aesar, 99.99% metals basis), CdO (Cerac, 99.95% pure),  $Li_2O$  (Alfa Aesar, 99.5%), and  $Na_2O_2$  (Alfa Aesar, 95%). Stoichiometric amounts of the appropriate starting materials were thoroughly mixed using a mortar and pestle in an argon-filled glovebox. The mixture was loaded into an alumina container and sealed in a silica tube under dynamic vacuum. The tube was then placed in a furnace and heated to 1000 °C for 24–48 h. For the compounds containing osmium, a separate alumina cap containing  $MnO_2$  was also enclosed in the sealed quartz tube as the decomposition of  $MnO_2$  acted as the oxygen source needed to oxidize Os metal via reaction  $3 MnO_2(s) \rightarrow Mn_3O_4(s) + O_2(g)$ . The amount of  $MnO_2$  used was sufficient to produce 1/4 mole excess  $O_2(g)$  for every mole of double perovskite formed. The furnace was located inside a fume hood so that toxic  $OsO_4(g)$  would be vented out of the laboratory should the integrity of the silica tube be compromised during heating.

Laboratory X-ray powder diffraction (XRPD) was performed at room temperature using a Bruker D8 Advance diffractometer equipped with a Cu source and a Ge (111) incident beam monochromator. The low-temperature X-ray powder diffraction measurements were performed using a PANalytical X'Pert Pro MPD diffractometer with copper  $K\alpha_1$  radiation and an Oxford Phenix cryostat between 20 and 300 K. Synchrotron X-ray powder diffraction data were collected on  $Ba_2ZnReO_6$  and  $Ba_2CdReO_6$  at temperatures of 300 and 90 K using the 11-BM beamline at the Advanced Photon Source, with a wavelength  $\lambda = 0.4147$  Å. Synchrotron X-ray powder diffraction data were collected on  $Sr_2LiOsO_6$  at 300 K using the Brockhouse X-ray diffraction and scattering beamline (BXDS-WLE) at the Canadian Light Source, with wavelength  $\lambda = 0.82015$  Å.

Time-of-flight neutron powder diffraction (TOF-NPD) data were obtained on all three osmium-containing double perovskites using the POWGEN diffractometer at the Spallation Neutron Source (SNS) located at Oak Ridge National Laboratory. Approximately 3 g of  $Ba_2NaOsO_6$ , 3 g of  $Ba_2LiOsO_6$ , and 6 g of  $Sr_2LiOsO_6$  were packed in the cylindrical vanadium cans 6 to 8 mm in diameter. Data were collected with scan times ranging from 30 to 120 min per scan. Constant wavelength neutron powder diffraction (NPD) data sets were collected on  $Ba_2ZnReO_6$  using the triple-axis spectrometer HB-1A at the High Flux Isotope Reactor (HFIR) to look for signs of magnetic scattering. Approximately 11 g of powdered sample was sealed into a cylindrical aluminum can under a He atmosphere. Data were collected at 1.5 and 25 K using constant wavelength neutrons ( $\lambda = 2.37$  Å) and collimation of 40'–40'–80'–open. The X-ray and neutron diffraction patterns were analyzed using the Rietveld method, as implemented in either the TOPAS-Academic (v6) package<sup>16</sup> or the Fullprof software package.<sup>17</sup>

DC magnetic susceptibility for all samples were measured using a Quantum Design Magnetic Property Measurement System (MPMS) SQUID magnetometer. Polycrystalline samples of approximately 0.1 g were encapsulated in gel capsules, which were inserted into the center of a straw and then mounted in the magnetometer. Data were collected between 2 and 400 K under both zero-field-cooled (ZFC) and field-cooled (FC) conditions with an applied field of 1000 Oe. A diamagnetic correction was applied by subtracting the temperature-dependent susceptibility measured on an empty gel capsule and the diamagnetic constant of the constituent ions.<sup>18</sup> Isothermal magnetization curves were measured between  $-7$  and  $+7$  T. The temperature-dependent specific heat data were collected using a 9 T Quantum Dynamics PPMS in the temperature range  $1.9$  K  $< T < 300$  K.

**Table 1. Summary of Key Structural Parameters for the Double Perovskites Studied at Room Temperature<sup>a</sup>**

compound	tolerance factor	space group	lattice parameters (Å)	Os/Re–O dist. (Å)	M–O dist. (Å)
Ba <sub>2</sub> ZnReO <sub>6</sub>	1.041	<i>Fm</i> $\bar{3}$ <i>m</i>	<i>a</i> = 8.10610(1)	1.941(1) × 6	2.112(1) × 6
Ba <sub>2</sub> LiOsO <sub>6</sub>	1.036	<i>Fm</i> $\bar{3}$ <i>m</i>	<i>a</i> = 8.10148(2)	1.8964(9) × 6	2.1543(9) × 6
Ba <sub>2</sub> CdReO <sub>6</sub>	0.990	<i>Fm</i> $\bar{3}$ <i>m</i>	<i>a</i> = 8.32557(1)	1.906(3) × 6	2.257(3) × 6
Ba <sub>2</sub> NaOsO <sub>6</sub>	0.974	<i>Fm</i> $\bar{3}$ <i>m</i>	<i>a</i> = 8.28137(2)	1.8829(7) × 6	2.2575(7) × 6
Sr <sub>2</sub> LiOsO <sub>6</sub>	0.977	<i>I4/m</i>	<i>a</i> = 5.52746(4) <i>c</i> = 7.97506(6)	1.877(9) × 4 1.889(7) × 2	2.053(9) × 4 2.098(7) × 2

<sup>a</sup>Values based on analysis of either synchrotron X-ray diffraction data (Ba<sub>2</sub>ZnReO<sub>6</sub>, Ba<sub>2</sub>CdReO<sub>6</sub>, and Sr<sub>2</sub>LiOsO<sub>6</sub>) or time-of-flight neutron powder diffraction data (Ba<sub>2</sub>LiOsO<sub>6</sub> and Ba<sub>2</sub>NaOsO<sub>6</sub>). Full details of these refinements can be found in the [Supporting Information](#).

X-ray magnetic circular dichroism (XMCD) data at Re L<sub>2,3</sub> edges were collected on a powder sample of Ba<sub>2</sub>ZnReO<sub>6</sub> using transmission geometry at beamline 4-ID-D of the Advanced Photon Source at Argonne National Laboratory. The helicity of circularly polarized X-rays, generated by a 500 μm-thick diamond (111) phase plate, was switched at 13.1 Hz and the related modulation in X-ray absorption was detected with a phase lock-in amplifier. The sample was mounted in the variable temperature insert of a cryomagnet and cooled to 2 K in <sup>4</sup>He vapor. Measurements were done in 4 T applied field for two opposite field directions. The spectra for opposite field directions were combined to yield artifact-free XMCD data. The spectra collected at the L<sub>3</sub> and L<sub>2</sub> edges were normalized and integrated for sum rules analysis.<sup>19,20</sup>

Time-domain terahertz spectroscopy data sets were collected, as described in earlier works by Mai et al. and Warren et al.<sup>21,22</sup> Electrical conductivity was measured on cold-pressed pellets of Ba<sub>2</sub>ZnReO<sub>6</sub> and Ba<sub>2</sub>CdReO<sub>6</sub> using a Quantum Design Physical Property Measurement System (PPMS). The four-point probe geometry was made using copper wire and silver paint. The low temperature limit is determined by the temperature below which the sample becomes too resistive to be measured accurately.

