

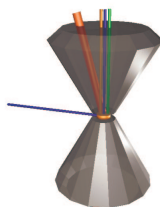


Applications of NRIXS and NFS Techniques at High Pressures

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Collaboration

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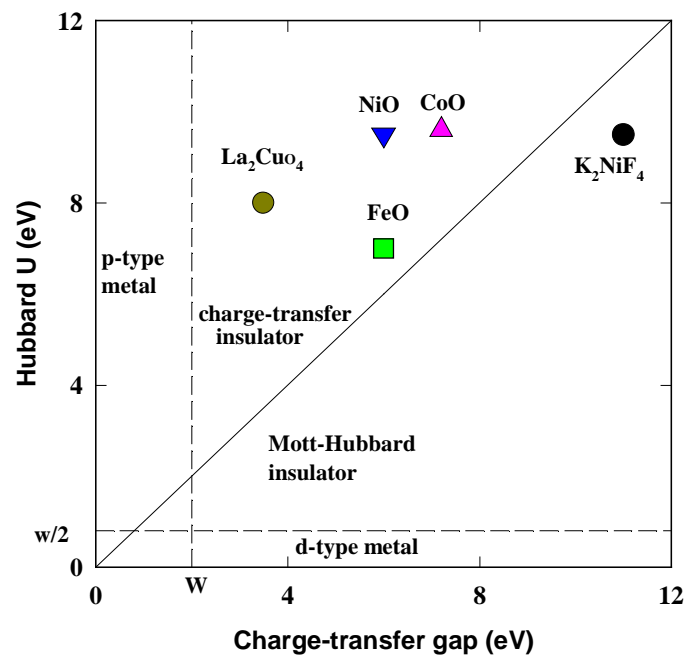
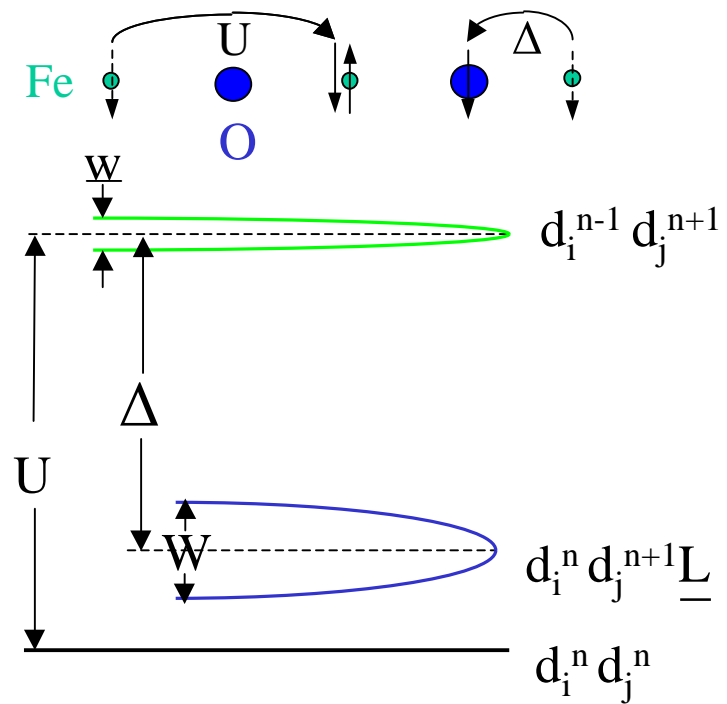
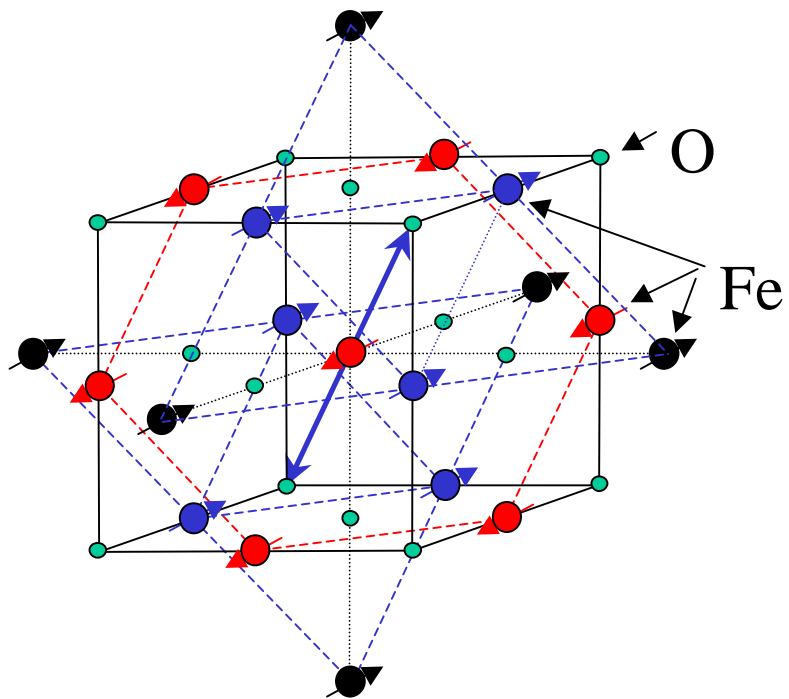
Support

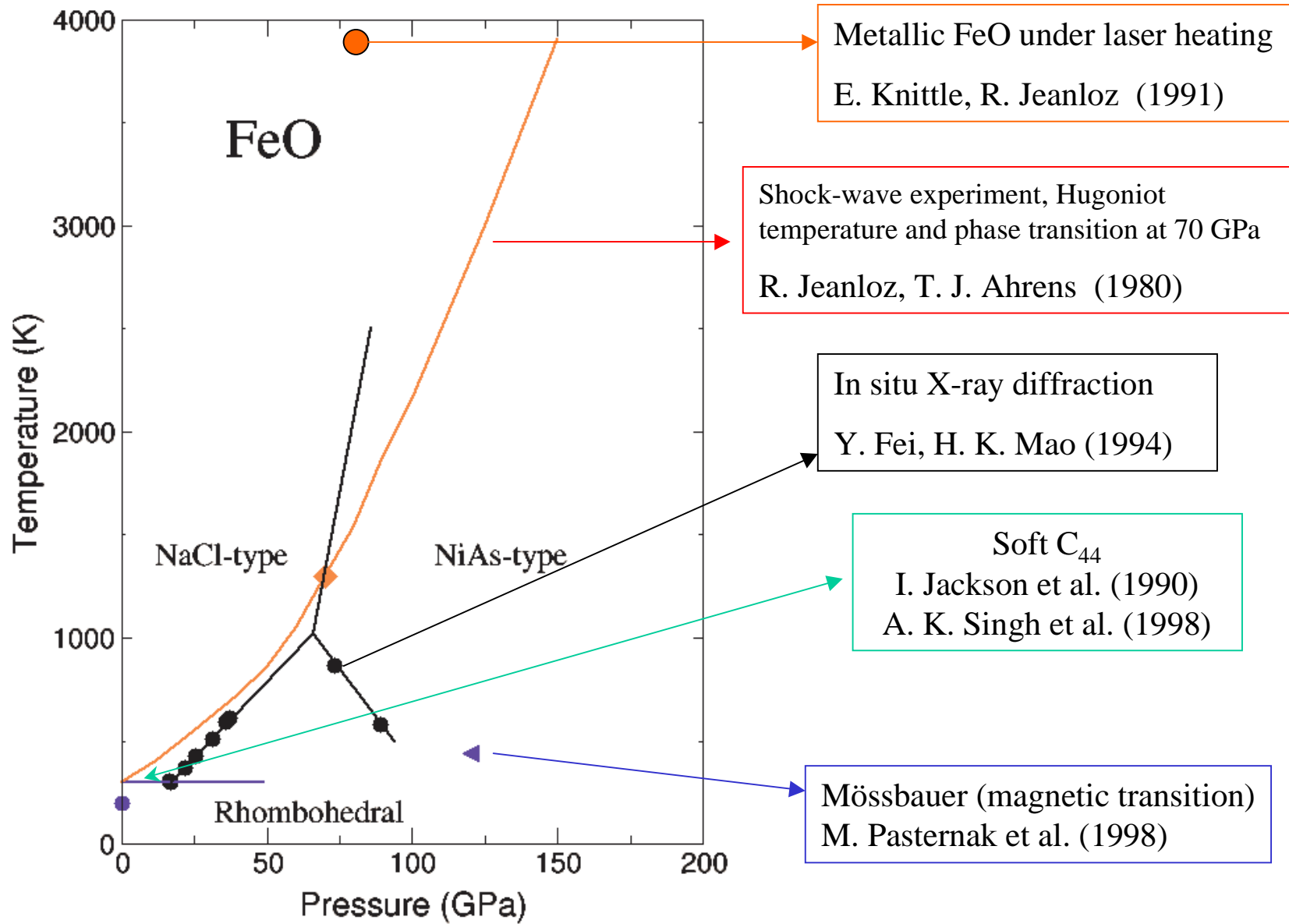
DOE (DE-FG02-02ER459555)
NSF

W. M. Keck Foundation

Outline

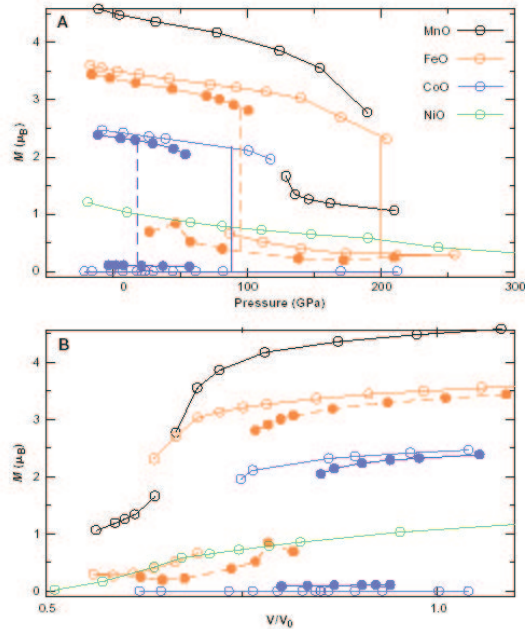
- Electronic correlations in simple oxides
- Phonon and magnon excitations in iron oxide - magnetoelastic coupling
- P-T magnetic phase diagram of $\text{Fe}_{0.94}\text{O}$
- Insulator-metal transition in $\text{Fe}_{0.94}\text{O}$
- Elastic properties of iron from NRIXS studies



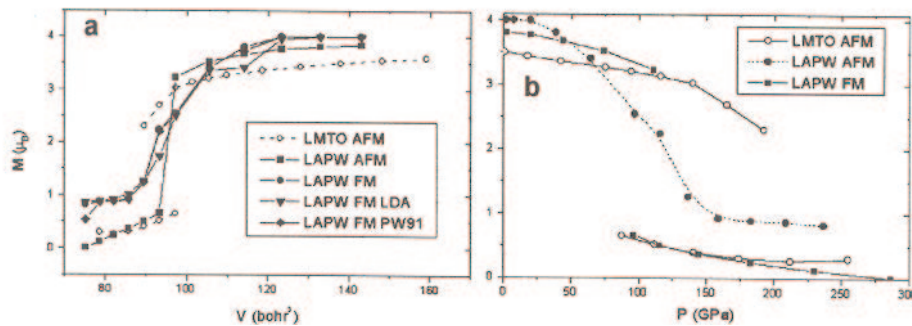


Magnetic collapse in transition metal oxides

Cohen, Mazin, Isaak, Science 1997



R. E. Cohen et al., MRS Symp proc. 1998



High-spin to low-spin transition

I. Jackson and A. E. Ringwood (1981)

$$\Delta G = \Delta E - P\Delta V + T\Delta S$$

$$\Delta E = Nn\{\pi - \Delta(r)\}, \Delta \sim \Delta_0(r_0/r)^5$$

For cubic (B1) FeO: $P_{tr} = 50$ GPa

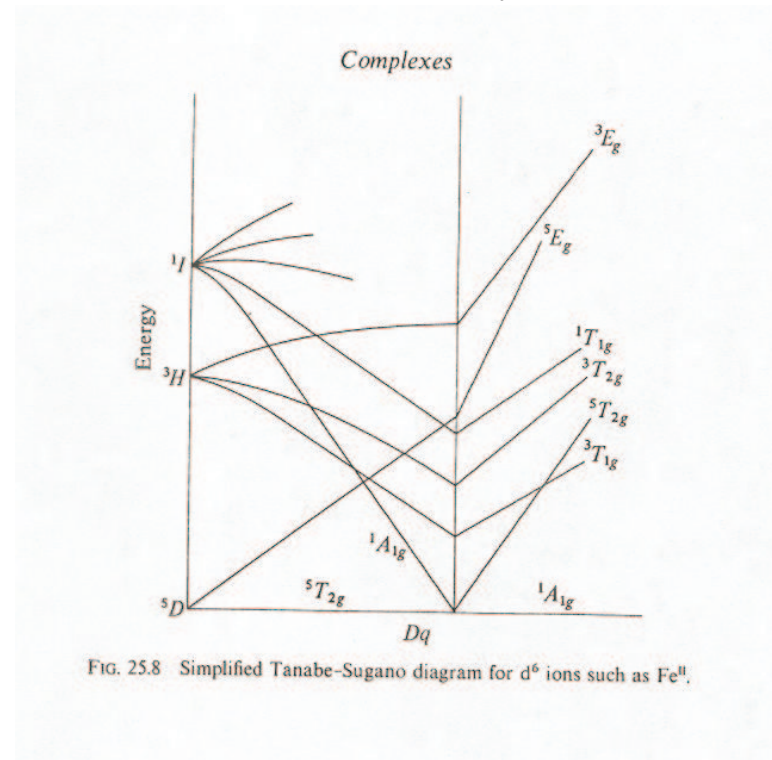
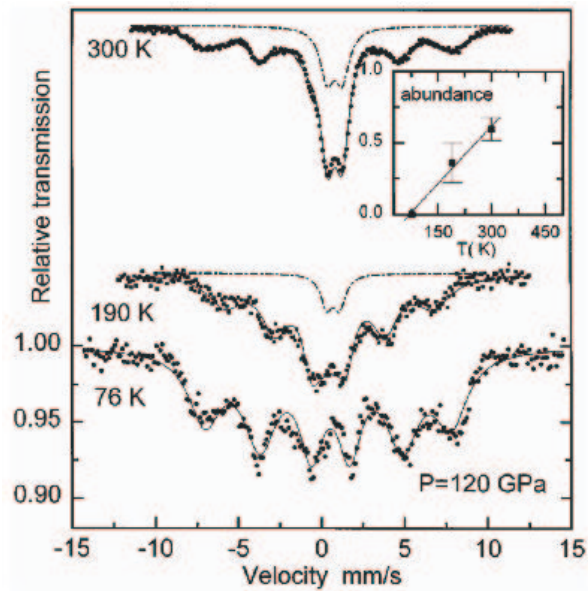


