Hyperhoneycomb Iridate β-Li_2IrO_3 as a Platform for Kitaev Magnetism

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A complex iridium oxide β-Li_2IrO_3 crystallizes in a hyperhoneycomb structure, a three-dimensional analogue of honeycomb lattice, and is found to be a spin-orbital Mott insulator with $J_{\text{eff}} = 1/2$ moment. Ir ions are connected to the three neighboring Ir ions via Ir-O_2-Ir bonding planes, which very likely gives rise to bond-dependent ferromagnetic interactions between the $J_{\text{eff}} = 1/2$ moments, an essential ingredient of Kitaev model with a spin liquid ground state. Dominant ferromagnetic interaction between $J_{\text{eff}} = 1/2$ moments is indeed confirmed by the temperature dependence of magnetic susceptibility $\chi(T)$ which shows a positive Curie-Weiss temperature $\theta_{\text{CW}} \sim +40$ K. A magnetic ordering with a very small entropy change, likely associated with a noncollinear arrangement of $J_{\text{eff}} = 1/2$ moments, is observed at $T_c = 38$ K. With the application of magnetic field to the ordered state, a large moment of more than 0.35 μ_B/Ir is induced above 3 T, a substantially polarized $J_{\text{eff}} = 1/2$ state. We argue that the close proximity to ferromagnetism and the presence of large fluctuations evidence that the ground state of hyperhoneycomb β-Li_2IrO_3 is located in close proximity of a Kitaev spin liquid.

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The recent surge of interest in the physics of spin-orbit coupling (SOC) in 5*d* transition-metal based oxides was initiated by the discovery of a spin-orbital Mott insulating state in the layered iridate Sr_2IrO_4 [1]. In Sr_2IrO_4, Ir^{4+} ions with five 5*d* electrons are octahedrally coordinated with O^{2-} ions. The large splitting between the t_{2g} and e_g manifolds, due to cubic crystal field, allocates all five electrons into the t_{2g} manifold. SOC of heavy Ir, as large as 0.6 eV, reconstructs the t_{2g} manifold into a lower filled $J_{\text{eff}} = 3/2$ quartet and upper half-filled $J_{\text{eff}} = 1/2$ doublet. The $J_{\text{eff}} = 1/2$ state consists of equal superposition of three t_{2g} orbitals with real and imaginary orbital components and opposite spins, $|J_{\text{eff}} = 1/2\rangle = (1/\sqrt{3})[|d_{xy}, \pm\sigma\rangle \pm |d_{yz}, \mp\sigma\rangle + i|d_{zx}, \mp\sigma\rangle]$, where σ denotes the spin state. Localized $J_{\text{eff}} = 1/2$ moments are produced by the presence of modest Coulomb U in the half-filled $J_{\text{eff}} = 1/2$ band, giving rise to a novel spin-orbital Mott insulator. The $J_{\text{eff}} = 1/2$ Mott state has been established in a number of complex Ir^{4+} oxides [2–4].

One of the most intriguing outcomes unique to the $J_{\text{eff}} = 1/2$ Mott state may be an exotic magnetic coupling derived from the imaginary component of the $J_{\text{eff}} = 1/2$ wave function [5]. In the edge-shared configuration of two adjacent IrO_6 octahedra, $J_{\text{eff}} = 1/2$ moments interact essentially via the two 90° Ir-O-Ir bonds forming a square Ir-O_2-Ir plane. The presence of imaginary components in the wave function yields a destructive interference of superexchange paths between the two Ir-O-Ir bonds. The remnant magnetic interaction, stemming from Hund's coupling, has a form of *bond-dependent ferromagnetic interaction*, which is an essential ingredient of the Kitaev model [6]. The Kitaev model consists of bond-dependent anisotropic and ferromagnetic coupling between the neighboring spins on a honeycomb lattice. If the three bonds sharing the same spin have ferromagnetic coupling only for *x*, *y*, and *z* components, respectively, the bond-dependent polarization of spins conflicts with each other, giving rise to a frustration. The ground state of the Kitaev model with such bond frustration was solved exactly, and known to be a quantum spin liquid. The solid-state platform for the model, however, has been elusive so far. The honeycomb iridates comprising edge-sharing IrO_6 octahedra thus appear to be a promising arena for its materialization.