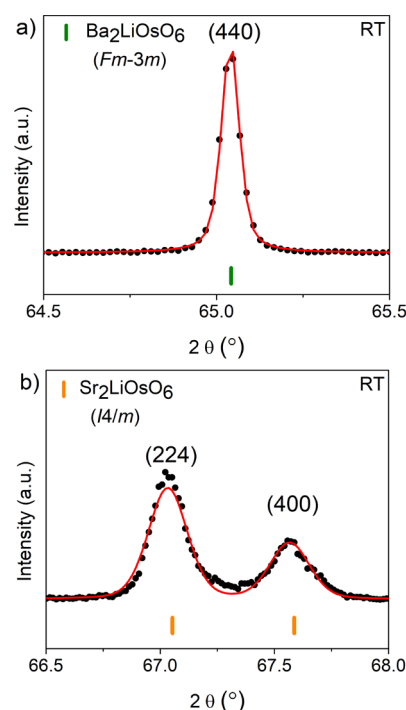
## RESULTS

**Room-Temperature Crystal Structures.** The crystal structures of Ba<sub>2</sub>MOsO<sub>6</sub> (M = Li and Na), Ba<sub>2</sub>MReO<sub>6</sub> (M = Zn and Cd), and Sr<sub>2</sub>LiOsO<sub>6</sub> were studied using a combination of synchrotron X-ray powder diffraction and neutron powder diffraction techniques. [Table 1](#) summarizes the results at room temperature, where all four barium-containing compounds adopt the cubic double perovskite structure with *Fm* $\bar{3}$ *m* space group symmetry. The values of the cell parameters and bond distances for the first four compounds are all in very good agreement (within 1% or less) with earlier literature reports.<sup>2,5,7,23</sup> To a first approximation, the osmium- and rhenium-centered octahedra are similar in size so that the variations in the cubic cell edge largely depend upon the size of the diamagnetic M cation. Those compounds containing Li<sup>+</sup> and Zn<sup>2+</sup> ions have smaller unit cells, whereas incorporation of larger Na<sup>+</sup> and Cd<sup>2+</sup> results in a 2–3% expansion of the unit cell edge. As the unit cell expands, the Os–Os and Re–Re distances also increase, which should lead to slightly weaker superexchange coupling between magnetic 5d ions and weaker Coulombic repulsions between the electrons in occupied 5d orbitals on neighboring Os/Re ions. Attempts to refine antisite disorder between octahedral-site cations did not lead to an improvement in the goodness of fit. If antisite disorder is present, it is too small to be detected by diffraction methods. Given the large differences in the charge and size of the M and M' cations, the absence of antisite disorder is not surprising.

The fit of the Ba<sup>2+</sup>/Sr<sup>2+</sup> ions to the cubic network of corner-sharing octahedra can be assessed with the tolerance factor  $\tau = \sqrt{2}(r_A + r_O)/(r_M + r_{M'} + 2r_O)$ ,<sup>24</sup> where *r*<sub>M'</sub> is the ionic radius of the osmium/rhenium ion, *r*<sub>O</sub> is the radius of the oxide

anion, and *r*<sub>A</sub> and *r*<sub>M</sub> are the radii of 12- and 6-coordinate diamagnetic cations, respectively. We see that for M = Li<sup>+</sup> and Zn<sup>2+</sup>, the tolerance factor is larger than 1, indicating that the Ba<sup>2+</sup> ion is stuffed into a framework for which it is slightly too large. This leads to a subtle expansion of the Re–O and Os–O bonds. The effect is surprisingly large for Ba<sub>2</sub>ZnReO<sub>6</sub>, although it should be noted that an earlier neutron powder study of this compound by Marjerrison et al. reported a somewhat shorter Re–O bond length of 1.922(2) Å.<sup>5</sup> Nevertheless, either value would represent an expansion from the 1.906(3) Å value obtained for Ba<sub>2</sub>CdReO<sub>6</sub>. This stretching of the bonds will lead to a small reduction in the crystal field splitting of the 5d orbitals and may subtly reduce the covalency of the Re/Os–O bonds.

Unlike its Ba<sub>2</sub>MM'O<sub>6</sub> counterparts, Sr<sub>2</sub>LiOsO<sub>6</sub> is tetragonally distorted from the cubic structure at room temperature, in contradiction to an earlier study that reported a cubic *Fm* $\bar{3}$ *m* structure.<sup>25</sup> The magnitude of the distortion can be quantified by the *c/a* ratio of the original cubic unit cell, which when expressed in terms of the tetragonal unit cell parameters, becomes *c*<sub>t</sub>/(√2*a*<sub>t</sub>) = 1.020. This 2% expansion of the *c*-axis leads to a peak splitting that is evident in both X-ray and neutron diffraction patterns ([Figure 2](#)). The tetragonal space

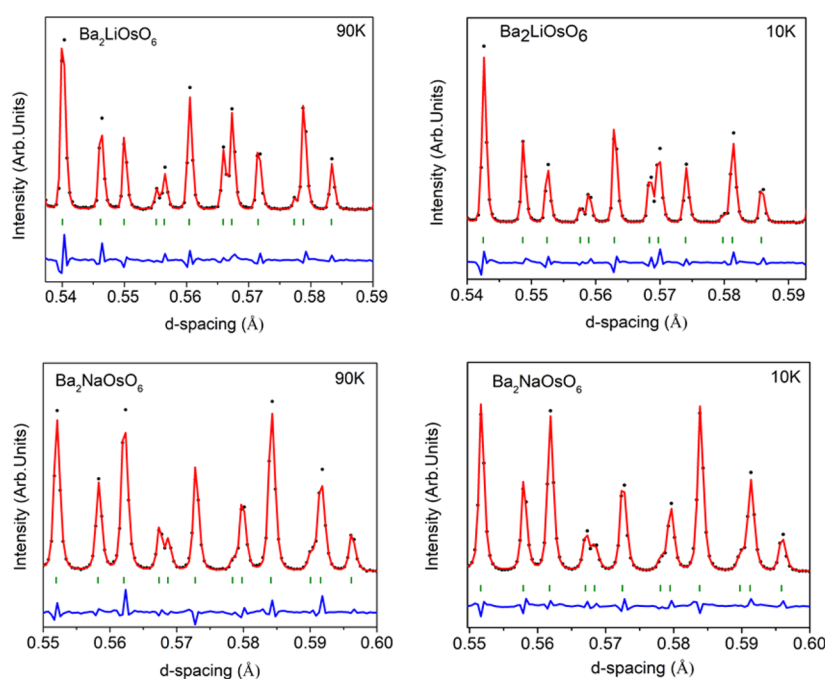


**Figure 2.** (a) The (440) peak in cubic *Fm* $\bar{3}$ *m* Ba<sub>2</sub>LiOsO<sub>6</sub> splits into the (b) (224) and (400) peaks in tetragonal *I4/m* Sr<sub>2</sub>LiOsO<sub>6</sub>.

**Table 2. Summary of Key Structural Parameters Obtained from Synchrotron X-ray Powder Diffraction (SXPd), Constant Wavelength Neutron Powder Diffraction (NPD), and Time-of-Flight Neutron Powder Diffraction (TOF-NPD) Data<sup>a</sup>**

compound	technique	temp (K)	space group	lattice parameters (Å)	Os/Re–O dist. (Å)	M–O dist. (Å)
Ba <sub>2</sub> ZnReO <sub>6</sub>	SXPd	90	<i>Fm</i> $\bar{3}$ <i>m</i>	<i>a</i> = 8.08998(1)	1.940(1) × 6	2.105(1) × 6
Ba <sub>2</sub> ZnReO <sub>6</sub>	NPD	25	<i>Fm</i> $\bar{3}$ <i>m</i>	<i>a</i> = 8.0940(5)	1.918(3) × 6	2.129(3) × 6
Ba <sub>2</sub> ZnReO <sub>6</sub>	NPD	1.5	<i>Fm</i> $\bar{3}$ <i>m</i>	<i>a</i> = 8.094(1)	1.920(3) × 6	2.127(3) × 6
Ba <sub>2</sub> LiOsO <sub>6</sub>	TOF-NPD	90	<i>Fm</i> $\bar{3}$ <i>m</i>	<i>a</i> = 8.08256(1)	1.8951(8) × 6	2.1462(8) × 6
Ba <sub>2</sub> LiOsO <sub>6</sub>	TOF-NPD	10	<i>Fm</i> $\bar{3}$ <i>m</i>	<i>a</i> = 8.07919(1)	1.8946(8) × 6	2.1450(8) × 6
Ba <sub>2</sub> CdReO <sub>6</sub>	SXPd	90	<i>I4/m</i>	<i>a</i> = 5.87193(7) <i>c</i> = 8.3236(1)	1.916(9) × 4 1.901(7) × 2	2.25(1) × 4 2.261(7) × 2
Ba <sub>2</sub> NaOsO <sub>6</sub>	TOF-NPD	90	<i>Fm</i> $\bar{3}$ <i>m</i>	<i>a</i> = 8.26077(2)	1.8829(5) × 6	2.2475(5) × 6
Ba <sub>2</sub> NaOsO <sub>6</sub>	TOF-NPD	10	<i>Fm</i> $\bar{3}$ <i>m</i>	<i>a</i> = 8.25622(1)	1.8834(5) × 6	2.2447(5) × 6
Sr <sub>2</sub> LiOsO <sub>6</sub>	TOF-NPD	90	<i>I4/m</i>	<i>a</i> = 5.4966(1) <i>c</i> = 8.0034(2)	1.889(3) × 4 1.916(4) × 2	2.032(3) × 4 2.086(4) × 2
Sr <sub>2</sub> LiOsO <sub>6</sub>	TOF-NPD	10	<i>I4/m</i>	<i>a</i> = 5.49088(1) <i>c</i> = 8.0111(2)	1.888(3) × 4 1.919(4) × 2	2.031(3) × 4 2.087(4) × 2

<sup>a</sup>Full details of these refinements can be found in the Supporting Information.