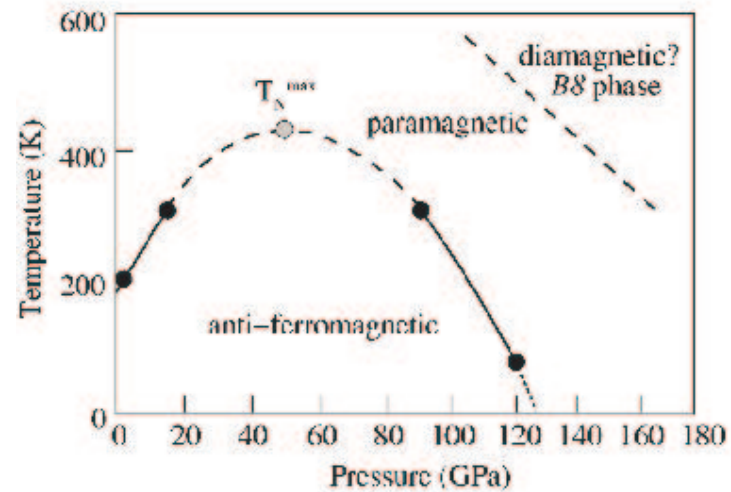
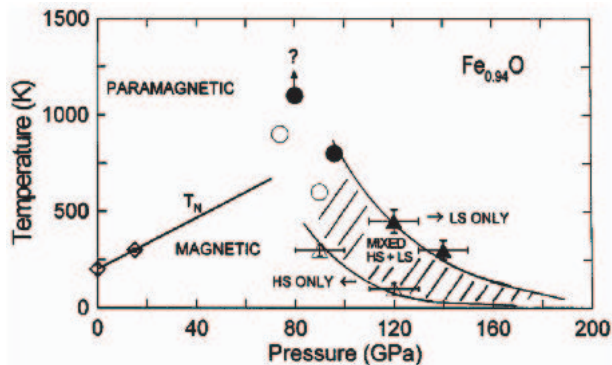
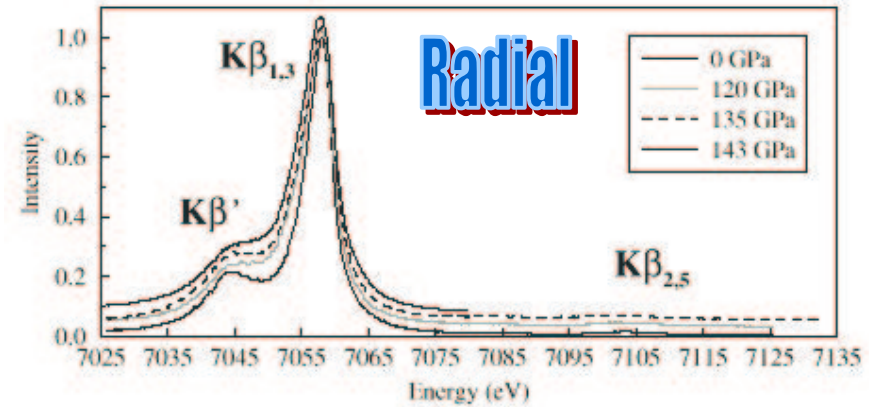
FIG. 25.8 Simplified Tanabe-Sugano diagram for d^6 ions such as Fe^{II} .

Comparison of Mössbauer and X-ray emission results: FeO

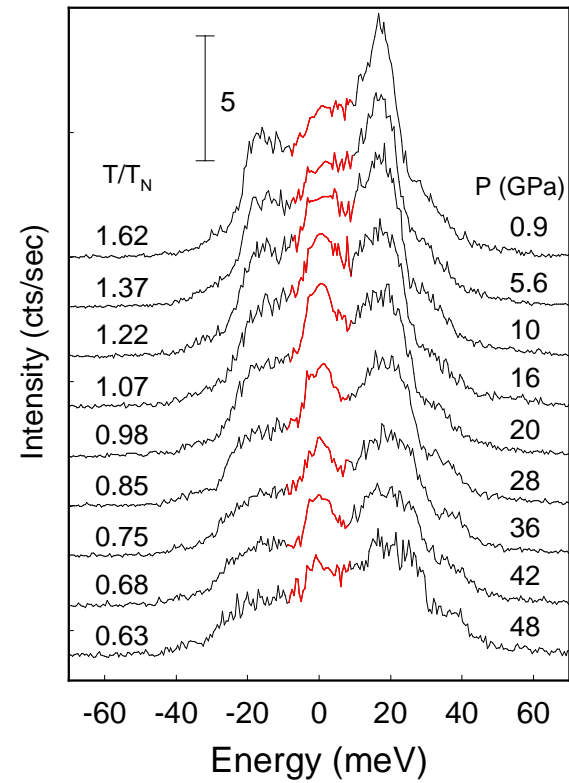
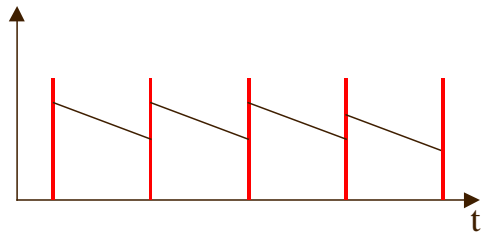
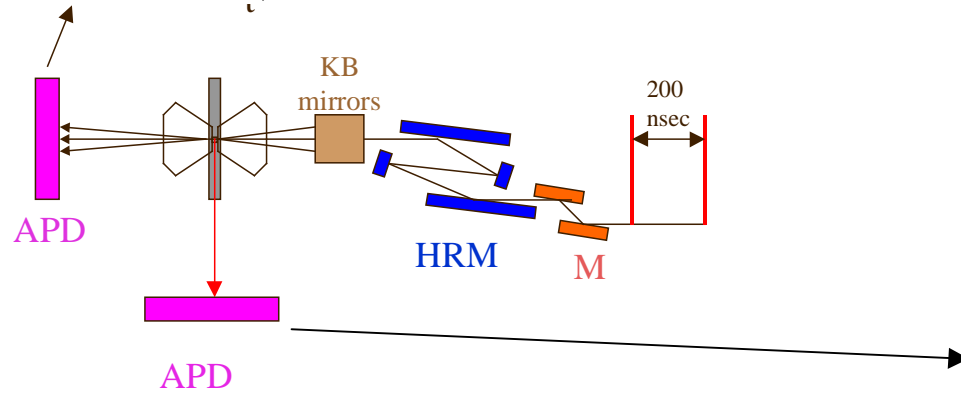
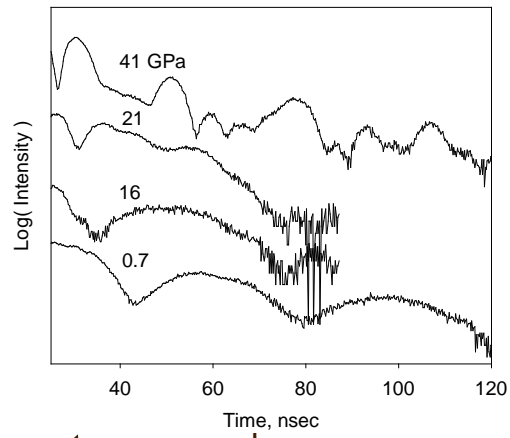
M. P. Pasternak et al. Phys. Rev. Lett. (1997)

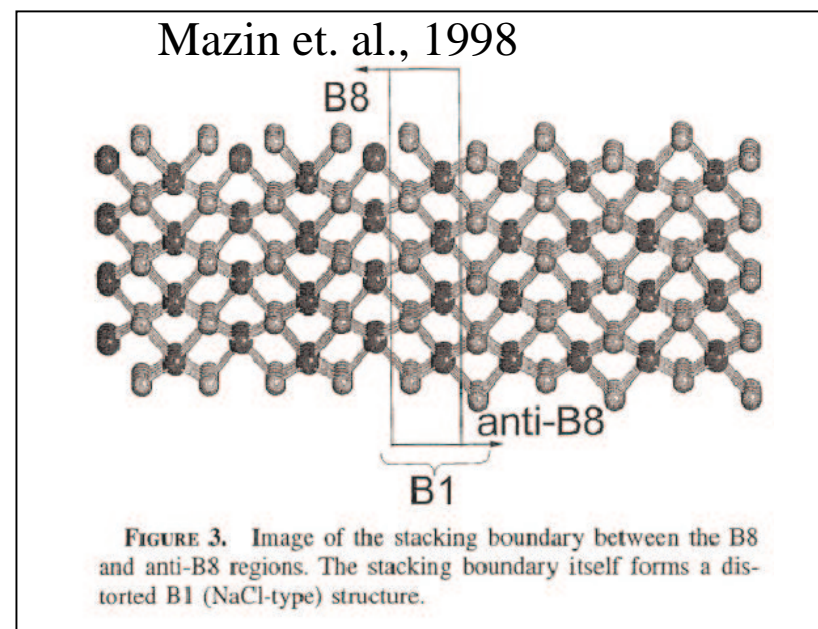
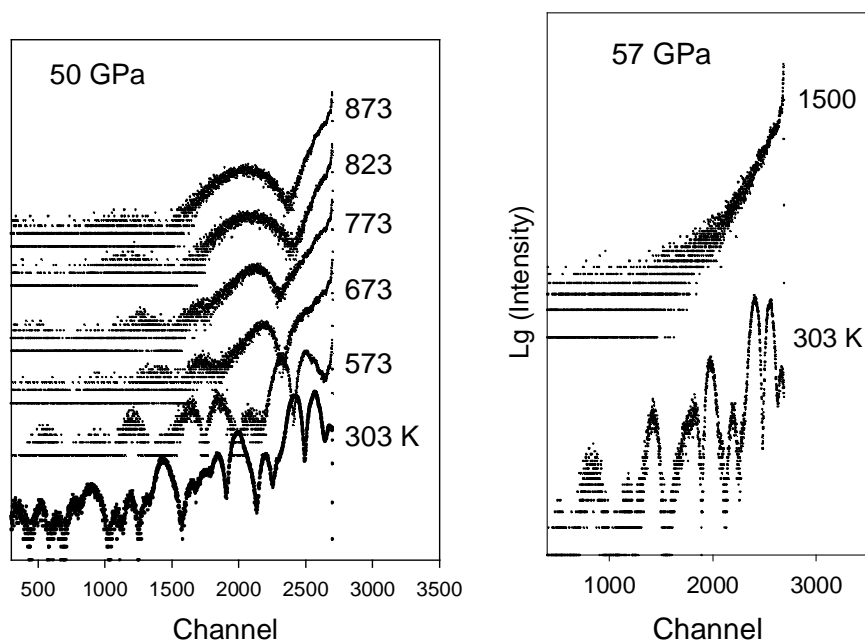
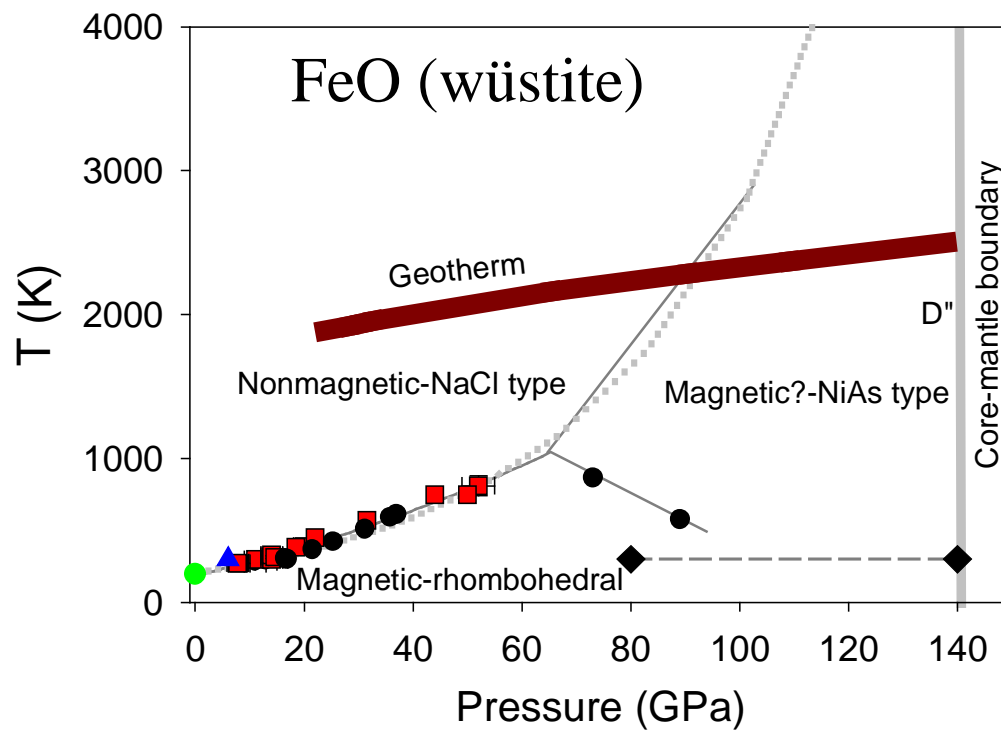
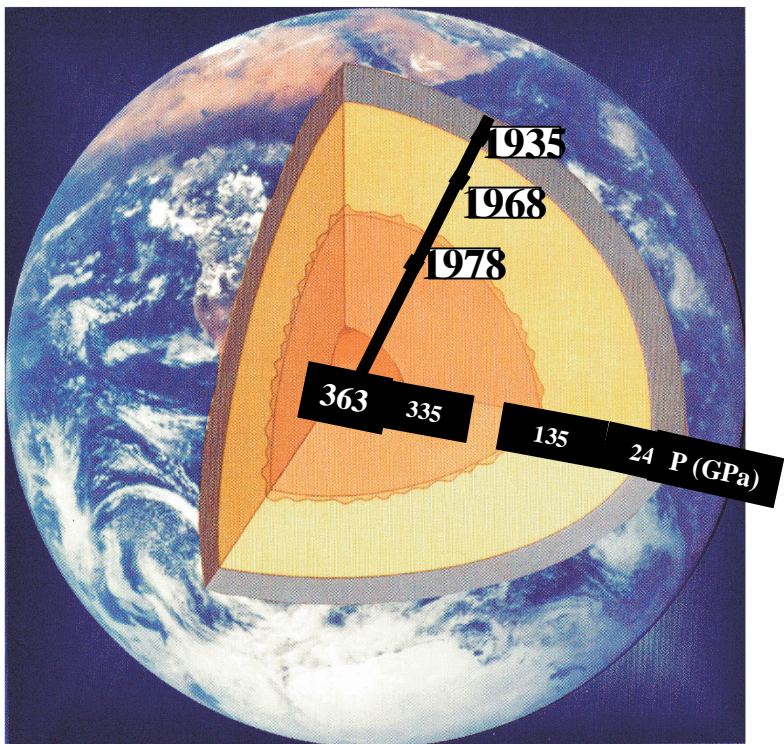