Possible realization of the Kitaev model in the honeycomb iridates α-Li_2IrO_3 and α-Na_2IrO_3 has triggered intensive investigations both experimentally and theoretically. Both α-Li_2IrO_3 and α-Na_2IrO_3 were discovered to order antiferromagnetically at around 15 K [7–9]. The Curie Weiss temperature is negative, ~ -125 K for Na_2IrO_3 and ~ -40 K for Li_2IrO_3. This means that antiferromagnetic interaction, stronger than the ferromagnetic superexchange coupling, is present [10]. The magnetic ordering of Na_2IrO_3 was found to be a zigzag type [11,12]. This could be ascribed to the coexistence of a Kitaev-type ferromagnetic interaction with dominant antiferromagnetic interactions [13,14]. The weak signature of the Kitaev interaction posed a serious question as to

whether it is possible to approach the Kitaev limit in honeycomb α-Na_2IrO_3 and α-Li_2IrO_3.

The two honeycomb iridates have been so far the sole playground for the realization of the Kitaev model. In the search for a new platform for Kitaev physics, we discovered a new form of Li_2IrO_3, β-Li_2IrO_3, consisting of a three-dimensional analogue of the honeycomb lattice of Ir^{4+} ions which we call the "hyperhoneycomb" lattice. The magnetic susceptibility $\chi(T)$ of β-Li_2IrO_3 evidences the dominant ferromagnetic coupling, very likely representing the Kitaev-type interaction. A noncollinear magnetic ordering is observed at 38 K, which turns into a ferromagnetic state of $J_{\text{eff}} = 1/2$ moments under magnetic fields above 3 T. Theoretical studies on an extended Kitaev model for a hyperhoneycomb lattice demonstrated that the ground state should be also a quantum spin liquid [15]. We argue that the above results place β-Li_2IrO_3 in close proximity to the three-dimensional Kitaev spin liquid.

The polycrystalline samples of β-Li_2IrO_3 were synthesized by a solid state reaction from Li_2CO_3, IrO_2 and LiCl in a molar ratio of 10:1:100. The mixture was pressed into a pellet, and heated at 1100 °C for 24 h, cooled to 700 °C at a rate of 30 K/h and furnace cooled to room temperature. The sample was rinsed with distilled water to remove excess LiCl. The obtained powder product was found to consist of a new phase and a small trace of IrO_2 from the powder x-ray diffraction pattern [16]. The new phase was revealed to be a new form of Li_2IrO_3, β-Li_2IrO_3, isostructural to β-Na_2PtO_3 [23]. The detailed structure was then refined by single crystal x-ray analysis using 50 μm-size crystal grains. The result of the refinement is summarized in Table I.

The crystal structure of β-Li_2IrO_3 is illustrated in Fig. 1(a). It can be described as a distorted cubic close packed arrangement of oxygen atoms with iridium and lithium atoms occupying all octahedral holes in a specific ordered manner. The local structure around an iridium atom is closely related to that of honeycomb α-Li_2IrO_3. Each IrO_6 octahedron is connected with three neighboring IrO_6 octahedra by sharing its three edges [Fig. 1(b)], which gives rise to three Ir-O_2-Ir planar bonds with their planes almost orthogonal to each other. When Ir ions have a $J_{\text{eff}} = 1/2$ moment, the exchange interaction via Ir-O_2-Ir paths very likely gives rise to anisotropic ferromagnetic coupling [5]. The network of iridium ions in β-Li_2IrO_3, depicted in Fig. 1(c), is closely linked to a honeycomb lattice. The 2D honeycomb lattice can be viewed as planar zigzag chains connected at the corners with bridging bonds. In the Ir sublattice of β-Li_2IrO_3, the zigzag Ir chains are connected by the bridging bonds parallel to the c axis. In contrast to the 2D honeycomb lattice, however, the zigzag chains are alternately rotated by 69.9° about the c axis [pink and blue chains in Fig. 1(c)] and connected to the bridging bonds in the layers above and below. Because of the close link to honeycomb structure, the Ir sublattice in β-Li_2IrO_3 may be called hyperhoneycomb. In the hyperhoneycomb Ir sublattice, all the angles between the three Ir-Ir bonds are very close to 120°, and the distances between Ir atoms are almost equivalent (only ~0.2% difference).