**Figure 3.** Rietveld refinements of TOF-NPD data collected on Ba<sub>2</sub>LiOsO<sub>6</sub> (top) and Ba<sub>2</sub>NaOsO<sub>6</sub> (bottom) at 90 K (left) and 10 K (right). The black dots represent experimental intensities, the red line is the fit to the data with a cubic model, the green tick marks denote the expected peak positions, and the blue curve is the difference between experiment and the calculated fit.

group *I4/m* allows for distortions of the octahedra as well as out-of-phase rotations of the octahedra about the *c*-axis (Glazer tilt system *a*<sup>0</sup>*a*<sup>0</sup>*c*<sup>-</sup>).<sup>26</sup> From the bond lengths in Table 1, we see a 2.2% elongation of the axial bonds of the Li-centered octahedron, whereas the axial bonds of the Os-centered octahedron only elongate by 0.6%. This would seem to suggest that the distortion is driven by the small tolerance factor and the need to optimize the Sr–O bonding, rather than an electronically driven distortion arising from the partially filled *t*<sub>2g</sub> orbitals on Os<sup>7+</sup>. The Os–O–Li bond angle in the *ab*-plane, which would be linear in the cubic structure, is reduced to 167.9(5)° by rotations of the octahedra. The rotations of Os-centered octahedra as well as the elongation of the *c*-axis make the superexchange interactions within the *ab*-plane subtly different than the interactions between different (001) planes, presumably reducing the frustration of the face-centered cubic topology.

**Crystal Structures below Room Temperature.** Table 2 summarizes the results of low-temperature structural studies carried out using a combination of synchrotron X-ray and neutron powder diffraction methods. No evidence of a reduction in symmetry from the cubic double perovskite structure was detected in Ba<sub>2</sub>ZnReO<sub>6</sub>, Ba<sub>2</sub>LiOsO<sub>6</sub>, or Ba<sub>2</sub>NaOsO<sub>6</sub>. Sr<sub>2</sub>LiOsO<sub>6</sub> retains its tetragonal structure down to 10 K, but the tetragonal elongation of the OsO<sub>6</sub> octahedron increases at low temperatures. Ba<sub>2</sub>CdReO<sub>6</sub> is the only compound of these five that undergoes a detectable structural phase transition, undergoing a cubic-to-tetragonal phase transition upon cooling below approximately 170–180 K, as discussed below.

Given the relatively large tolerance factors of Ba<sub>2</sub>ZnReO<sub>6</sub> ( $\tau = 1.041$ ) and Ba<sub>2</sub>LiOsO<sub>6</sub> ( $\tau = 1.036$ ), it is not surprising that the cubic *Fm* $\bar{3}$ *m* structure is retained at low temperatures. However, a recent single-crystal synchrotron X-ray diffraction

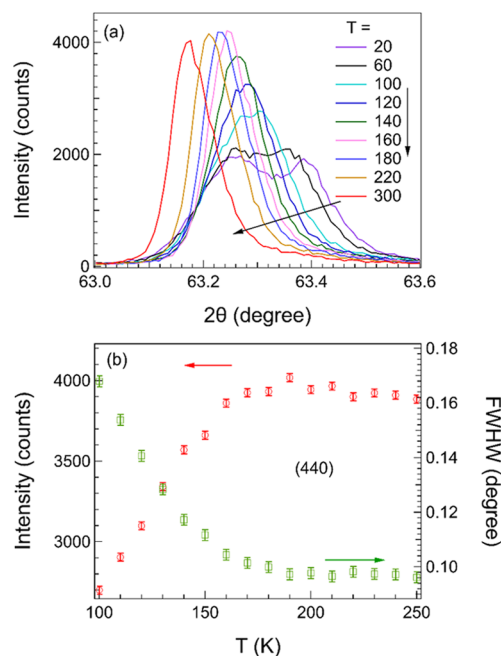
investigation of  $\text{Ba}_2\text{MgReO}_6$  ( $\tau = 1.046$ ) detected a transition to the tetragonal space group  $P4_2/mnm$  below 33 K. This transition appears to be driven by a complex pattern of orbital ordering.<sup>9</sup> SXPD data collected on  $\text{Ba}_2\text{ZnReO}_6$  at 90 K shows little change from the cubic structure seen at room temperature. NPD data sets collected on the triple-axis spectrometer HB-1A above (25 K) and below (1.5 K)  $T_C$  also show no sign of deviation from cubic symmetry, but the relatively low resolution of this instrument is not sufficient to detect the symmetry breaking reported for  $\text{Ba}_2\text{MgReO}_6$ .

High-resolution TOF-NPD data, better suited to detect subtle crystallographic distortions, were collected for the three osmate double perovskites studied. Rietveld refinements using data collected at 10 K are shown in Figure 3. The pattern collected on  $\text{Ba}_2\text{LiOsO}_6$  was fit with both cubic ( $Fm\bar{3}m$ ) and tetragonal ( $P4_2/mnm$ ) space groups, the latter derived from the low-temperature tetragonal structure of  $\text{Ba}_2\text{MgReO}_6$ .<sup>9</sup> When refined with a tetragonal model, the degree of distortion at 10 K is very small ( $c/a = 1.0004$ ) but comparable to the values reported for  $\text{Ba}_2\text{MgReO}_6$  ( $c/a = 1.0008$ ). However, there is no sign of peak splitting and/or superlattice reflections within the d-space range of the data (0.502–3.106), and the goodness of fit only shows marginal improvement on lowering the symmetry from  $Fm\bar{3}m$  ( $R_{wp} = 4.65\%$ ) to  $P4_2/mnm$  ( $R_{wp} = 4.43\%$ ). Furthermore, refinements of the 90 K data using a tetragonal model produce a comparable degree of distortion ( $c/a = 1.0004$ ). Thus, we find no evidence of a tetragonal distortion at 10 K using high-resolution neutron data, but neither can we definitively rule out a very small distortion similar to the one reported in single-crystal studies of  $\text{Ba}_2\text{MgReO}_6$ .

The smaller tolerance factor of  $\text{Ba}_2\text{NaOsO}_6$  ( $\tau = 0.974$ ) makes a phase transition to tetragonal symmetry more likely. Its tolerance factor is comparable to  $\text{Sr}_2\text{LiOsO}_6$  ( $\tau = 0.977$ ), and as discussed above, the latter is already tetragonally distorted at room temperature. Furthermore,  $^{23}\text{Na}$  NMR studies reported breaking of the cubic symmetry below 13 K in  $\text{Ba}_2\text{NaOsO}_6$ , creating two distinct orthorhombically distorted Na sites.<sup>8,27</sup> Despite the fact that the 10 K data are in the regime that Lu et al. refer to as the broken local point symmetry (BLPS) phase, the time-of-flight NDP data collected at 10 K were well fit by the cubic  $Fm\bar{3}m$  space group. As with  $\text{Ba}_2\text{LiOsO}_6$ , it is not possible to categorically rule out a small tetragonal distortion, similar to the one reported for  $\text{Ba}_2\text{MgReO}_6$ , but neither is there any visible evidence of such a distortion in our data.

TOF-NPD data for  $\text{Sr}_2\text{LiOsO}_6$  collected at 90 and 10 K were refined with the tetragonal  $I4/m$  space group seen at room temperature. Fits to the data can be found in the Supporting Information. Upon cooling, the  $a$ -axis contracts while the  $c$ -axis expands, increasing the tetragonal distortion of the unit cell. The tetragonal distortion of the Os-centered octahedron increases in a similar manner. The Os–O bond distances in the  $ab$ -plane—1.889(3) Å at 90 K and 1.888(3) Å at 10 K—are similar to the Os–O bond lengths seen in  $\text{Ba}_2\text{LiOsO}_6$  and  $\text{Ba}_2\text{NaOsO}_6$ . However, the axial Os–O bonds are clearly elongated, with values of 1.916(4) Å at 90 K and 1.919(4) Å at 10 K. In percentage terms, the axial bonds are elongated with respect to the equatorial bonds by 0.6% at 300 K, 1.4% at 90 K, and 1.6% at 10 K. A similar elongation of the axial bonds has been reported in the isoelectronic and isostructural  $\text{Sr}_2\text{MgReO}_6$  at a low temperature.<sup>11,28</sup>