J. Badro et al. Phys. Rev. Lett. (1999)

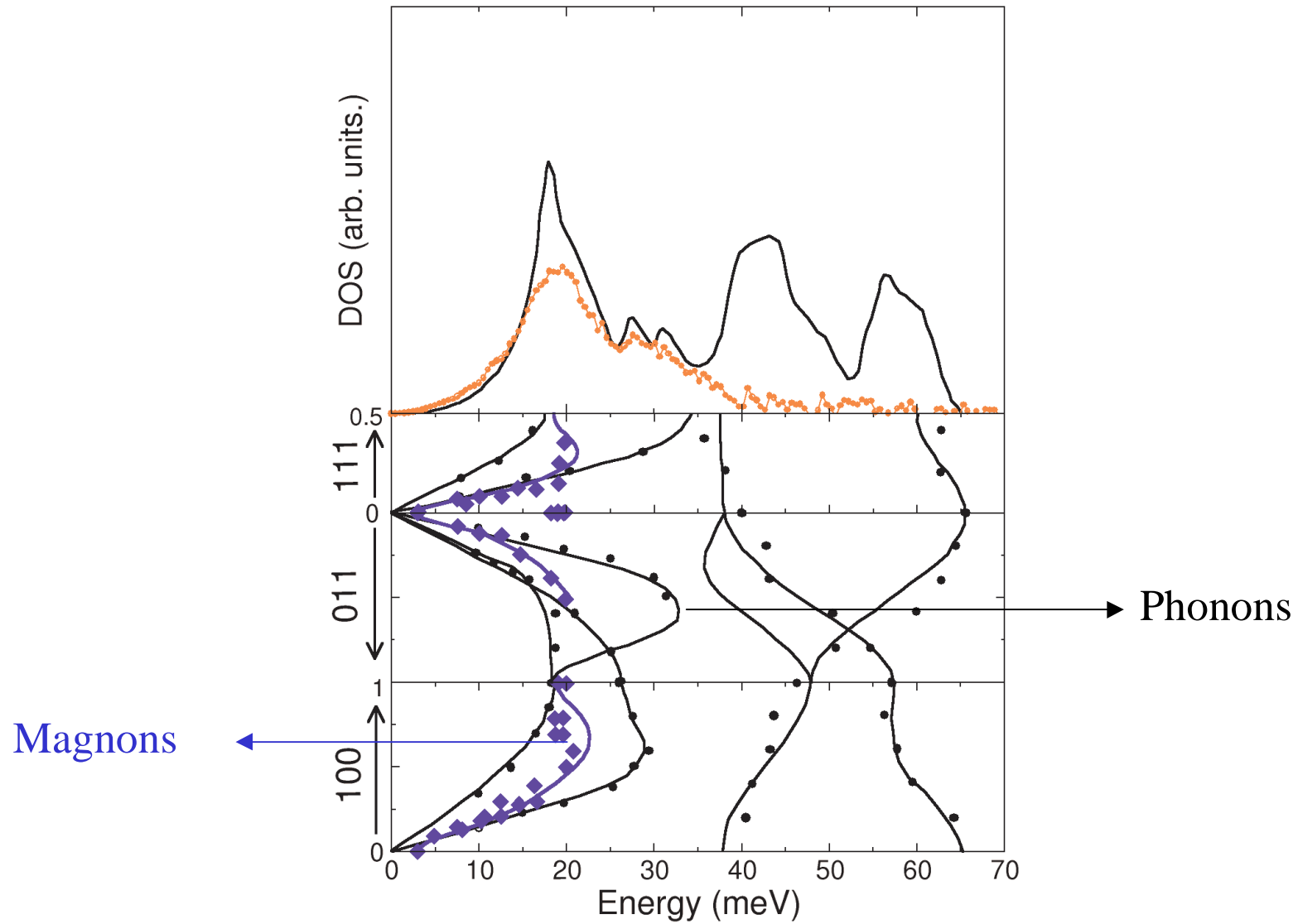


Nuclear inelastic scattering set-up (W. Sturhahn, E. Alp, M. Hu)

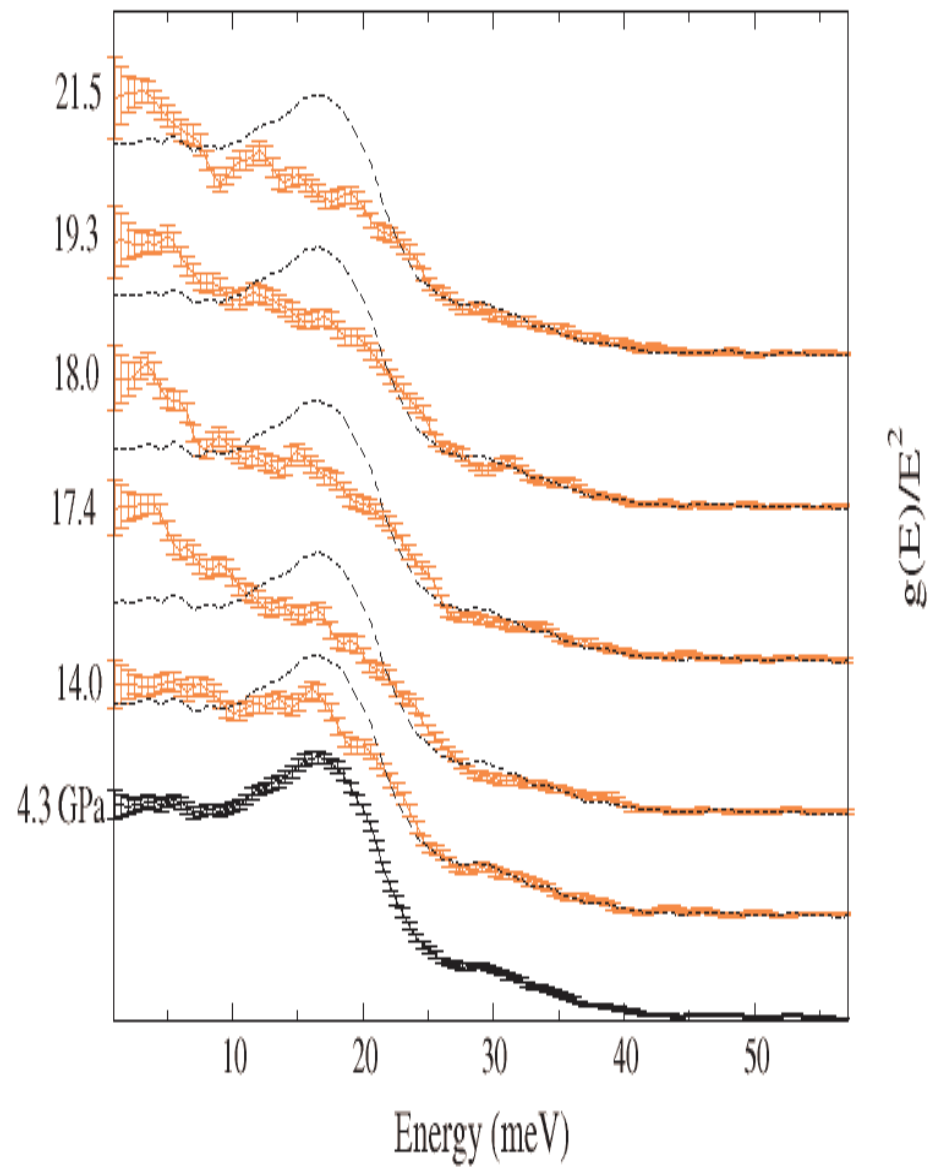
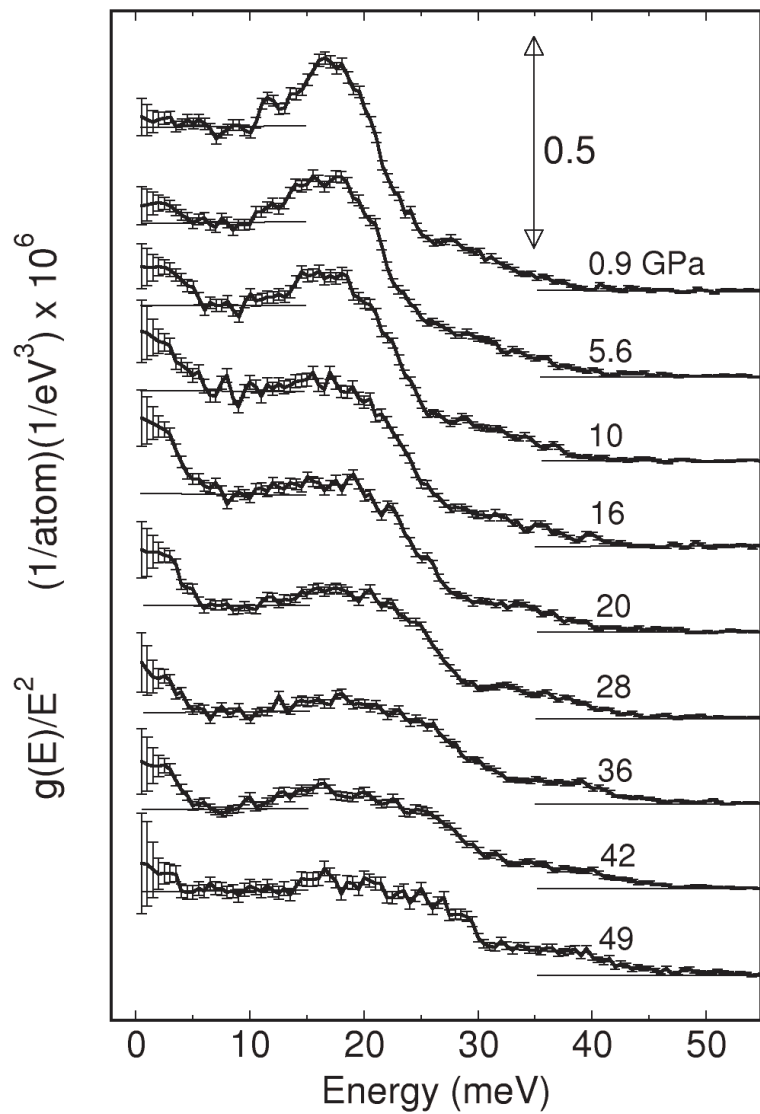




Density of states (DOS) , compared with neutron data by Kugel (1977)



Debye-like part of DOS : $g(E)/E^2$

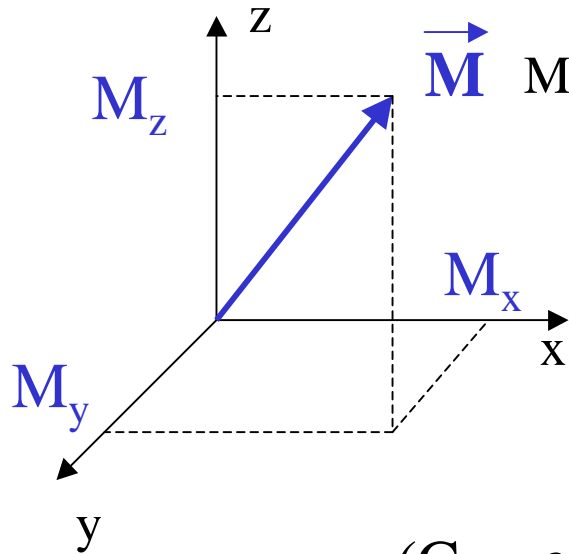


Magnetoelastic coupling (cubic crystal)

$$F = B_1(\alpha_1^2 e_{xx} + \alpha_2^2 e_{yy} + \alpha_3^2 e_{zz}) + B_2(\alpha_1 \alpha_2 e_{xy} + \alpha_2 \alpha_3 e_{yz} + \alpha_1 \alpha_3 e_{xz}) \quad \text{Magnetoelastic energy}$$

$$+ (1/2)C_{11}(e_{xx}^2 + e_{yy}^2 + e_{zz}^2) + (1/2)C_{44}(e_{xy}^2 + e_{yz}^2 + e_{zx}^2) \quad \text{Pure elastic contribution}$$

$$+ C_{12}(e_{yy}e_{zz} + e_{xx}e_{zz} + e_{xx}e_{yy})$$



\vec{M} Magnetic moment, in antiferromagnet $\vec{M} = \vec{M}_1 - \vec{M}_2 = 2\vec{M}_1$

$$\alpha_1 = \frac{M_x}{|\mathbf{M}|} \quad \alpha_2 = \frac{M_y}{|\mathbf{M}|} \quad \alpha_3 = \frac{M_z}{|\mathbf{M}|}$$

Minimize F, and find (Kittel, 1949)

$$e_{ii} = \frac{(C_{12} - \alpha_i^2(C_{11} + 2C_{12}))}{(C_{11} - C_{12})(C_{11} + 2C_{12})} B_1, \quad e_{ij} = \frac{\alpha_i \alpha_j}{C_{44}} B_2$$