As an extension of the Kitaev model, the lattice equivalent to hyperhoneycomb lattice, with competing ferromagnetic polarizations between the three bonds, was studied theoretically [15]. The model could be mapped onto the Kitaev model and is exactly solvable. The ground state is a spin-liquid state as in the original Kitaev model.

TABLE I. Structural parameters of β-Li_2IrO_3. The space group is *Fddd* (No. 70) and $Z = 16$, and the lattice constants are $a = 5.9104(3)$ Å, $b = 8.4562(4)$ Å, and $c = 17.8271(9)$ Å. g and U_{iso} denote site occupancy and the isotropic displacement parameter, respectively. The final R indices are $R = 0.027$ and $wR = 0.0480$.

Atom	Site	g	x	y	z	U_{iso}(Å^2)
Ir	16g	1	1/8	1/8	0.70854(2)	0.00560(4)
O(1)	16e	1	0.8572(5)	1/8	1/8	0.0078(4)
O(2)	32h	1	0.6311(5)	0.3642(3)	0.0383(1)	0.0094(3)
Li(1)	16g	1	1/8	1/8	0.0498(5)	0.0051(11)
Li(2)	16g	1	1/8	1/8	0.8695(7)	0.0155(18)

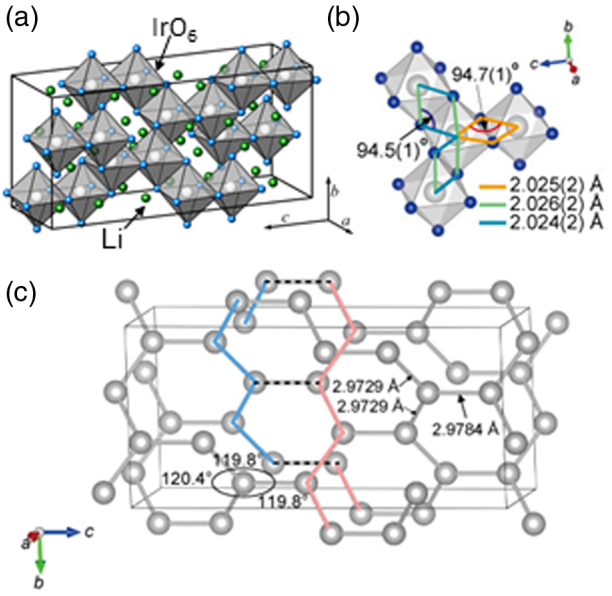

FIG. 1 (color online). (a) Crystal structure of β-Li_2IrO_3. Green, gray, and blue spheres represent lithium, iridium, and oxygen atoms, respectively. (b) Local lattice network of IrO_6 octahedra in β-Li_2IrO_3 [24], displaying Ir-O bond lengths and two different Ir-O-Ir angles obtained from the single crystal analysis [16]. (c) Hyperhoneycomb lattice of Ir ions in β-Li_2IrO_3. The pink and blue lines show the twisted zigzag chains alternating along the c axis. The black dotted lines are the bond bridging the zigzag chains. The numbers indicated are Ir-Ir distances and the angles between Ir atoms.