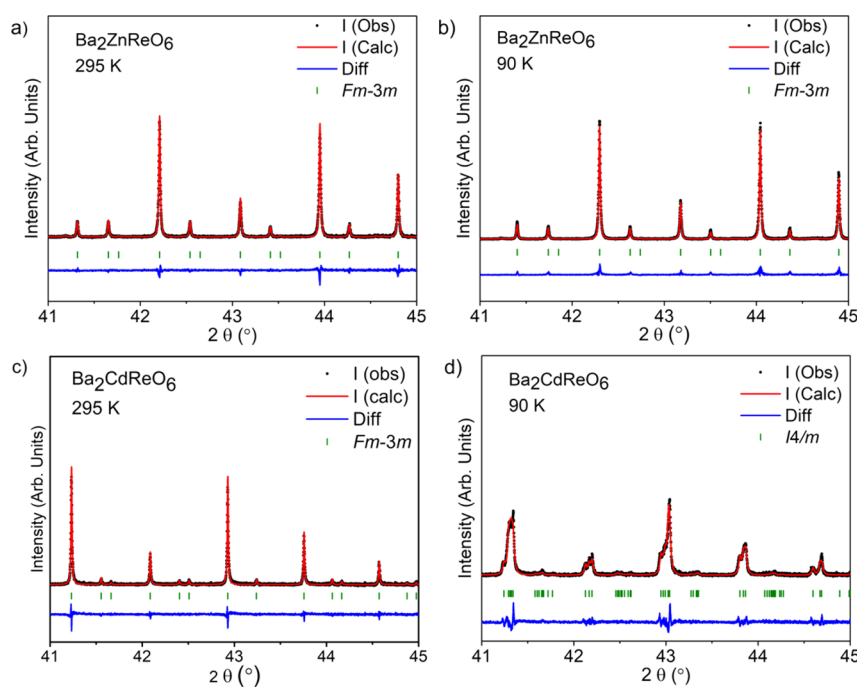
The large neutron absorption cross section of Cd prevented neutron studies of  $\text{Ba}_2\text{CdReO}_6$ , but variable temperature laboratory XRPD data collected on a sample of  $\text{Ba}_2\text{CdReO}_6$  show splitting of the (440) peak into a doublet below 100 K, signifying a cubic-to-tetragonal phase transition (Figure 4).



**Figure 4.** (a) Variable temperature laboratory XRPD data for  $\text{Ba}_2\text{CdReO}_6$  revealing a splitting of the (440) peak as the temperature is lowered. The arrow shows the direction the peak shifts as the temperature is lowered. (b) Temperature dependence of the maximum intensity and FWHM of the (440) peak.

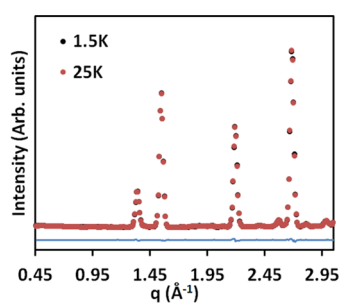
The FWHM of this peak starts to show signs of broadening at higher temperatures, roughly 170 to 180 K. This is in good agreement with recent studies by Hirai and Hiroi, who also observed a cubic-to-tetragonal phase transition at 170 K.<sup>7</sup> Fits to synchrotron X-ray powder diffraction patterns at 90 K clearly reveal the tetragonal distortion, which can be modeled with the  $I4/m$  structure of  $\text{Sr}_2\text{LiOsO}_6$  (Figure 5). Although the two tetragonal structures share the same space group symmetry, the Re-centered octahedra are distorted in the opposite direction than are the Os-centered octahedra in  $\text{Sr}_2\text{LiOsO}_6$ . The Re–O bonds parallel to the  $c$ -axis are shorter, 1.895(6) Å, than those that lie in the  $ab$ -plane, 1.926(8) Å. The opposite direction of the tetragonal distortion is also evident in the distortion of the unit cell. The magnitude of the tetragonal distortion for  $\text{Ba}_2\text{CdReO}_6$  at 90 K,  $c_t/(\sqrt{2}a_t) = 1.002$ , is much smaller than the comparable metric in  $\text{Sr}_2\text{LiOsO}_6$  at 90 K,  $c_t/(\sqrt{2}a_t) = 1.030$ . An analogous  $Fm\bar{3}m$ -to- $I4/m$  structural phase transition resulting in compressed  $\text{ReO}_6$  octahedra has been reported in the isoelectronic compound  $\text{Ba}_2\text{CaReO}_6$  near 120 K.<sup>29</sup>

No sign of magnetic Bragg reflections was observed in any of the samples studied by low-temperature neutron diffraction. While the TOF-NPD data collected on POWGEN are not ideal for observing weak magnetic reflections, the same cannot be said for the constant wavelength data obtained for  $\text{Ba}_2\text{ZnReO}_6$ . The triple-axis spectrometer HB-1A at Oak Ridge National Laboratory is well suited to detect weak magnetic reflections owing to its excellent signal-to-noise ratio,



**Figure 5.** Selected regions of the synchrotron XRD patterns of (a, b)  $\text{Ba}_2\text{ZnReO}_6$  and (c, d)  $\text{Ba}_2\text{CdReO}_6$  at 295 and 90 K. The experimental points are represented by black dots, while red and blue lines show the calculated and difference curves. Green tick marks indicate the positions of the allowed peaks.

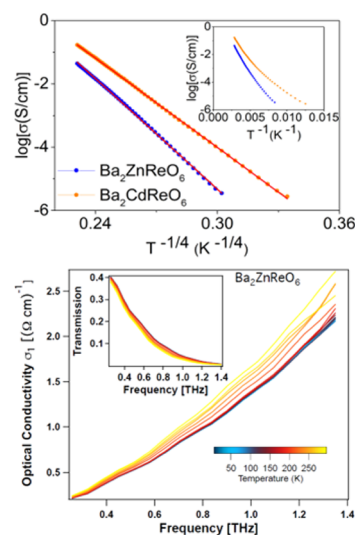
arising from the combined use of a double-bounce monochromator and an analyzer. Figure 6 shows the



**Figure 6.** Comparison of the neutron diffraction pattern above (25 K) and below (1.5 K) the Curie transition temperature in  $\text{Ba}_2\text{ZnReO}_6$ . Black and red dots are data collected at 1.5 and 25 K, respectively, and the blue curve is the difference between the two.

comparison between data collected above (25 K) and below (1.5 K) the Curie temperature. Even though no obvious difference is observed, this result should not be taken as evidence against long-range magnetic ordering. The ordered moments of oxides containing  $5d^1$  ions are sufficiently small; they can fall below the detection limit. The moment of  $0.6 \mu_B$  seen on the same instrument for the  $5d^2$  ion  $\text{Re}^{5+}$  in  $\text{Ba}_2\text{LuReO}_6$  was not far above the detection limit.<sup>30</sup>

**Electrical Conductivity.** Previous studies of  $\text{A}_2\text{MM}'\text{O}_6$  ( $M' = \text{Os}, \text{Re}$ ) double perovskites, where M is a diamagnetic main group ion, have consistently found activated electrical transport.<sup>3,6,7</sup> Given the open-shell configuration of the  $\text{Os}^{7+}$  and  $\text{Re}^{6+}$  ions, Mott insulating behavior is implied. To confirm similar behavior in the compounds discussed here, the electric conductivity of  $\text{Ba}_2\text{ZnReO}_6$  and  $\text{Ba}_2\text{CdReO}_6$  was measured as a function of temperature. As shown in Figure 7, the conductivity increases with increasing temperature, confirming



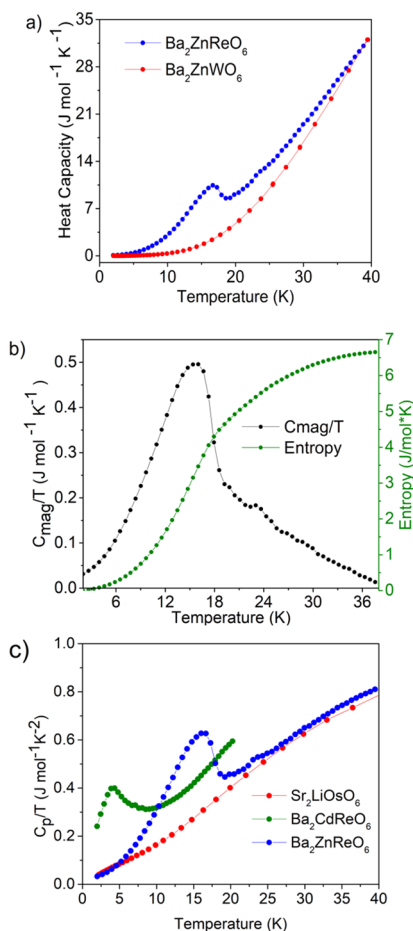
**Figure 7.** Electric conductivity of  $\text{Ba}_2\text{ZnReO}_6$  and  $\text{Ba}_2\text{CdReO}_6$  (top). The inset is the  $\log \sigma$  as a function of  $T^{-1}$ . Time domain terahertz spectroscopy on  $\text{Ba}_2\text{ZnReO}_6$  as a function of frequency and temperature (bottom).

the insulating nature of both materials. The conductivity can be fit to a 3D Mott variable range hopping transport model, where  $\log \sigma$  is a linear function of  $T^{-1/4}$ . Attempts to fit the conductivity to a simple Arrhenius model ( $\log \sigma$  vs  $T^{-1}$ ) were not successful.