Magnetoelastic coupling

(Peletninskii, 1960)

From equations of motion of sound in antiferromagnet along magnetization axis (111):

$$(\omega^2 - \omega_s^2)(\omega^2 - \omega_m^2) = M^2 B_2^2 k^2 g \Omega / 2\rho$$

ω_s - frequency of acoustic sound branch

$\omega_m^2 = \Omega g M (\beta + \alpha k^2)$ - magnetic dispersion branch

$$\Omega = g M (\beta + 2\gamma)$$

α, β, γ - exchange, and magnetic anisotropy

M - magnetic moment of the magnetic sublattice

B_2 - magnetoelastic coupling

ρ - density of the material

k - wavevector

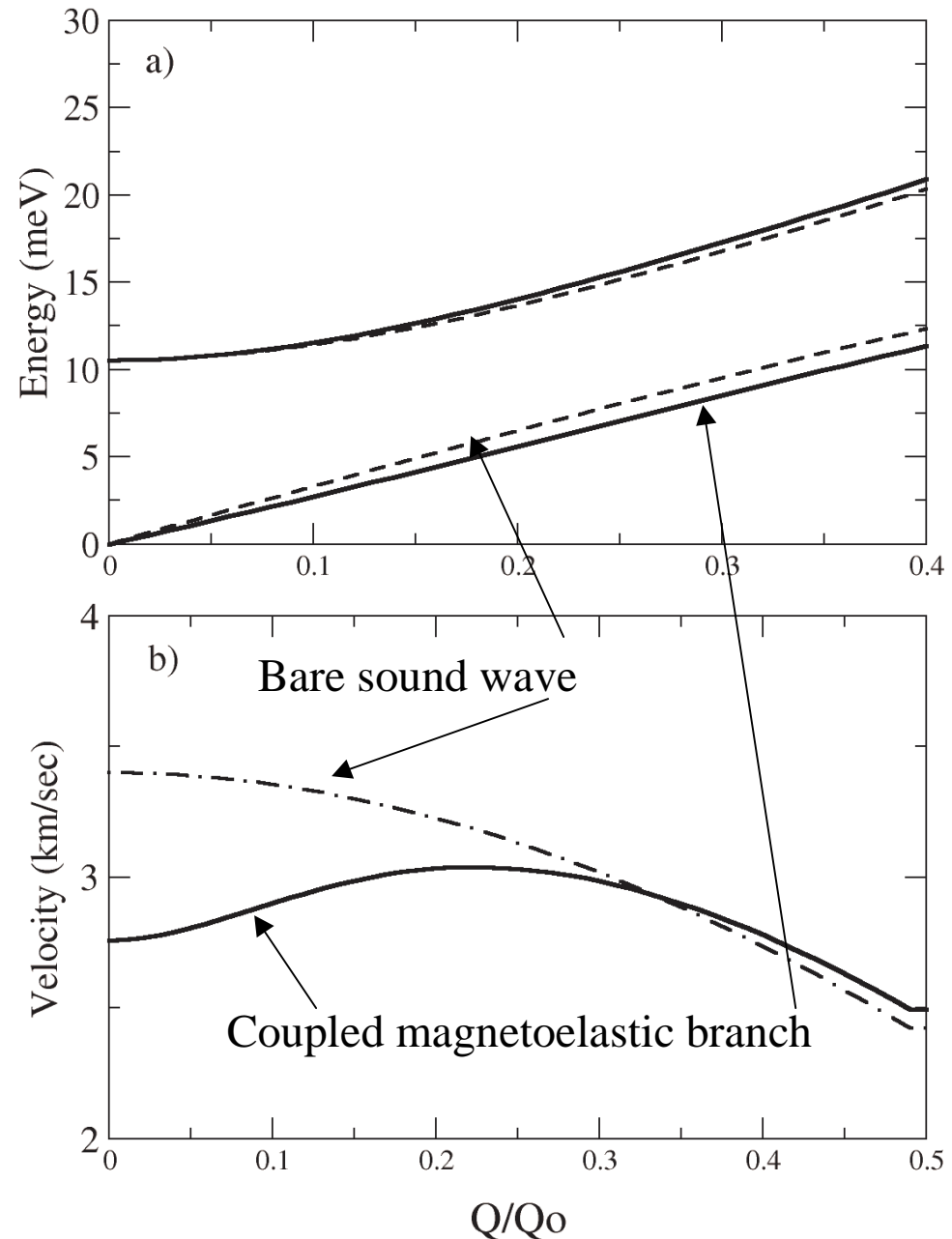
g - gyromagnetic ratio

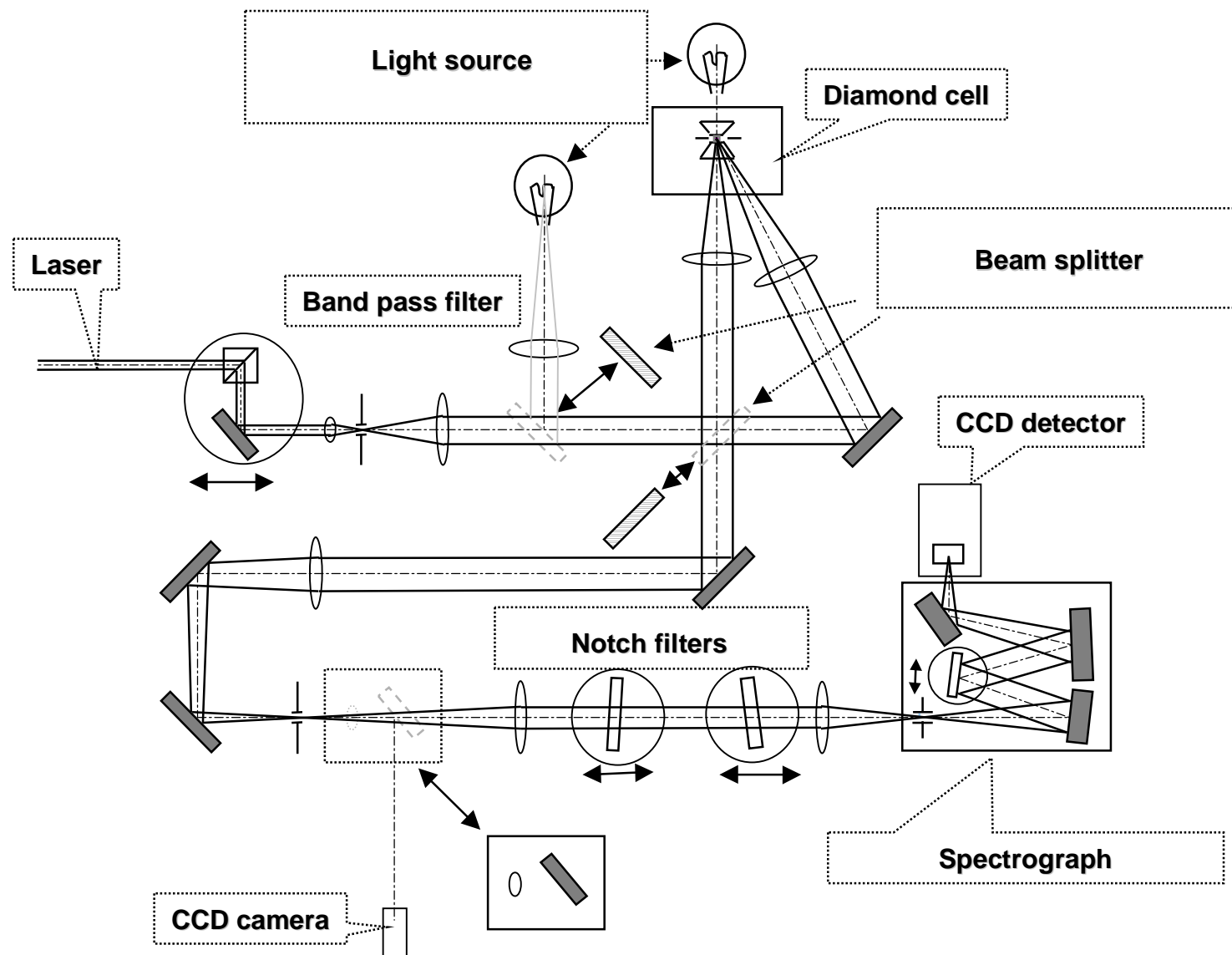
$B_2 = 2.5 \cdot 10^{10} \text{ erg/cm}^3$, $M = 1400 \text{ Gauss}$,

$\alpha = 10^{-6} \text{ erg cm}$, $\rho = 6.2 \text{ g/cm}^2$, $\gamma = 0$

$\Omega = 2.6 \text{ THz}$

Estimated coupling at 28 GPa

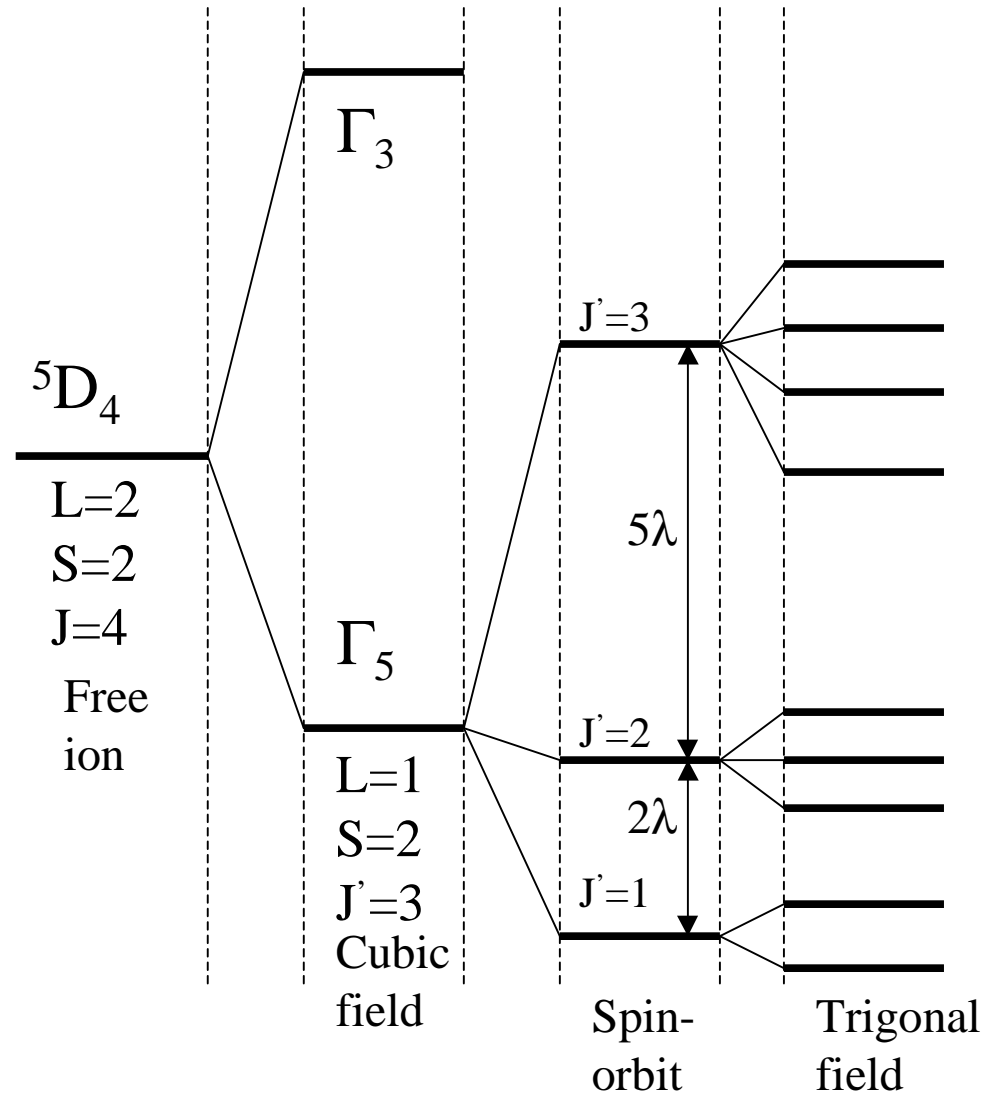
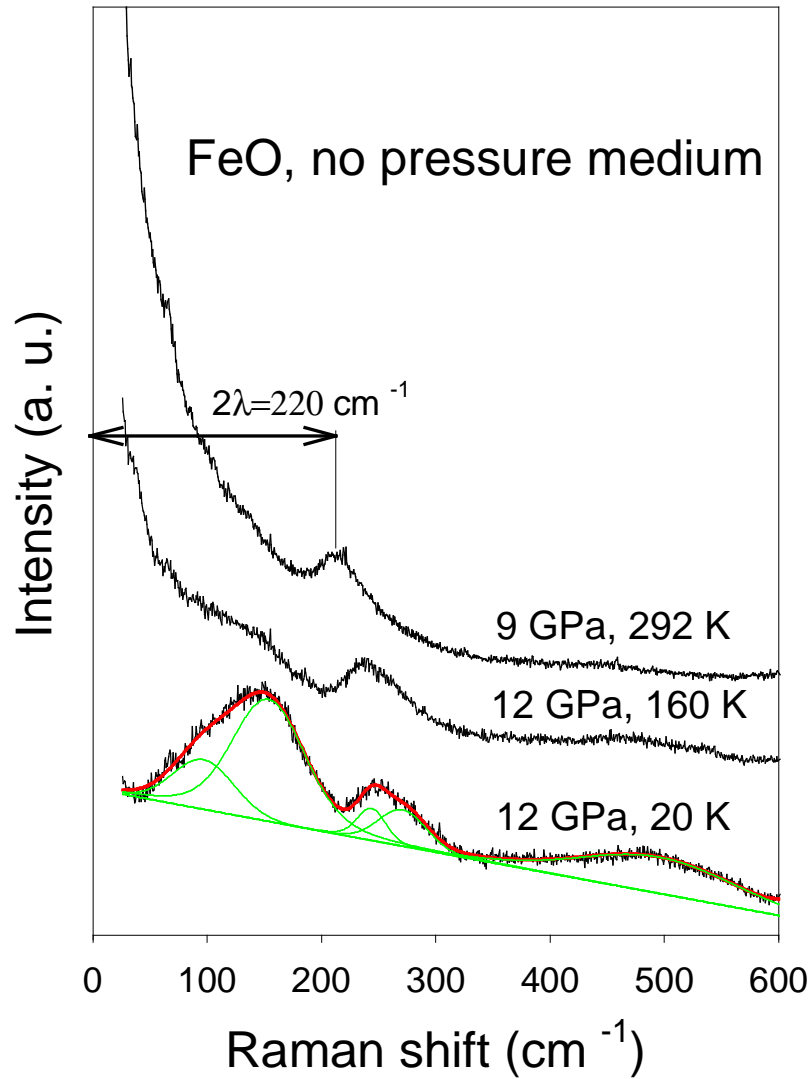