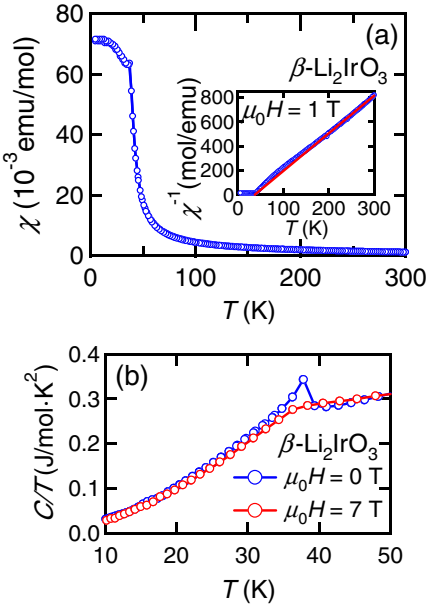

FIG. 2 (color online). (a) Temperature dependence of magnetic susceptibility for β-Li_2IrO_3 under 1 T. The inset shows the temperature dependence of the inverse of magnetic susceptibility. The red solid line delineates the Curie-Weiss fit at high temperatures between 200 and 350 K. (b) Temperature dependence of specific heat divided by temperature recorded at 0 and 7 T.

We may therefore anticipate Kitaev physics and a possible spin-liquid state in β-Li_2IrO_3.

Resistivity measurements indicate that β-Li_2IrO_3 is an insulator with a magnitude of resistivity of the order of 100 Ω cm at room temperature, which is 1 order of magnitude larger than that of α-Li_2IrO_3 [9]. Combined with the presence of the $J_{\rm eff} = 1/2$ moments described below, we conclude that β-Li_2IrO_3 is a spin-orbital Mott insulator as in α-Li_2IrO_3. The temperature dependence of magnetic susceptibility $\chi(T)$, measured on the polycrystalline sample, is shown in Fig. 2(a). The Curie-Weiss fitting at high temperatures between 200 and 350 K yields an effective moment of 1.61 μ_B/Ir, close to 1.73 μ_B/Ir of the ideal $J_{\rm eff} = 1/2$ moment, and a positive Curie-Weiss temperature $\theta_{\rm CW} \sim +40$ K. These imply the formation of $J_{\rm eff} = 1/2$ moments and the dominant ferromagnetic interaction among them. With decreasing temperature, $\chi(T)$ shows a steep increase below ~50 K, followed by a sharp kneelike anomaly at $T_c = 38$ K indicative of magnetic ordering. The specific heat $C(T)$ shows an anomaly at $T_c = 38$ K, evidencing a second order magnetic phase transition. $\chi(T)$ does not show a decrease below T_c, in contrast to those of collinear antiferromagnets. The ground state therefore is very likely a noncollinear antiferromagnet.

The Curie-Weiss temperature $\theta_{\rm CW} \sim +40$ K is very close to $T_c = 38$ K, which at a glance would suggest a mean field like transition. Contrary to this, however, the magnetic entropy associated with the transition, estimated as ~0.2 J/mol K from the specific heat anomaly, is at most a few % of $R \ln 2$, indicative of the presence of strong fluctuations. $\theta_{\rm CW} \sim +40$ K is therefore very likely a consequence of cancellation of ferromagnetic and antiferromagnetic interactions and the actual energy scale of ferromagnetic interactions should be much larger than that estimated from $\theta_{\rm CW}$. This can be reasonably understood as the dominance of bond-dependent ferromagnetic interaction over other antiferromagnetic ones [25]. Frustrations must be involved in the magnetism and the magnetic ordering at $T_c = 38$ K is marginally achieved [26].

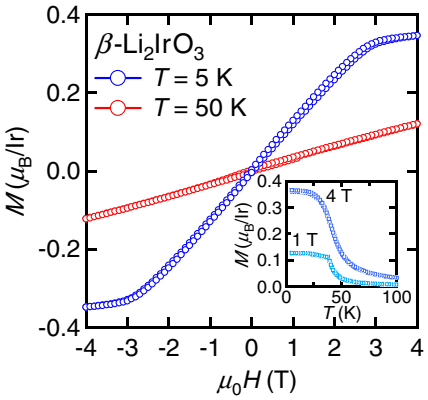

FIG. 3 (color online). Magnetization curve of β-Li_2IrO_3. The blue and red dots are data taken at 5 and 50 K, respectively. The inset shows the temperature dependence of magnetization under a magnetic field of 1 and 4 T.