Electrical transport measurements on polycrystalline pellets can be complicated by resistance at grain boundaries. To confirm the insulating nature of the bulk, time-domain terahertz spectroscopy (TDTS), which is sensitive both to surface and bulk properties, was performed on  $\text{Ba}_2\text{ZnReO}_6$ . TDTS on a polycrystalline pellet of  $\text{Ba}_2\text{ZnReO}_6$  reveals behavior indicative of a small gap insulator in the approximate

frequency range of 0.25–1.5 THz, with conductivity increasing as the temperature increases (Figure 7). The observation of increasing conductivity with increasing frequency is consistent with the variable range hopping behavior observed in the resistivity data. In general, little temperature dependence beyond increasing conductivity with temperature could be discerned.

**Specific Heat.** The onset of long-range magnetic order in  $\text{Ba}_2\text{ZnReO}_6$  is confirmed by the anomaly present at 16 K in its specific heat (Figure 8). The transition temperature agrees well



**Figure 8.** (a) Heat capacity and (b) magnetic contribution to the heat capacity and entropy release for  $\text{Ba}_2\text{ZnReO}_6$ . (c)  $C_p/T$  for  $\text{Ba}_2\text{ZnReO}_6$ ,  $\text{Ba}_2\text{CdReO}_6$ , and  $\text{Sr}_2\text{LiOsO}_6$ .

with the magnetometry result discussed below. In addition, there is a very small feature at 23 K that, by analogy with specific heat data collected on  $\text{Ba}_2\text{MgReO}_6$ , may indicate a transition into an orbitally ordered state.<sup>6</sup> To estimate the magnetic contribution, the lattice part of the specific heat was subtracted using data measured on the isostructural double perovskite  $\text{Ba}_2\text{ZnWO}_6$ . An integration of the magnetic specific heat yields an entropy release of 6.7 J/(mol·K). Thus, we recover an  $S_{\text{mag}}$  that is intermediate between the pure spin limit ( $S = 1/2$ ) of  $R \cdot \ln(2S + 1) = R \cdot \ln(2) = 5.76$  J/(mol·K) and the full spin–orbit coupling limit ( $J = 3/2$ ) of  $R \cdot \ln(2J + 1) = R \cdot \ln(4) = 11.52$  J/(mol·K). The  $\text{Ba}_2\text{CdReO}_6$  data show an unmistakable peak at 4 K that signals the onset of long-range magnetic order.

**Magnetometry.** The sharp rise in zero-field-cooled (ZFC) and field-cooled (FC) susceptibility observed at  $\sim 16$  K (Figure

9a), as well as the hysteresis seen at 2 K in the isothermal magnetization data (Figure 9f), indicates a ferromagnetic or canted-ferromagnetic ground state for  $\text{Ba}_2\text{ZnReO}_6$ . The transition temperature  $T_C = 16$  K is determined from the dip in the derivative of the susceptibility and this value agrees well with the feature in the specific heat (Figure 8). The saturated moment at 2 K is  $\sim 0.24 \mu_B/\text{formula unit}$  (f.u.), about double the previously reported value.<sup>5</sup>

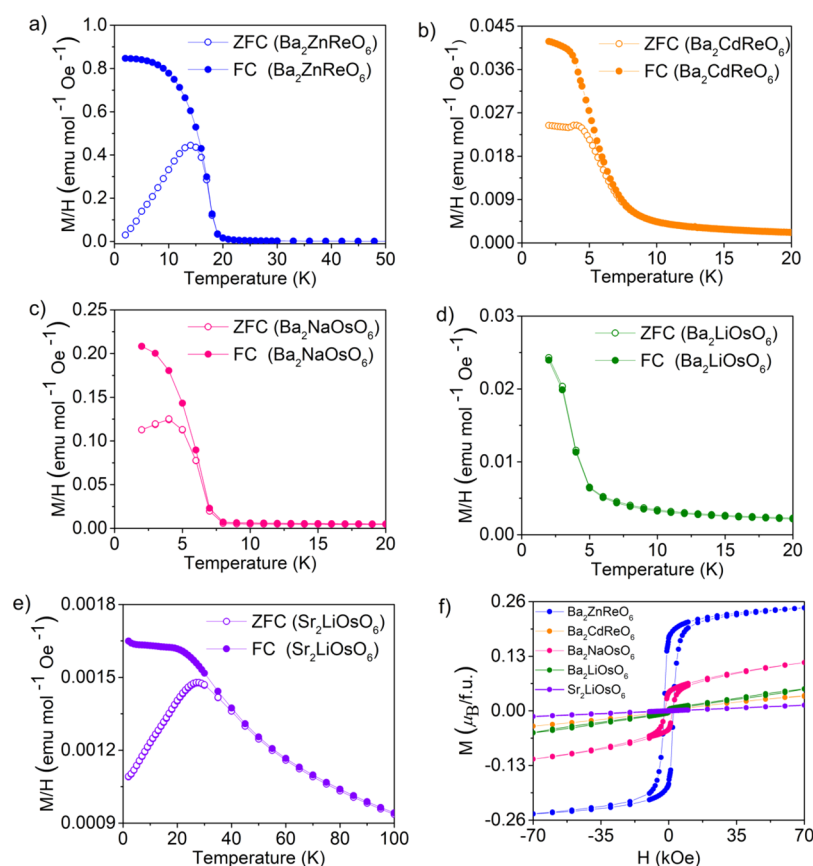
The temperature-dependent magnetic susceptibility of  $\text{Ba}_2\text{CdReO}_6$  shows a rise at temperatures below 10 K (Figure 9b). While this rise could signal many things, the presence of a peak in the specific heat (Figure 8c), taken together with the observation that the isothermal magnetization at 2 K is linear (Figure 9f), suggests antiferromagnetic ordering, with  $T_N = 4$  K. Unlike the resistivity and structural characterization discussed above, this result does not agree with the recent study of Hirai and Hiroi. They observed a clear hysteresis at 2 K, consistent with the canted ferromagnetic structure (Figure 1d), and reported an ordering temperature of 12 K.<sup>7</sup>

A sharp rise in magnetization near 7 K is observed for  $\text{Ba}_2\text{NaOsO}_6$  (Figure 9c). This feature, together with the hysteresis seen in the isothermal magnetization at 2 K (Figure 9f), is consistent with previous reports of canted ferromagnetism.<sup>2,8,27</sup> The saturation magnetization is approximately  $0.11 \mu_B/\text{f.u.}$ , which is smaller by a factor of approximately 2 than the values reported in the literature. A previous report indicates that  $\text{Ba}_2\text{LiOsO}_6$  has an antiferromagnetic ground state with  $T_N \approx 8$  K.<sup>2</sup> The temperature-dependent magnetization data (Figure 9d) do not show a clear cusp indicative of the onset of long range order, but the linear magnetization as a function of applied field at 2 K is at least consistent with antiferromagnetism. Unlike the other compounds studied, there is minimal divergence between FC and ZFC curves, which is also consistent with antiferromagnetic ordering. The temperature dependent magnetization of  $\text{Sr}_2\text{LiOsO}_6$  shows an antiferromagnetic-like cusp at 30 K. However, the absence of anomaly in the specific heat data (vide infra) suggests that the cusp corresponds to freezing of spins into a glassy state. This would be consistent with the significant divergence seen between the zero-field-cooled and field-cooled curves.