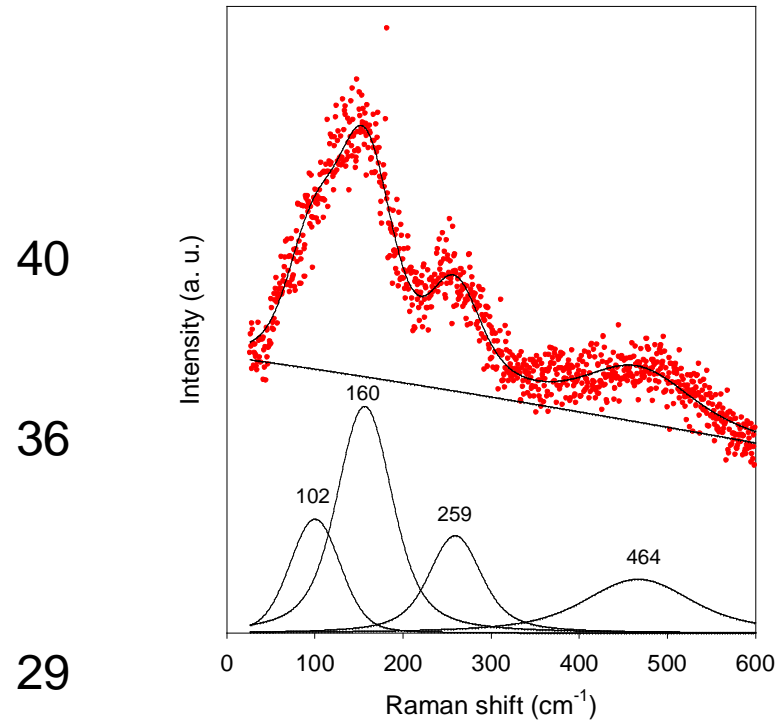
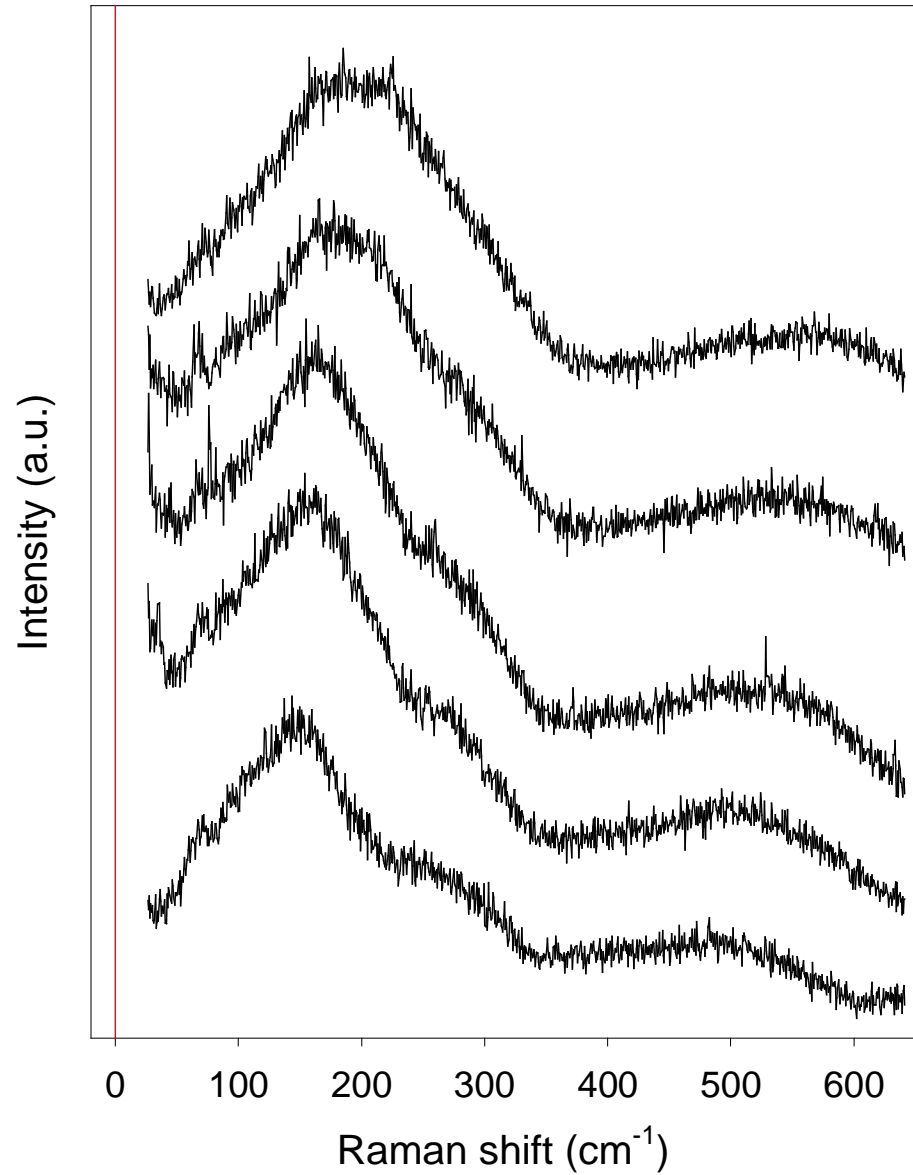
Raman setup

A. F. Goncharov, V. V. Struzhkin, JRS 2003

Magnetic excitations in FeO probed by Raman scattering



Magnetic excitations in FeO probed by Raman scattering



$$H = H_{ion} + H_{ex} = \sum_{\{jk\}} H_{so-cf}(jk) + \sum_{\{jk\}} \sum_{\{j'k'\}} J(jk, j'k') S(jk) S(j'k').$$

$$H = H_i + H'_{ex} = (H_{ion} + H_{mf}) + (H_{ex} - H_{mf}),$$

$$H_{mf} = \sum_{\{jk\}} (-1)^k H_z S_z(jk), \quad H_z = 2 \sum_{\{r\}} Z_r J_r \langle S_z \rangle$$

$$H_i = \sum_{\{jk\}} [H_{so-cf}(jk) + (-1)^k H_z S_z(jk)] = \sum_{\{jk\}} H_{jk}$$

$$H_{so-cf} = -\alpha \lambda (\mathbf{L} \mathbf{S}) + C_z L_z^2 + D_z S_z^2 + C_{xy} (L_x^2 - L_y^2) + D_{xy} (S_x^2 - S_y^2)$$

$$a(kp, \mathbf{q}) = N^{-1/2} \sum_{\{j\}} a_p(jk) \exp\{i \mathbf{q} \cdot \mathbf{R}(jk)\}$$

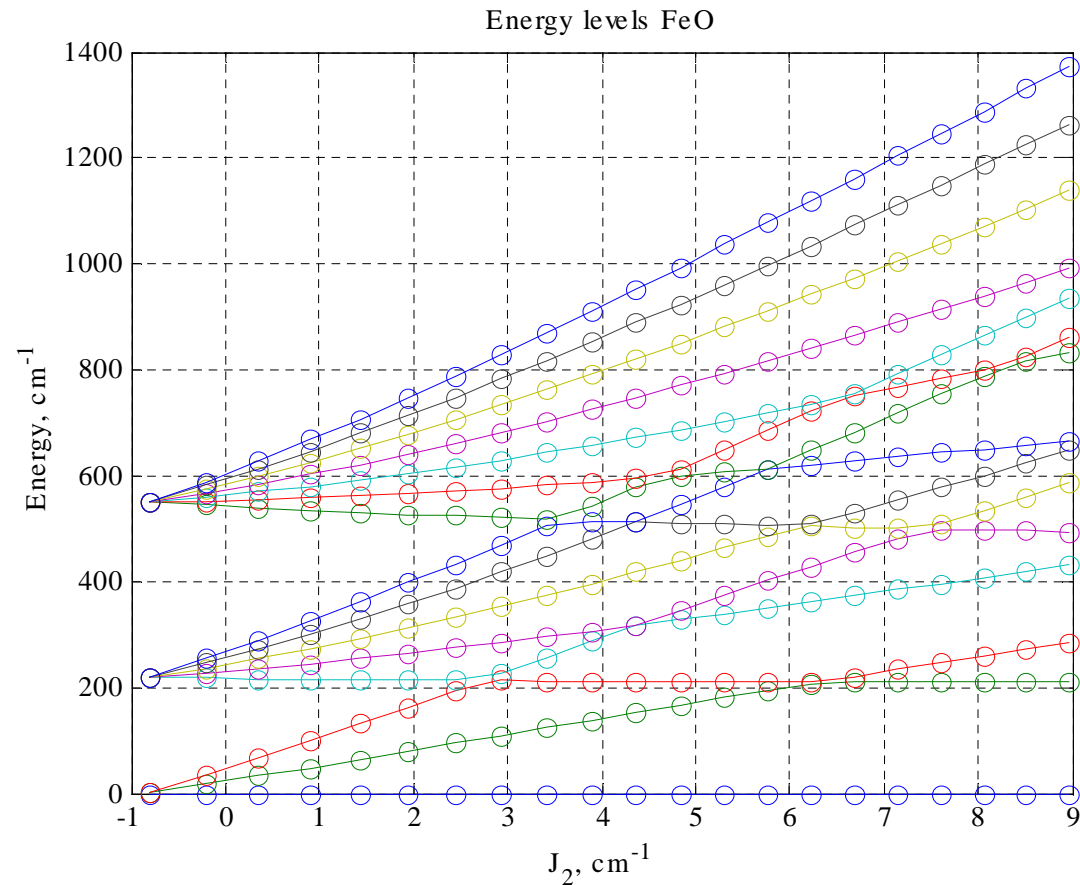
$$L=1$$

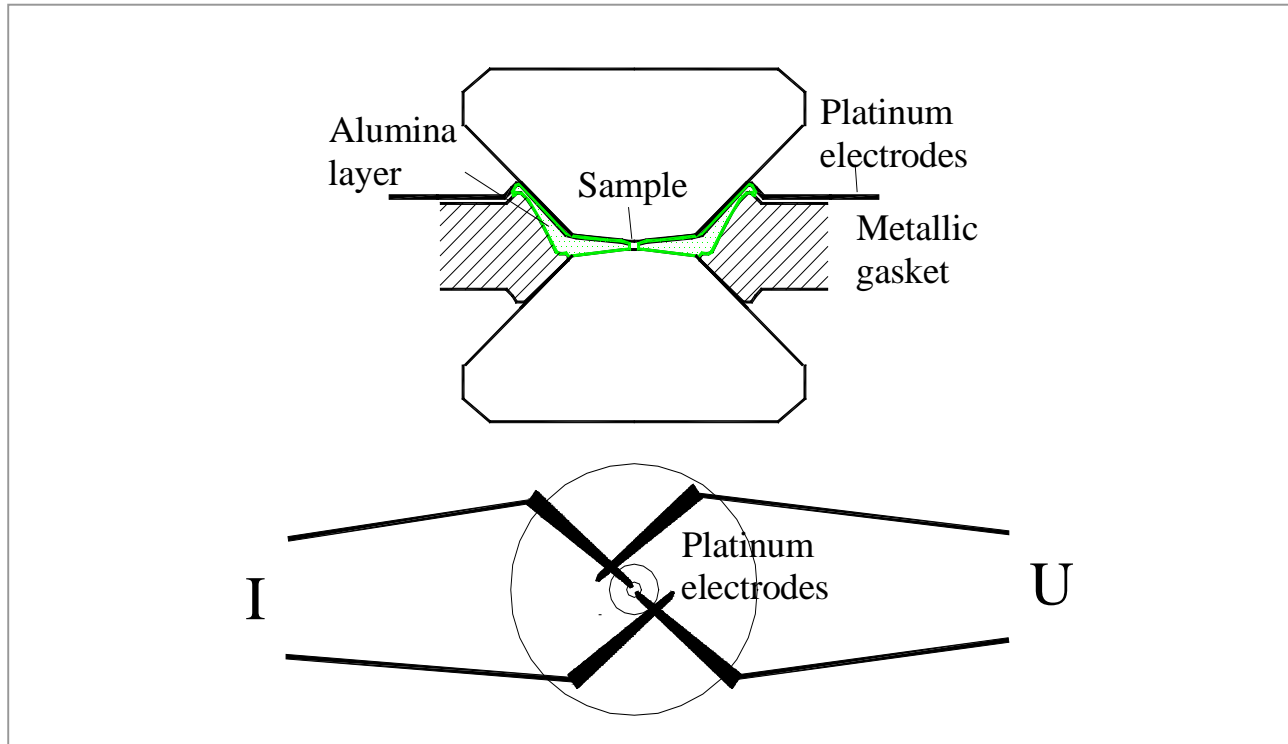
$$S=2$$

$$J_{1+} = 1.8 \text{ cm}^{-1}$$

$$J_{1-} = 1 \text{ cm}^{-1}$$

Magnetic excitations
in FeO probed by
Raman scattering:
model Hamiltonian
with spin-wave
excitations