The ground state is very close to ferromagnetism. The magnetization curve at 5 K (Fig. 3) clearly shows a magnetic-field induced change to a ferromagnetic state. At low fields, the magnetization increases linearly with field. With further increasing field, a kink is observed at $\mu_0 H_c \sim 3$ T, followed by a gradual increase above 3 T. The magnitude of magnetization above 3 T is remarkably large, ~0.35 μ_B/Ir, which is in marked contrast to the weak ferromagnetism with a moment of 0.07 μ_B/Ir arising from the canted $J_{\rm eff} = 1/2$ moments in Sr_2IrO_4 [1]. The ordered moment in other antiferromagnetic iridates such as Sr_2IrO_4 and α-Na_2IrO_3 was reported to be around 0.20–0.36 μ_B/Ir [27,28] and 0.22 μ_B/Ir [12], respectively. The large induced magnetization above 0.35 μ_B/Ir cannot be attributed to canting of $J_{\rm eff} = 1/2$ moments, implying that the $J_{\rm eff} = 1/2$ moments in β-Li_2IrO_3 are about being fully polarized above 3 T. We argue that the kink at $\mu_0 H_c \sim 3$ T may represent the lowest saturation field of $J_{\rm eff} = 1/2$ moments in the magnetization measurement on a polycrystalline sample with randomly oriented grains. The torque measurements on a small single crystal grain in fact indicated the presence of magnetic anisotropy [29]. Under a magnetic field of 4 T, the cusp at 38 K seen in the low field $M(T)$ fades out as shown in the inset of Fig. 3. In accord with this, the peak in C/T is smeared out above 3 T, consistent with a ferromagnetic state of $J_{\rm eff} = 1/2$ moments in the field.

The proximity to a ferromagnetic state, as well as the presence of strong fluctuations, indicates that

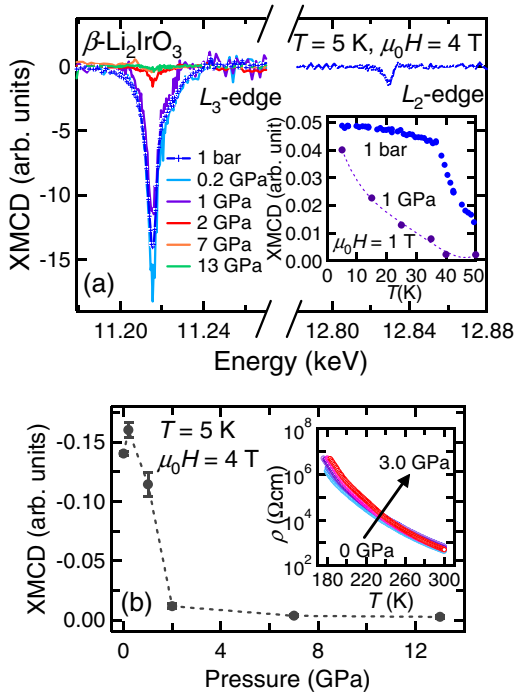

FIG. 4 (color online). (a) XMCD spectra at the Ir $L_{2,3}$ edges for β-Li_2IrO_3. The data are collected at $T = 5$ K, $\mu_0 H = 4$ T. The spectra at the L_3 edge were also measured under high pressures. The inset shows the temperature dependence of the XMCD signal measure at 1 T under ambient pressure and 1–1.5 GPa. The uncertainty of pressure derives from the pressure change with temperature. (b) Pressure dependence of the XMCD signal of the L_3 edge at $T = 5$ K, $\mu_0 H = 4$ T. The inset shows the temperature dependence of resistivity measured at 0, 0.3, 0.9, 1.2, 1.8, 2.4, and 3.0 GPa.

hyperhoneycomb β-Li_2IrO_3 is located at much closer vicinity to the Kitaev spin liquid than α-Na_2IrO_3 and α-Li_2IrO_3. In those honeycomb iridates the weak signature of Kitaev-type interaction was at least partly ascribed to the distortion of planar Ir-O_2-Ir bonds [9,30]. The Ir-O-Ir angles of ~95° for α-Li_2IrO_3 [7] and ~98° for α-Na_2IrO_3 [31] deviate appreciably from the ideal value of 90°. The two Ir-O bonds forming the Ir-O_2-Ir plane are not equivalent, ~5.7% different in length for α-Li_2IrO_3 [7]. In sharp contrast, in β-Li_2IrO_3, the Ir-O-Ir angles are ~94.5° and the difference in the length among the inequivalent Ir-O bonds is only ~0.2%, orders of magnitude smaller than that of α-Li_2IrO_3.