The inverse susceptibility in the high-temperature paramagnetic region can be fit to a linear Curie–Weiss plot provided that a temperature-independent parameter (TIP) is included in the fit:

$$\chi = \frac{C}{(T - \theta)} + \chi_0$$

where  $\chi$  represents magnetic susceptibility,  $T$  represents the temperature,  $C$  represents the Curie constant,  $\theta$  represents the Weiss constant, and  $\chi_0$  represents the temperature-independent correction. Given the small sizes of the magnetic moments in these compounds, the Curie–Weiss plots are in general not very linear unless one is careful to subtract out the diamagnetic contribution of the core electrons (which has been done) and include a TIP.<sup>31</sup> From the Curie–Weiss plots, shown in the Supporting Information, the effective moments and Weiss constants can be extracted (see Table 3). The Weiss constant is negative for all five compounds, even  $\text{Ba}_2\text{ZnReO}_6$  and  $\text{Ba}_2\text{NaOsO}_6$ , which are nearly ferromagnetic, as discussed in the Introduction. Not surprisingly, the effective moments are significantly reduced from the spin-only value of  $1.73 \mu_B$ . The observation that the effective moments are slightly larger for the tetragonal compounds,  $\text{Ba}_2\text{CdReO}_6$  and  $\text{Sr}_2\text{LiOsO}_6$ , may



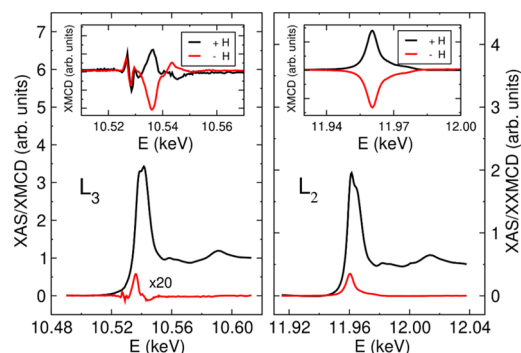
**Figure 9.** Temperature-dependent magnetic susceptibility for (a)  $\text{Ba}_2\text{ZnReO}_6$ , (b)  $\text{Ba}_2\text{CdReO}_6$ , (c)  $\text{Ba}_2\text{NaOsO}_6$ , (d)  $\text{Ba}_2\text{LiOsO}_6$ , and (e)  $\text{Sr}_2\text{LiOsO}_6$  and (f) isothermal magnetization for all five compounds at 2 K.

**Table 3. Ordering Temperatures as well as the Effective Moments and Weiss Constants Obtained from Curie–Weiss Fits to the High-Temperature Susceptibility Data for the  $5d^1$  Double Perovskites**

compound	effective moment ( $\mu_B$ )	Weiss constant, $\theta$ (K)	$\chi_0$ ( $\text{emu mol}^{-1} \text{Oe}^{-1}$ )	ground state	ordering/freezing temperature
$\text{Ba}_2\text{ZnReO}_6$	0.7141(9)	−3.1(5)	$5.1 \times 10^{-5}$	canted ferromagnet	$T_C = 16$ K
$\text{Ba}_2\text{LiOsO}_6$	0.897(1)	−55.7(6)	$3.4 \times 10^{-4}$	antiferromagnet	
$\text{Ba}_2\text{CdReO}_6$	1.04(1)	−65.8(2)	$-2.8 \times 10^{-5}$	antiferromagnet	$T_N = 4$ K
$\text{Ba}_2\text{NaOsO}_6$	0.844(1)	−41.7(6)	$2.2 \times 10^{-4}$	canted ferromagnet	$T_C = 7$ K
$\text{Sr}_2\text{LiOsO}_6$	0.936(1)	−49.4(5)	$2.1 \times 10^{-4}$	spin glass	$T_g = 30$ K

reflect partial quenching of the orbital moment due to the reduction in symmetry, but the effect is subtle.

**X-ray Magnetic Circular Dichroism.** To estimate the size of the spin and orbital moments, a sample of  $\text{Ba}_2\text{ZnReO}_6$  was evaluated using XMCD. Figure 10 shows the normalized X-ray absorption (helicity-averaged) and XMCD spectra collected at the  $L_3$  and  $L_2$  edges of rhenium. Assuming a  $5d^1$  configuration (9 holes), sum rules yield an orbital moment of  $m_l = -0.40(3) \mu_B/\text{Re}$  and an effective spin moment of  $m_s = 1.15(5) \mu_B/\text{Re}$  (the contribution of the magnetic dipole term,  $T_z$ , in the spin sum rule was neglected). The antiparallel alignment of orbital and spin moments is as expected from Hund's third rule for an ion whose available orbitals are less than half-filled. The absolute value of the spin moment exceeds the limit of  $1 \mu_B$  due to the neglect of the magnetic dipole term, but the absolute value of the orbital moment should be a reasonably reliable estimate. If we estimate the total moment to be equal to the saturated moment obtained from magnetometry ( $M_{\text{sat}} = 0.24 \mu_B$ ), we can make a rough estimate of  $0.6\text{--}0.7 \mu_B/\text{Re}$  for the spin moment,  $m_s$ . A similar result is obtained if we use the

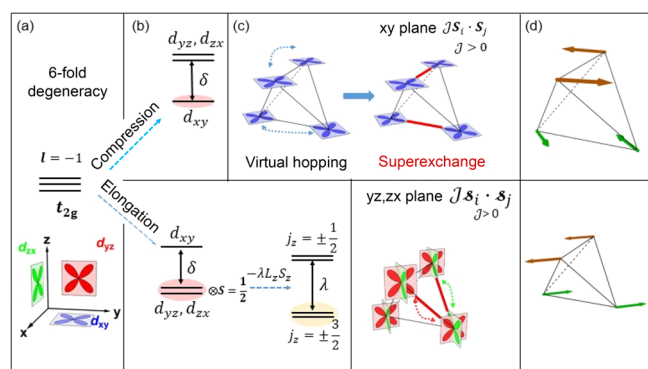


**Figure 10.** Main panels: normalized isotropic (helicity-averaged) and dichroic XMCD spectra at  $\text{Re } L_{2,3}$  edges. Insets: dichroic XMCD spectra for opposite magnetic field directions ( $H = \pm 4$  T) used to obtain “artifact-free” XMCD signals shown in the main panels. A small artifact (approx. 0.5% of absorption jump) is present in the low-energy side of the  $L_3$ -edge XMCD data.



total moment of  $0.2 \mu_B$  estimated for the  $5d^1$  ion  $\text{Os}^{7+}$  in  $\text{Ba}_2\text{NaOsO}_6$  from low-temperature  $\mu\text{SR}$  studies.<sup>4</sup> Our estimates agree reasonably well with the theoretically calculated values for  $\text{Ba}_2\text{NaOsO}_6$  of  $m_l = -0.35 \mu_B/\text{Re}$  and  $m_s = 0.5 \mu_B/\text{Re}$ .<sup>32</sup> The small moment is under the detection limit of neutron diffraction experiments described above.

**Theoretical Modeling.** Given the prior modeling of compounds that are nominally cubic,<sup>14,15</sup> here, we focus on “distorted” materials that already show an observable structural distortion at a higher temperature. Specifically, we examine the effects of two types of tetragonal distortions, either compression or elongation of the oxygen octahedron surrounding the  $5d^1$  ion along the  $c$ -axis. The “spin 1/2” moments that arise from the  $5d^1$  configuration interact via primarily antiferromagnetic superexchange interactions described below, but the orbitals that are occupied and the orbital degeneracy of the ground state are different for the two types of distortions. A summary of our results can also be gleaned from Figure 11.



**Figure 11.** (a)  $t_{2g}$  orbitals,  $d_{xy}$  (blue),  $d_{yz}$  (red), and  $d_{zx}$  (green). (b) Two types of tetragonal distortions of the oxygen octahedron around the  $5d$  ion that lifts the degeneracy in different ways for compression (top row) and elongation (bottom row) along the  $z$ -axis. (c) Virtual hopping pathways between  $5d$  ions (dashed lines) and the resulting superexchange interactions. The dominant antiferromagnetic (AFM) interactions are shown as red bonds. (d) Resulting spin orientations in the magnetic ground state as determined from a four-site mean field theory.

**Compression.** We first consider the case of a uniform compression along one of the principal axes, say the  $z$ -axis, which leads to a preferential occupation of the  $d_{xy}$  orbital on every site. This is the type of distortion that occurs in  $\text{Ba}_2\text{CdReO}_6$ . Our analysis is greatly simplified compared to the cubic case<sup>14,15</sup> for a variety of reasons. First, the orbital angular momentum in this nondegenerate state is quenched, so we do not need to take into account the atomic spin–orbit coupling. Also, we do not need to consider the electric quadrupole–quadrupole interaction since there is no possibility of an electronically driven orbital ordering. We thus only need to derive the magnetic interaction between the  $S = 1/2$  moments following the usual prescription of a strong coupling expansion in powers of the ratio of the hopping amplitude to the Hubbard  $U$ .

The largest hopping amplitude  $t_0$  is between two orbitals in a “head-to-head configuration”. This is the hopping between two  $d_{xy}$  orbitals, both of which lie in the same  $xy$  plane (blue orbital to blue orbital hopping in the  $xy$  plane in Figure 11). We neglect, to begin with, the hopping  $t_1$  between two orbitals in a

“parallel configuration”, i.e., the hopping between  $d_{xy}$  orbitals in two different  $xy$  planes, since  $t_1 \ll t_0$ . Within this approximation, the compressed tetragonal system is described by the simple isotropic Heisenberg Hamiltonian  $H_{\text{eff}} = \mathcal{J} \sum_{\langle i,j \rangle \in xy \text{ plane}} \mathcal{S}_i \cdot \mathcal{S}_j$ , where  $\langle i, j \rangle$  represent nearest-neighbor (NN)  $5d^1$  sites on the  $xy$  planes and the superexchange is given by  $\mathcal{J} = 4t_0^2/U$ . This gives rise to AFM ordering in each  $xy$  plane, but the planes are decoupled when we neglect  $t_1$ . It is easy to see that inclusion of  $t_1$  leads to a weak AFM superexchange  $\mathcal{J}' = 4t_1^2/U$  between the  $xy$  planes, which stabilizes the 3D order. Using mean field theory, we find the magnetic ground state shown in the top row Figure 11d. Note that AFM order is frustrated on the face-centered cubic lattice, and we find Néel AFM order within the  $xy$  plane and canted AFM order between  $xy$  planes with the canting angle determined by the ratio  $\mathcal{J}'/\mathcal{J}$ .