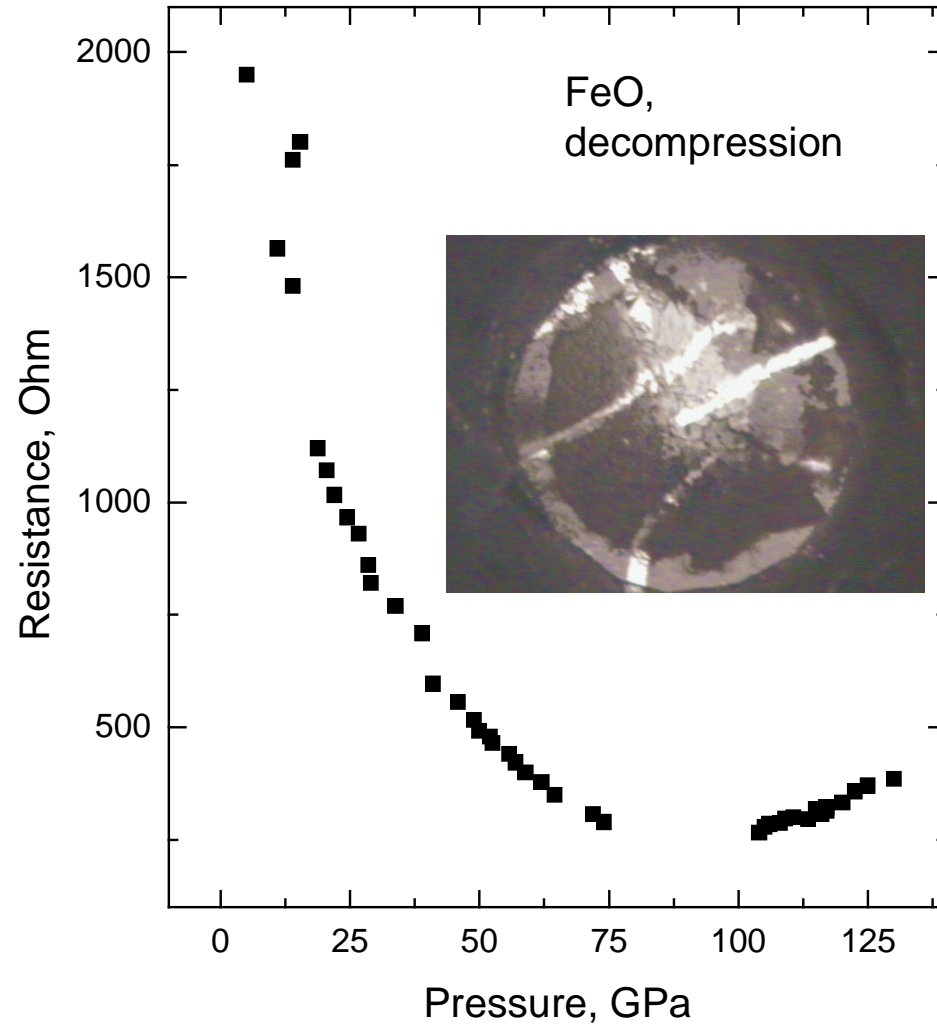
Electrodes

- Foils and wires
- Sputtering techniques

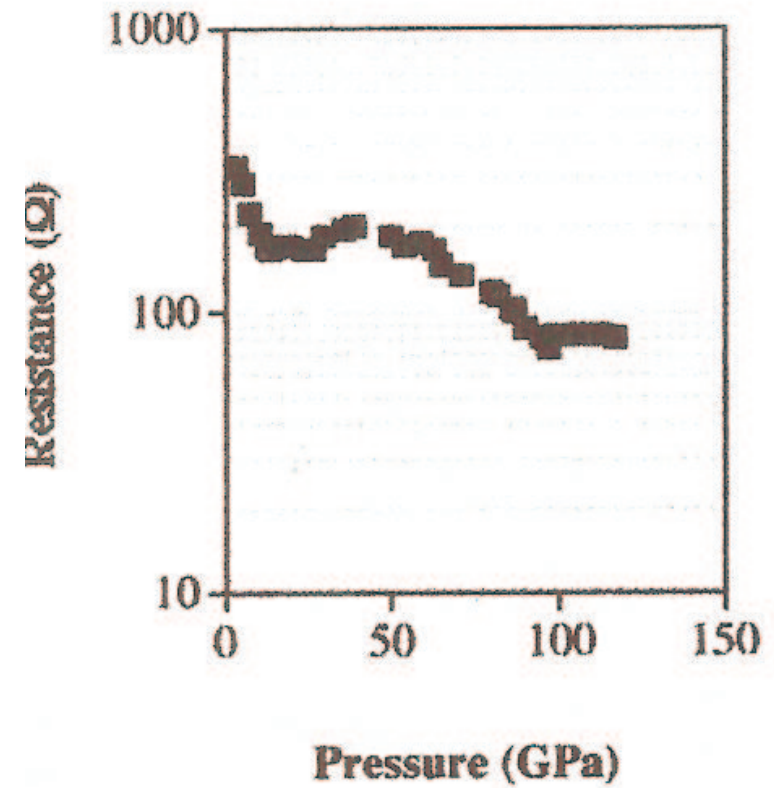
Insulating layer

- Epoxy mixed with cubic BN, diamond or other powders
- Compacted Al_2O_3 powder
- CVD diamond coating

M. I. Erements, V. Struzhkin, 2004



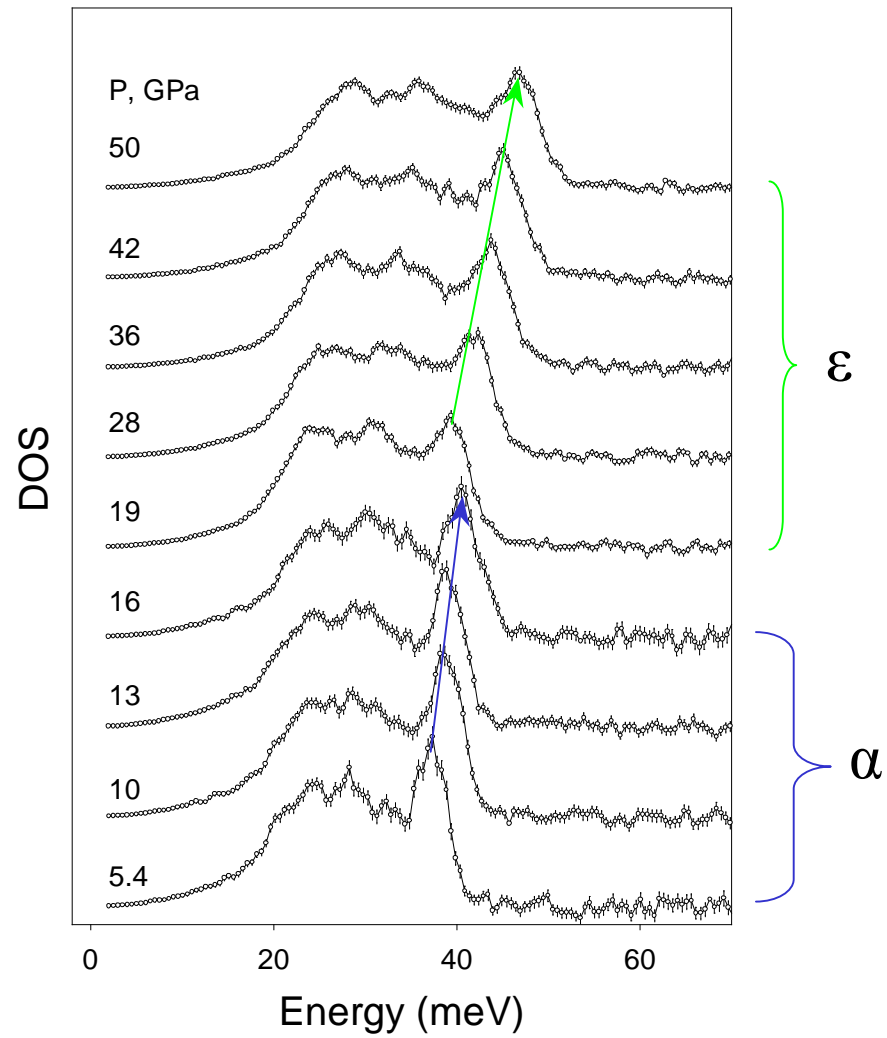
S. T. Weir, et. al. 1999, AIRAPT-17



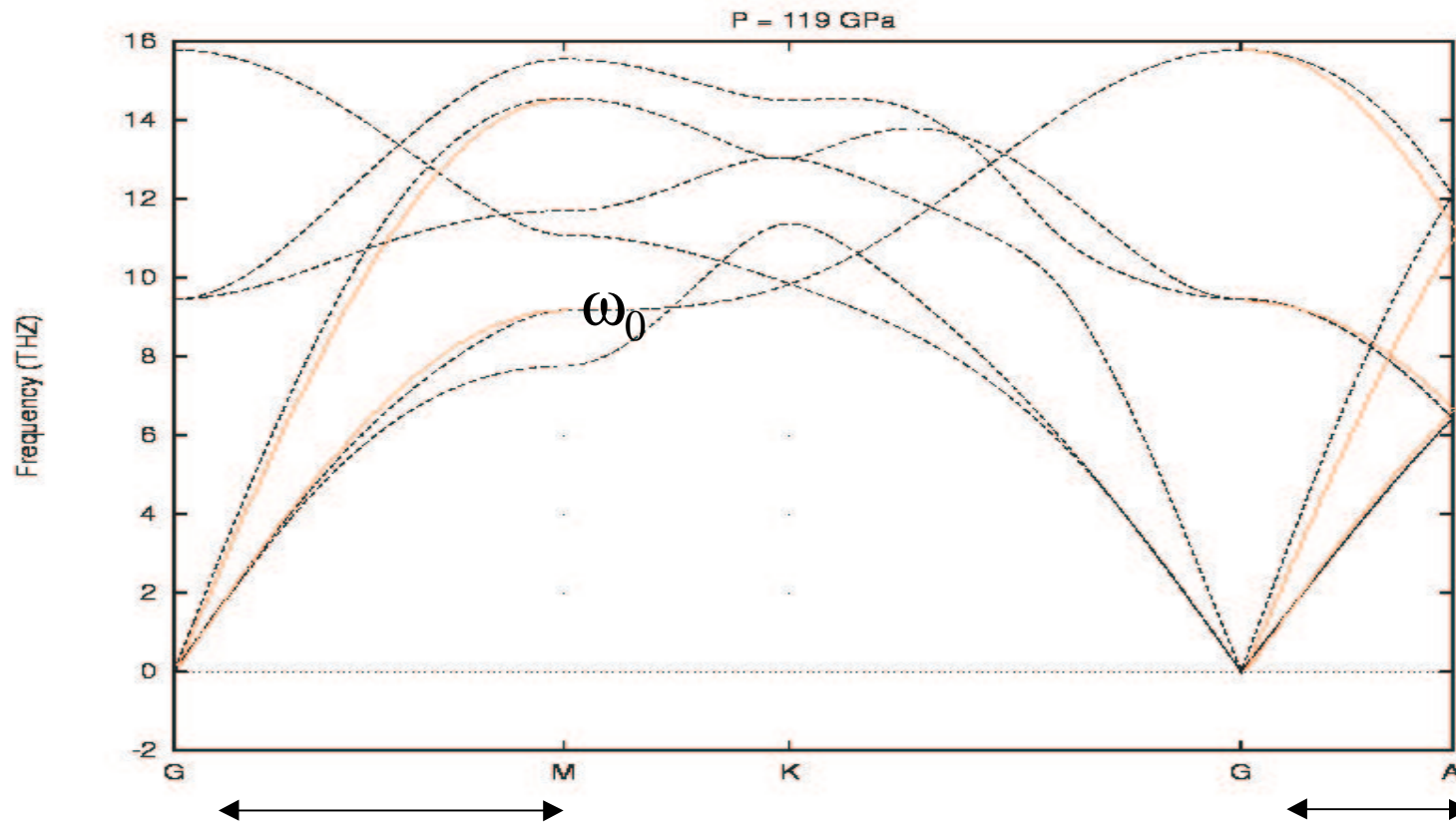
Conclusions: FeO

- Magnetic phase diagram below 60 GPa is in very good agreement with x-ray diffraction data
- Magnetic properties of the high-pressure modification : the spin state of Fe^{2+} in a “metallic” FeO at pressures above 100 GPa is still an open question
- Inelastic scattering reveals a strong magnetoelastic coupling
- Resistance measurements are compatible with a sluggish transition to a “nearly” metallic state in the range from 70 to 140 GPa (conductivity $\sim 1 \Omega^{-1} \text{ cm}^{-1}$)

NRIXS of Fe in He pressure medium



Theory,
L. Vocadlo et al.



$$Q_0 = g_2 = 2\pi / a\sqrt{3}$$

$$V = (\pi/2) \omega_0 / Q_0$$

$$C_k = \rho V^2$$

$$Q_0 = 2g_3 = 4\pi / c$$

Antonangeli et. Al., EPSL 2004

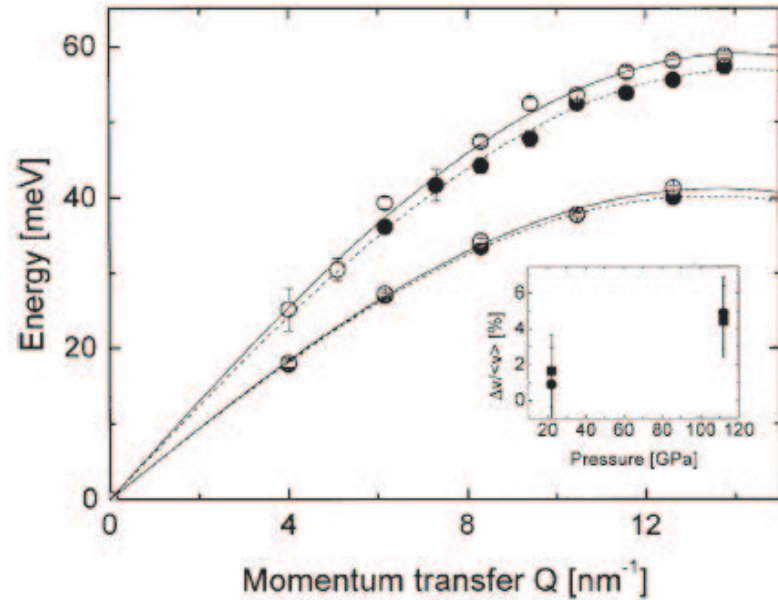


Fig. 4. LA phonon dispersion curves of iron at room temperature and at pressures P of 22 GPa (lower curve) and 112 GPa (upper curve) for the two orientations of the DAC; full (open) circles: sound propagation at 90° (50°) to the DAC loading axis. The displayed error bars of the energy position results from the statistic error of the fit and the finite Q -resolution of the spectrometer. The lines through the data points are fits to the data, with Q_{\max} as a free parameter. The inset reports the relative difference of the sound speeds $\Delta v/\langle v \rangle$ as a function of pressure. The two methods used to derive the sound speed (see Section 3.1) yield slightly different results, indicated by full circles (Q_{\max} free) and squares (Q_{\max} fixed).