The nature of field-induced moments in the ordered state was investigated by x-ray magnetic circular dichroism (XMCD) on polycrystalline samples [16]. XMCD enables us to separate the spin and the orbital contributions to the magnetic moments. The XMCD spectra at 4 T shown in Fig. 4(a) display a clear asymmetry between the L_3 (13% dichroism) and L_2 (1.4% dichroism) edges, similar to those observed in other iridates [32,33]. Assuming $\langle n_h \rangle = 5$ for the number of $5d$ holes, the net orbital moment is estimated to be $M_L = 0.242\,\mu_B$/Ir from the orbital sum rule for XMCD [34]. The magnitude of magnetization M_{total} measured at 4 T, $\sim 0.35\,\mu_B$/Ir, yields the net spin moment $M_S = M_{\text{total}} - M_L = 0.35 - 0.242 \sim 0.11\ \mu_B$/Ir. The ratio of the orbital and the spin moments $\langle L_z \rangle / \langle S_z \rangle$ is therefore ~4.4, which is very close to 4, expected for the ideal $J_{\text{eff}} = 1/2$ moments [35]. The $J_{\text{eff}} = 1/2$ picture works very well in β-Li_2IrO_3.

The magnetic-field-induced ferromagnetic moments were found to be suppressed rapidly by applying pressure. As shown in Figs. 4(a) and 4(b), the XMCD signal starts to decrease above a pressure of 1 GPa accompanied by the strongly broadened transition, and almost vanishes above 2 GPa. The resistivity data shown in the inset of Fig. 4(b) indicate that β-Li_2IrO_3 remains insulating above 2 GPa. This implies that the vanishing of the XMCD signal is due to the rearrangement of $J_{\text{eff}} = 1/2$ moments rather than the disappearance of localized $J_{\text{eff}} = 1/2$ moments, suggesting the presence of energetically almost degenerate states near the ground state.

We argue that the small structural distortion of Ir-O_2-Ir bonds and the almost ideal $J_{\text{eff}} = 1/2$ local wave function in β-Li_2IrO_3 result in the predominance of Kitaev-type ferromagnetic interaction over the other interactions, including the nearest-neighbor Heisenberg and the long-range interactions. The other interactions, however, are not zero and superposed onto Kitaev-type ferromagnetic interaction, which we argue stabilize marginally the noncollinear ordering below $T_c = 38$ K. The noncollinear spiral order is indeed envisaged to manifest itself at the critical boundary to the Kitaev liquid in the theoretical phase diagram of the extended Kitaev-Heisenberg model for 2D honeycomb lattice [36] and also for 3D analogues [37]. Under pressure, the intricate balance between Kitaev-type and other interactions is modified, resulting in a different magnetic ground state.

In summary, a complex Ir^{4+} oxide, β-Li_2IrO_3, crystallizes in an intriguing structure, the hyperhoneycomb, which is a three-dimensional analogue of two-dimensional honeycomb structure. $J_{\text{eff}} = 1/2$ moments on the hyperhoneycomb lattice, connected by the planar Ir-O_2-Ir bonds, provide a promising playground towards the realization of Kitaev spin liquid. The magnetization data clearly support the predominance of Kitaev-type ferromagnetic interaction and the close proximity of β-Li_2IrO_3 to the Kitaev spin liquid state. However, the presence of other interactions, small but finite, appears to stabilize marginally a noncollinear ordering below $T_c = 38$ K. Those results suggest that β-Li_2IrO_3 be the most promising candidate for the long-sought Kitaev spin liquid to date.

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