**Elongation.** Next, we consider the case of uniform elongation along the  $z$ -axis of the lattice, which lifts the three-fold degeneracy of the  $t_{2g}$  manifold to favor occupation of the doubly degenerate  $d_{yz}$ ,  $d_{zx}$  orbitals. The four-fold degeneracy of this manifold is split into two doublets by the atomic spin–orbit coupling (SOC). We denote by  $\mathcal{S}_i$  the “isospin 1/2” operator that acts in the lowest Kramers doublet at site  $i$ . Note that isospin  $\mathcal{S}_i^z = \pm 1/2$  actually corresponds to  $j_{\text{eff}} = \pm 3/2$  given the inverted sign of SOC, since the effective orbital angular momentum operator in the  $t_{2g}$  sector has a negative sign relative to the usual  $\mathbf{L}$  operator.

As in the compressive case, in the elongation case too, we can ignore the electric quadrupole–quadrupole interaction that was important for the cubic materials,<sup>14,15</sup> since there is no possibility of an electronically driven orbital ordering. We next use a strong coupling expansion to determine the interaction between isospins  $\mathcal{S}_i$  and  $\mathcal{S}_j$  on NN  $5d^1$  sites. As before, the hopping  $t_0$ , arising from “head-to-head configuration” of orbitals, dominates. In this case, it is hopping between  $d_{yz}$ – $d_{yz}$  orbitals in the  $yz$  plane (red orbital to red orbital hopping in the  $yz$  plane in Figure 11) and between  $d_{zx}$ – $d_{zx}$  orbitals in the  $zx$  plane (green orbital to green orbital hopping in the  $zx$  plane in Figure 11). We ignore the subdominant contribution arising from the hopping  $t_1 \ll t_0$  between orbitals in a “parallel configuration”, such as  $d_{yz}$ – $d_{yz}$  orbitals in the  $xy$  plane (red to red orbital hopping in the  $xy$  plane), and the hopping  $t_2 \ll t_0$  between orbitals in a  $90^\circ$  configuration, such as  $d_{yz}$ – $d_{zx}$  orbitals in the  $xy$  plane (red to green orbital hopping within the  $xy$  plane). It is easy to see that the half-filled-to-half-filled superexchange leads to the usual AFM Heisenberg Hamiltonian for the isospins

$$H_{\text{eff}} = \mathcal{J} \sum_{\langle ij \rangle \in \{yz, zx\}} \mathcal{S}_i \cdot \mathcal{S}_j$$

in the case of elongated octahedron. As a result of the dominant hopping  $t_0$  described above, the AFM interaction  $\mathcal{J}$  acts on pairs of isospin moments connected by bonds in the  $xz$  plane (e.g., the red bond that is highlighted between the two green  $d_{zx}$  orbitals in the lower row of Figure 11c) and in the  $yz$  plane (e.g., the red bond that is highlighted between the two red  $d_{yz}$  orbitals in the lower row of Figure 11c).  $\mathcal{J} \sim t_0^2/U_{\text{eff}} > 0$ , where  $U_{\text{eff}}$  is the energy cost of double occupancy that can be computed by projecting the Kanamori Hamiltonian (with Hubbard  $U$  and Hunds’ coupling  $J_H$ ) onto the lowest Kramers’

doublet. We omit the details of this calculation here since they are not relevant for the qualitative arguments presented here.

The upshot of the effective Hamiltonian described above is that we find, within mean field theory, the AFM ground state shown in the lower row in Figure 11d. This is effectively the type I AFM structure introduced in Figure 1c. We note that the AFM ground states obtained in both the distorted cases, either compression or elongation, have a zero net moment within each unit cell, distinct from a canted FM state.

To conclude, we summarize the key differences between the theoretical results presented here for the distorted  $Sd^1$  double perovskites with the results for cubic  $Sd^1$  systems.<sup>14,15</sup> The effective low-energy Hamiltonians in the cubic case have a complex structure involving the interplay of spin and orbital degrees of freedom, which then leads to two distinct phase transitions:<sup>15</sup> an electronically driven orbital ordering (or quadrupolar order) at a higher temperature  $T_o$  followed by the onset of magnetic ordering at a lower temperature  $T_c$ . In contrast, in the noncubic materials, lattice distortion leads to Kramers doublets on each transition-metal site, a simple AFM superexchange between spin or isospin-1/2 moments, and a single-phase transition to an AFM-ordered state. The AFM states for the distorted cases are in marked contrast to the prediction<sup>14,15</sup> of canted FM order in the cubic case.

## DISCUSSION

The diversity of magnetic ground states found among double perovskites containing  $Sd^1$  ions is unusual. Since  $Re^{6+}$  and  $Os^{7+}$  are isoelectronic and parameters such as spin-orbit coupling and covalency are similar, it is reasonable to assume that the energies of competing magnetic ground states are highly sensitive to structural distortions. Of the nominally cubic, canted ferromagnetic double perovskites,  $Ba_2MgReO_6$  and  $Ba_2NaOsO_6$  have been the most extensively studied. In both compounds, there is experimental evidence for a very subtle crystallographic distortion at low temperatures. The  $P4_2/mnm$  symmetry reported below 33 K for  $Ba_2MgReO_6$  leads to three different Re–O bond lengths.<sup>9</sup> The Re–O bonds are elongated parallel to the  $c$ -axis, while in the  $ab$ -plane, the bonds are compressed in one direction and elongated in the other. The direction of the compressed bonds in the  $ab$ -plane is rotated by  $90^\circ$  with respect to neighboring (001) planes. This distortion, which produces a local orthorhombic symmetry, is also consistent with the peak splitting seen in low-temperature  $^{23}Na$  NMR studies of  $Ba_2NaOsO_6$ .<sup>8,27</sup> Previously published theoretical modeling shows that this pattern of orbital order is essential to produce the superexchange interactions that stabilize a canted ferromagnetic state.<sup>14,15</sup>

The magnetism and phase transitions of  $Ba_2ZnReO_6$  are similar to those that have been documented for  $Ba_2MgReO_6$ .<sup>6,9</sup> The resolution of our low-temperature NPD data is not sufficient to detect the quadrupolar orbital order that has been reported below  $T_q = 33$  K in  $Ba_2MgReO_6$ , but there is a small feature seen at 23 K in the specific heat that may correspond to  $T_q$ . The effective moment ( $\mu_{eff} = 0.7141(9) \mu_B$ ), negative Weiss constant ( $\theta = -3.1(S)$  K), and saturated moment ( $M_{sat} = 0.24 \mu_B/f.u.$ ) of  $Ba_2ZnReO_6$  are all similar to the values reported for  $Ba_2MgReO_6$  ( $\mu_{eff} = 0.68 \mu_B$ ,  $\theta = -14$  K, and  $M_{sat} = 0.3 \mu_B/f.u.$ ). We find an entropy release of 6.7 J/(mol·K) that is smaller than the value of 11.3 J/(mol·K) reported by Hirai and Hiroi on single crystals of  $Ba_2MgReO_6$ .<sup>6</sup> Some of the discrepancy may be due to differences in subtracting the lattice contribution to the specific heat. We use a diamagnetic analog

$Ba_2ZnWO_6$  to estimate the lattice contribution and integrate the data up to  $\sim 40$  K, while Hirai and Hiroi fit the high-temperature data to the sum of two Debye functions and integrate the data up to 80 K.

The crystal structure and bulk magnetic properties of  $Ba_2NaOsO_6$  are very similar to  $Ba_2MgReO_6$  and  $Ba_2ZnReO_6$ , albeit with a slightly lower onset of magnetic order,  $T_C = 7$  K.<sup>2</sup> Although no crystallographic evidence for quadrupolar orbital order has been reported, the  $^{23}Na$  NMR spectra indicate a symmetry-lowering phase transition that is consistent with the quadrupolar phase below 13 K.<sup>8</sup> Here, we show that in the temperature range between  $T_q$  and  $T_C$ , the very subtle crystallographic distortion detected by NMR cannot be detected with high-resolution TOF-NPD data. This observation may help explain why it has been so difficult to find evidence for orbital order in canted ferromagnetic  $Sd^1$  double perovskites.