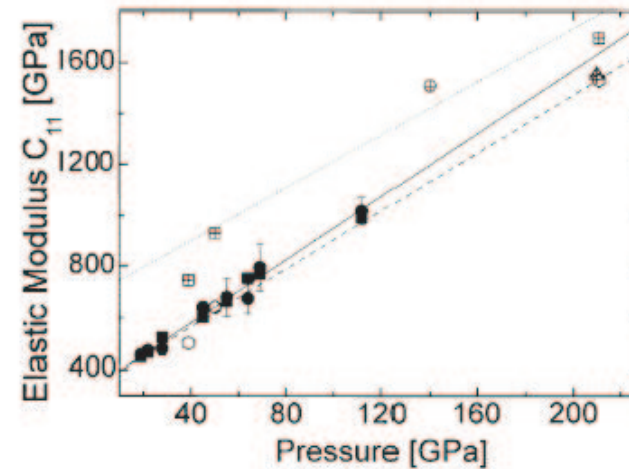
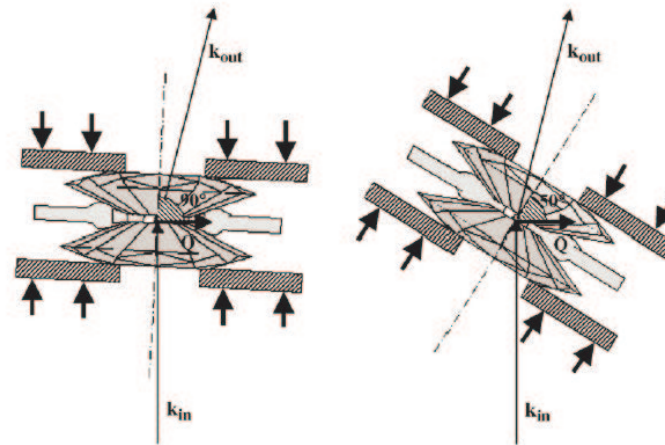
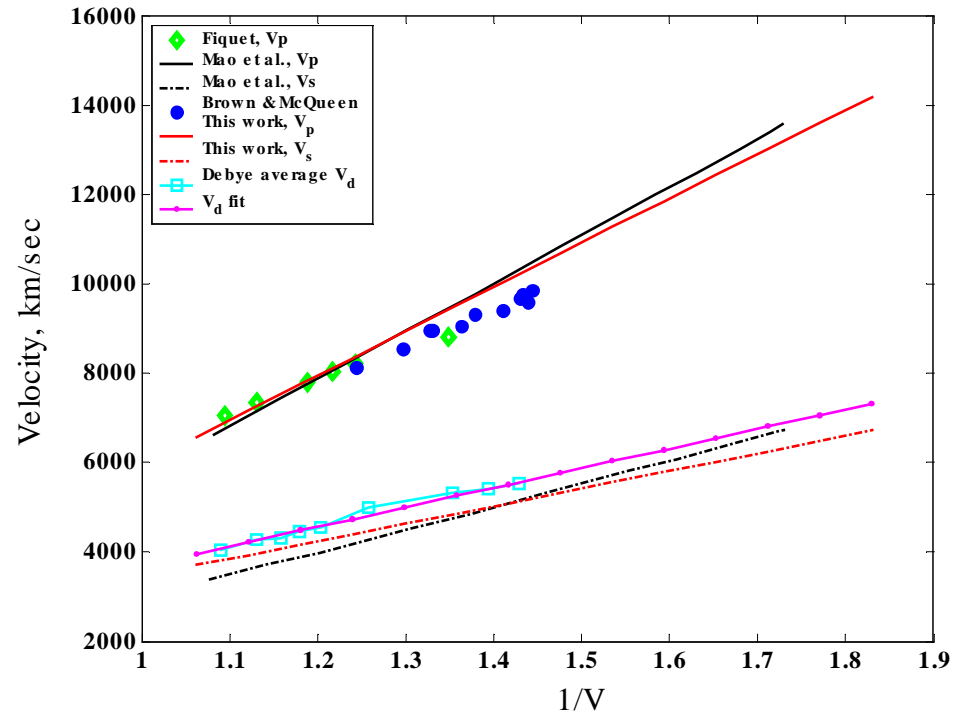
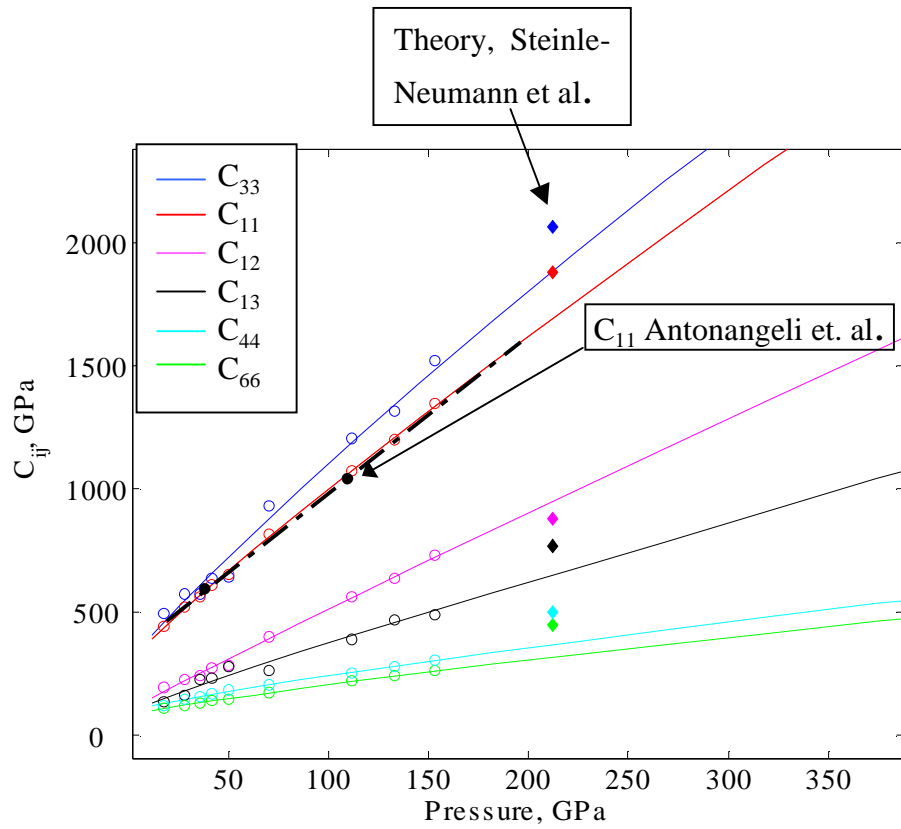


Fig. 6. Derived elastic modulus C_{11} as a function of pressure. Full circles (squares): IXS data analysed with Q_{\max} free (fix), solid (dashed) line: corresponding linear fits to the IXS data with Q_{\max} free (fix); hexagons: XRD data [18,27]. All the experimental results are at room temperature. Calculations at 0 K: crossed squares [21,23], crossed circles [20], and dotted line [22]. Calculations at 300 K: crossed triangles [24].



	C_{44}	C_{33}	C_{11}
Theory	0.91	1.15-1.05	1.10

Best fit with theoretical shape for dispersion branches, using bulk modulus, and Debye average velocity V_d as constraints.

Kohn, Chumakov, Ruffer, 1998
**Nuclear resonant inelastic absorption of synchrotron
radiation in an anisotropic single crystal**

FeBO_3

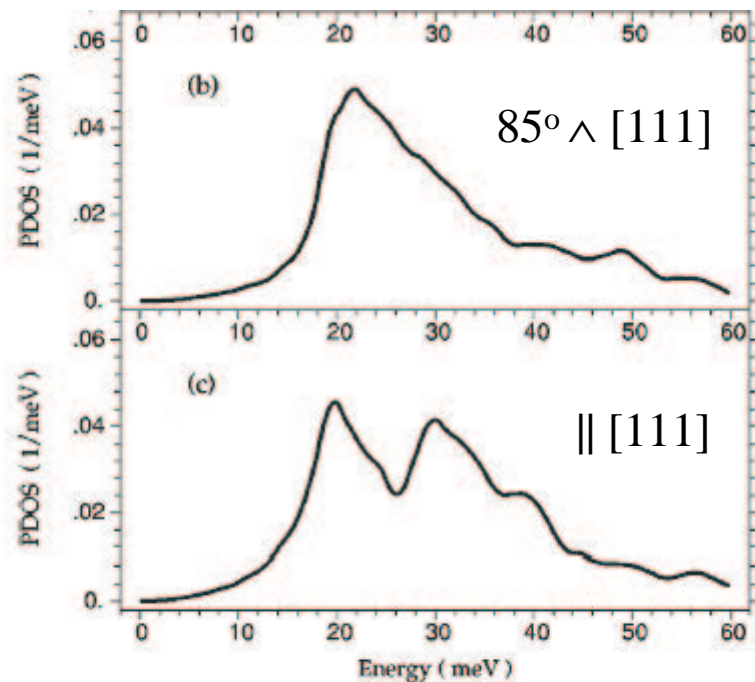


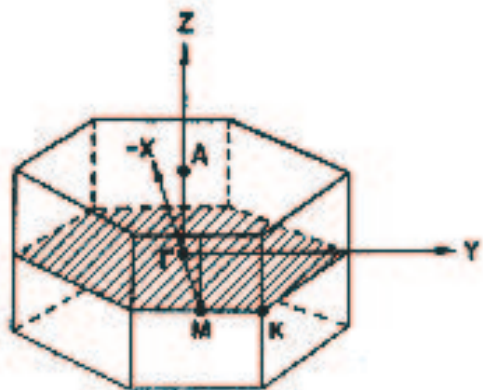
FIG. 2. Results of processing the experimental data from Fig. 1. (a) DOS for the polycrystalline α -iron foil, (b),(c) PDOS for the $^{57}\text{FeBO}_3$ single crystal in the cases where the axis of projection has the angle of (b) 85° relative to the [111] axes, or (c) parallel to the [111] axes.

$$g_m(E, \mathbf{s}) = V_0 \sum_j \int \frac{d\mathbf{q}}{(2\pi)^3} \delta[E - \hbar\omega_j(\mathbf{q})] |\mathbf{s} \cdot \mathbf{e}_{mj}(\mathbf{q})|^2$$

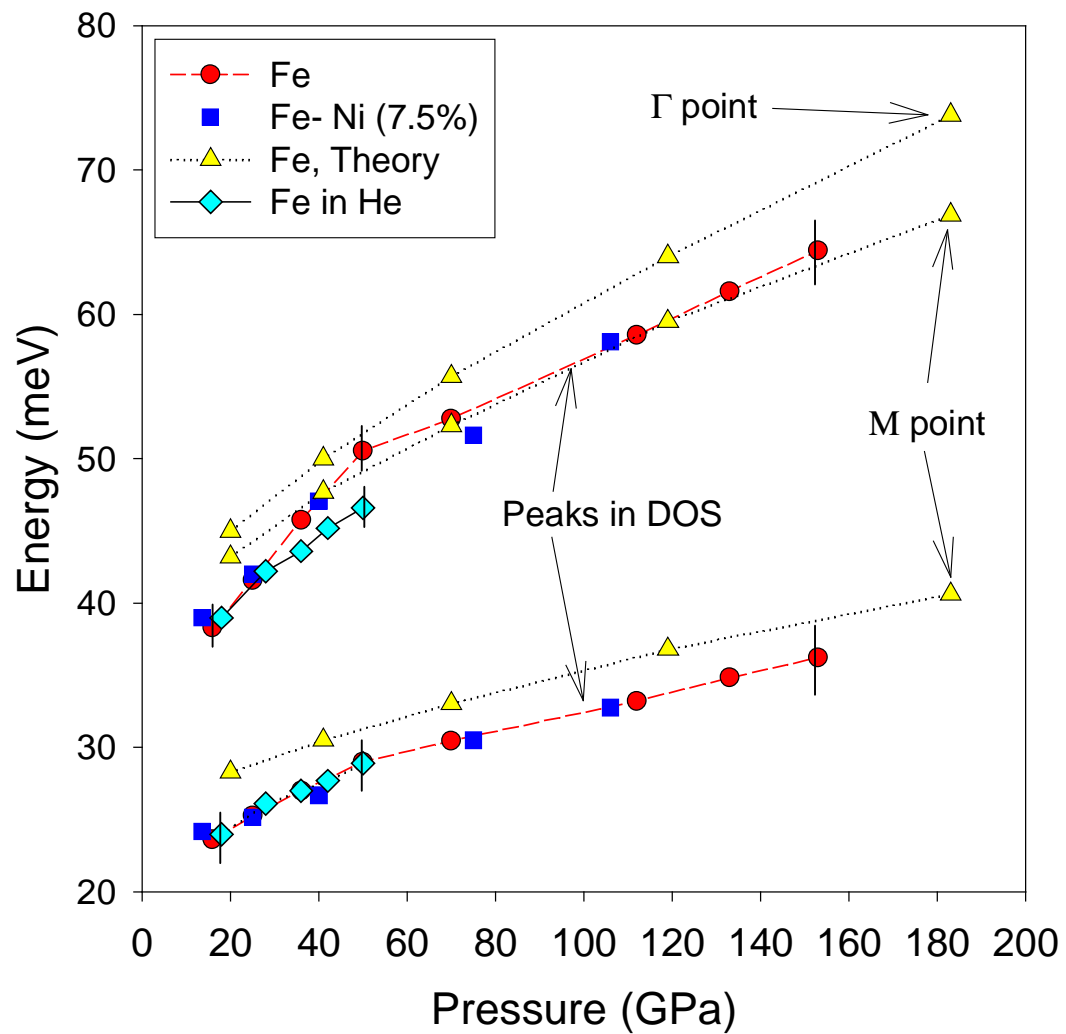
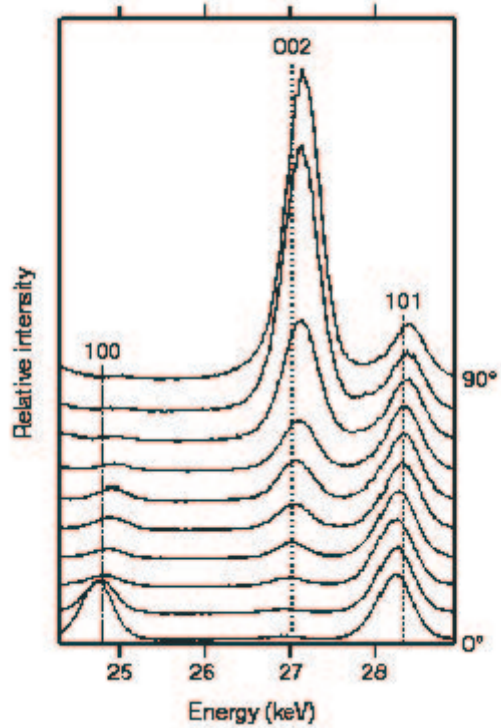
$$= \frac{V_0}{(2\pi)^3} \sum_j \int \frac{dq_1 dq_2}{|\text{grad}_{\mathbf{q}} \hbar\omega_j(\mathbf{q})|} |\mathbf{s} \cdot \mathbf{e}_{mj}(\mathbf{q})|^2.$$