Among the nominally cubic  $Sd^1$  double perovskites,  $Ba_2LiOsO_6$  is the only compound not reported to be ferromagnetic. The reasons for this anomaly remain enigmatic. The tolerance factor and lattice parameter are very similar to  $Ba_2MReO_6$  ( $M = Mg$  and  $Zn$ ). TOF-NPD data reported here indicate that  $Ba_2LiOsO_6$  and  $Ba_2NaOsO_6$  are isostructural at 10 K. Perhaps,  $Ba_2LiOsO_6$  does not exhibit quadrupolar orbital order, which could be enough to stabilize a colinear antiferromagnetic state over the canted ferromagnetic state. High-resolution, low-temperature single crystal studies of the structures of  $Ba_2LiOsO_6$  and  $Ba_2NaOsO_6$  may help shed light on this issue. Even if it is shown that  $Ba_2LiOsO_6$  does not have quadrupolar orbital order, why this compound behaves differently than its isoelectronic, structural doppelgangers  $Ba_2MReO_6$  ( $M = Mg$  and  $Zn$ ) would remain a mystery.

Finally, we turn our attention to the two compounds where a clear structural phase transition can be seen with conventional powder diffraction techniques:  $Ba_2CdReO_6$  and  $Sr_2LiOsO_6$ . The theoretical modeling presented above explains the emergence of antiferromagnetism in  $Ba_2CdReO_6$  where a cubic-to-tetragonal phase transition at 180 K leads to a compression of the Re–O bonds parallel to the  $c$ -axis. This distortion occurs at a much higher temperature than the cubic-to-tetragonal transition described above for  $Ba_2MgReO_6$  and is likely driven by underbonding of the  $Ba^{2+}$  ions rather than an electronically driven distortion. This distortion results in a different space group symmetry ( $I4/m$  vs  $P4_2/mnm$ ), which leads to preferential occupation of the  $d_{xy}$  orbitals and, in turn, favors antiferromagnetic superexchange coupling within the  $xy$  plane as shown by theoretical modeling. The Weiss constant of  $-65.8(2)$  K would seem to indicate that antiferromagnetic interactions within the  $xy$  plane are of moderate strength. The low  $T_N$  of 4 K likely arises from weak coupling between  $Re^{6+}$  ions in neighboring planes.

Curiously, the results reported in ref 7 agree with the data presented here with the exception of the magnetic ground state. In that work, the magnetic measurements provide strong support for the canted ferromagnetic state seen for the nominally cubic perovskites, unlike what is seen here. Yet both our sample and that in ref 7 are single-phase powders with nearly identical lattice parameters, and both undergo a cubic-to-tetragonal phase transition near 170 K. The only logical conclusion is that the two samples are different in some way that is not easily observed; presumably, there are subtle differences in the stoichiometry and/or defects. While both samples were prepared from similar reagents in sealed silica

tubes, our sample was prepared with a slight overpressure of oxygen at 1000 °C, while the sample studied in ref 7 did not include an overpressure of oxygen and was prepared at 800 °C. This raises the possibility that the oxygen content may be nonstoichiometric, but it is very difficult to say which sample is closest to the ideal stoichiometry. However, the antiferromagnetic ordering of the sample studied here is in better agreement with the predictions of theoretical modeling.

While the tetragonal space group symmetry of Sr<sub>2</sub>LiOsO<sub>6</sub> is the same as Ba<sub>2</sub>CdReO<sub>6</sub>, the Os-centered octahedron undergoes an axial elongation, instead of a compression. This leads to a different occupation of the 5d orbitals, a superposition of d<sub>zx</sub> and d<sub>yz</sub> orbitals. The other documented example of a tetragonal distortion that involves an elongation of the bonds parallel to the *c*-axis is Sr<sub>2</sub>MgReO<sub>6</sub>. Using a combination of NPD, muon spin resonance, specific heat, and magnetization to analyze a polycrystalline sample, Wiebe et al. concluded that Sr<sub>2</sub>MgReO<sub>6</sub> was a spin glass below T<sub>g</sub> ≈ 50 K,<sup>11</sup> but a recent resonant X-ray scattering experiment on a single crystal by Gao et al. showed compelling evidence for a collinear type I AFM (T<sub>N</sub> = 55 K). Here, also the competing magnetic ground states appear to be quite sensitive to subtle perturbations from defects. Theoretical modeling suggests that these compounds should adopt AFM order, like the more recent study of Sr<sub>2</sub>MgReO<sub>6</sub>. It should also be noted that the frustration index, 49 K/30 K ≈ 1.6, is rather small for a spin-glass ground state. It is possible in these compounds that some type of defect is responsible for local disorder that can stabilize the spin-glass state seen here for Sr<sub>2</sub>LiOsO<sub>6</sub> and in the earlier studies on Sr<sub>2</sub>MgReO<sub>6</sub>.

## CONCLUSIONS

The links between the crystal structure and the magnetism of double perovskites containing 5d<sup>1</sup> transition-metal ions have been studied. Ba<sub>2</sub>ZnReO<sub>6</sub> and Ba<sub>2</sub>NaOsO<sub>6</sub> crystallize with the cubic double perovskite structure and retain that structure down to 10 K within the detection limits of TOF-NPD data. Both compounds adopt a canted ferromagnetic structure. Ba<sub>2</sub>ZnReO<sub>6</sub> has a T<sub>C</sub> = 16 K and a saturated moment of 0.24 μ<sub>B</sub>/Re. The orbital moment is estimated to be |m<sub>l</sub>| = 0.4 μ<sub>B</sub>/Re by XMCD analysis. This moment opposes the spin moment, leading to a small net moment on Re of 0.2–0.3 μ<sub>B</sub>, a value too small to be seen in the neutron powder diffraction data obtained here. Ba<sub>2</sub>LiOsO<sub>6</sub> is also cubic and appears to retain the cubic structure down to 10 K but inexplicably adopts an antiferromagnetic ground state. Ba<sub>2</sub>CdReO<sub>6</sub> and Sr<sub>2</sub>LiOsO<sub>6</sub> are both tetragonally distorted (I4/m space group symmetry) at a low temperature, but the Re–O bonds aligned parallel to the *c*-axis are compressed in the former, while analogous Os–O bonds are elongated in the latter. This distortion disrupts the quadrupolar orbital ordering that is thought to stabilize the canted ferromagnetic state, resulting in preferential occupation of the d<sub>xy</sub> orbitals in Ba<sub>2</sub>CdReO<sub>6</sub> and a linear combination of d<sub>yz</sub> and d<sub>xz</sub> orbitals in Sr<sub>2</sub>LiOsO<sub>6</sub>. This pattern of orbital occupation stabilizes antiferromagnetism in Ba<sub>2</sub>CdReO<sub>6</sub>, while Sr<sub>2</sub>LiOsO<sub>6</sub> appears to be a spin glass.

## ASSOCIATED CONTENT

### Supporting Information

The Supporting Information is available free of charge at <https://pubs.acs.org/doi/10.1021/acs.chemmater.1c03456>.

SXPD refinements of Ba<sub>2</sub>ZnReO<sub>6</sub> (Figure S1), SXPD refinements of Ba<sub>2</sub>CdReO<sub>6</sub> (Figure S2), SXPD and NPD refinements of Sr<sub>2</sub>LiOsO<sub>6</sub> (Figure S3), NPD refinements of Ba<sub>2</sub>NaOsO<sub>6</sub> (Figure S4), NPD refinements of Ba<sub>2</sub>LiOsO<sub>6</sub> (Figure S5), CW fit of Ba<sub>2</sub>ZnReO<sub>6</sub> (Figure S6), CW fit of Ba<sub>2</sub>CdReO<sub>6</sub> (Figure S7), CW fit of Sr<sub>2</sub>LiOsO<sub>6</sub> (Figure S8), CW fit of Ba<sub>2</sub>NaOsO<sub>6</sub> (Figure S9), CW fit of Ba<sub>2</sub>LiOsO<sub>6</sub> (Figure S10), refined structural parameters of Ba<sub>2</sub>ZnReO<sub>6</sub> (Table S1), refined structural parameters of Ba<sub>2</sub>CdReO<sub>6</sub> (Table S2), refined structural parameters of Sr<sub>2</sub>LiOsO<sub>6</sub> (Table S3), refined structural parameters of Ba<sub>2</sub>NaOsO<sub>6</sub> (Table S4), and refined structural parameters of Ba<sub>2</sub>LiOsO<sub>6</sub> (Table S5) (PDF)

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### Notes

The authors declare no competing financial interest.

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