$$\mathbf{s} = \mathbf{k}/k,$$

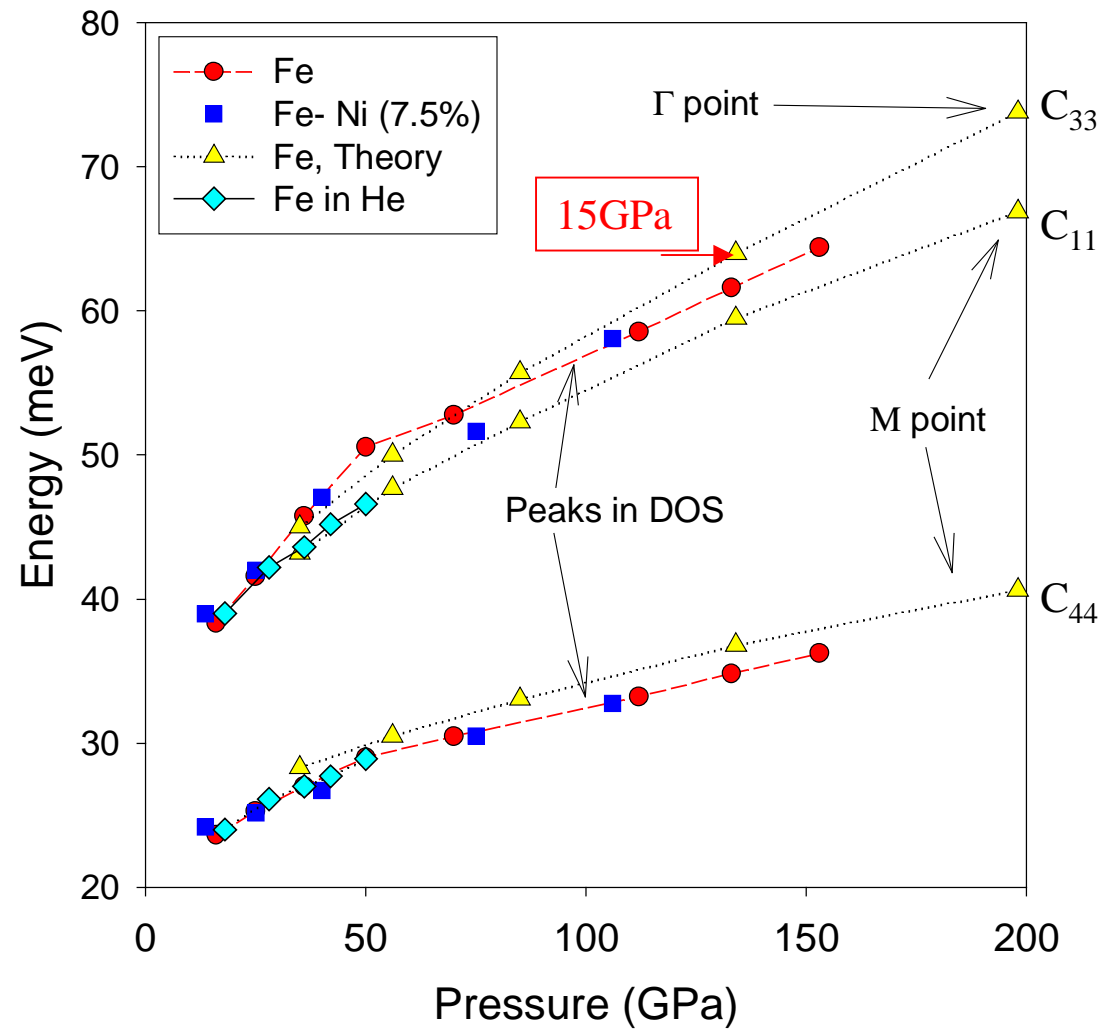
\mathbf{e}_{mj} - polarization of the phonon

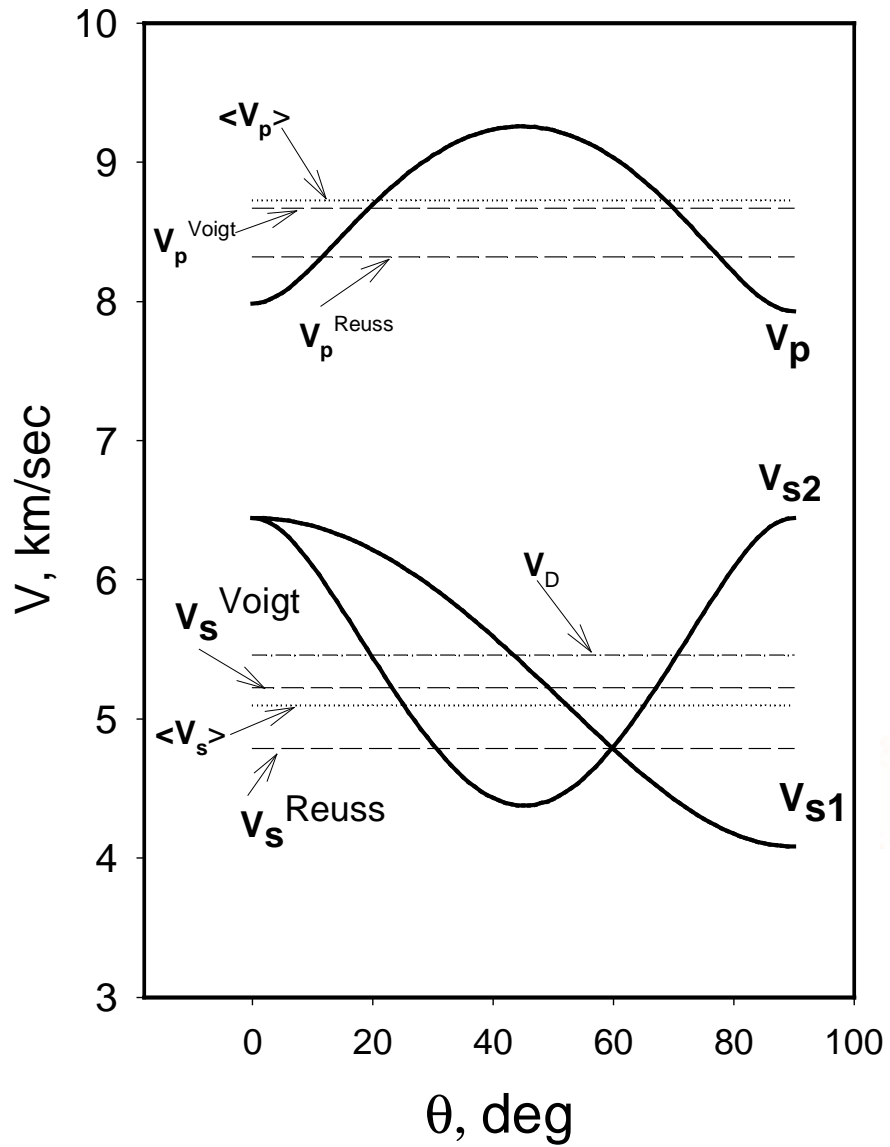


Wenk et al., Nature (2000)
 ϵ -Fe at 220 GPa



Empirical correction
 $\Delta P=15$ GPa
brings theory into better
agreement with experiment,
assuming that the sample
has strong preferred
orientation above 50 GPa





$$3V_D^{-3} = V_P^{-3} + 2V_S^{-3}$$

$$2V_S^{-3} = V_{S1}^{-3} + V_{S2}^{-3}$$

$$\rho V_p^2 = \frac{(A + B)}{2}$$

$$\rho V_{s1}^2 = C_{44} + \frac{1}{2}(C_{11} - C_{12} - 2C_{44})\sin^2\theta$$

$$\rho V_{s2}^2 = \frac{(A - B)}{2}$$

$$A = C_{11} + C_{44} + (C_{33} - C_{11})\cos^2\theta$$

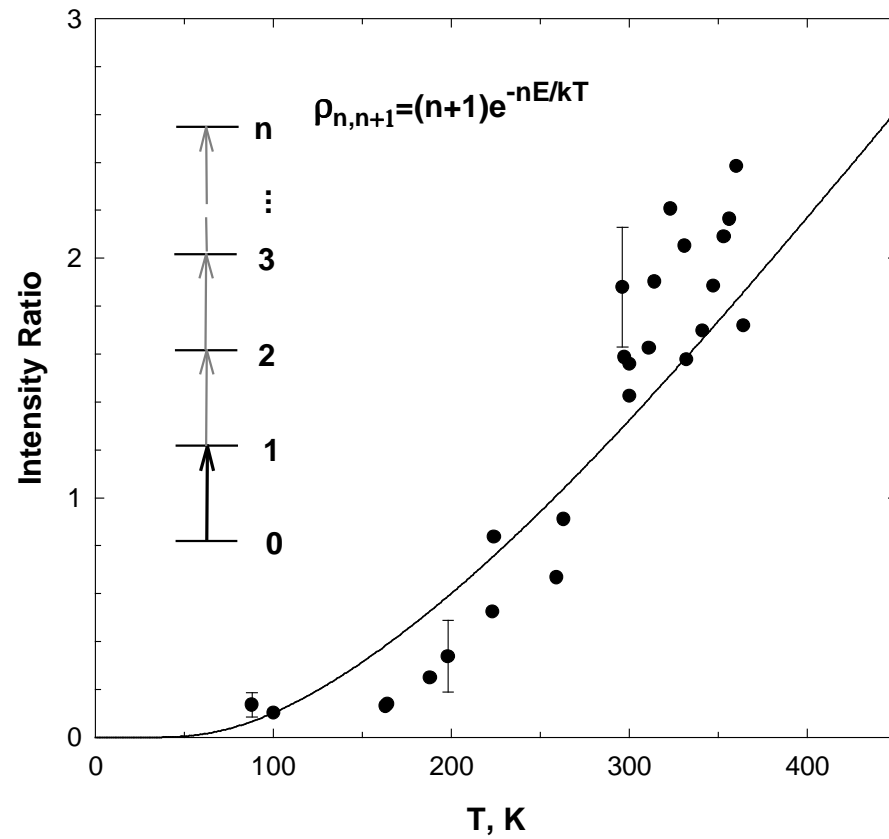
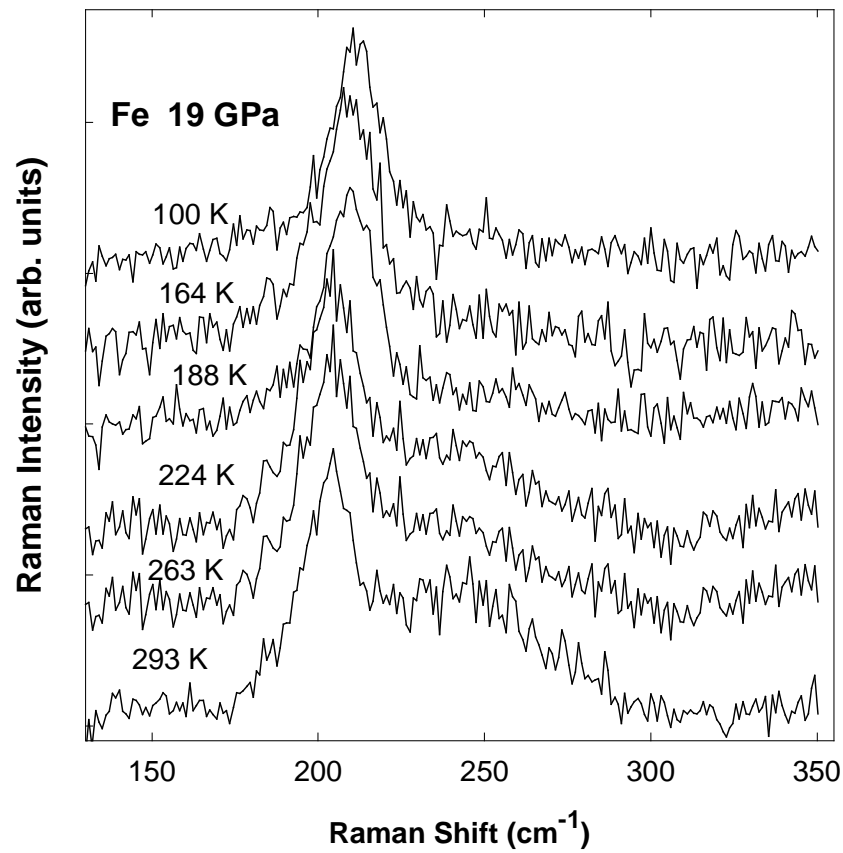
$$B = \frac{1}{2}\{(C_{11} - C_{33})^2 + 4(C_{13} + C_{44})^2 - 2(C_{11} - C_{33})(C_{11} + C_{33} - 2C_{44})\cos 2\theta + [(C_{11} + C_{33} - 2C_{44})^2 - 4(C_{13} + C_{44})^2]\cos^2 2\theta\}^{\frac{1}{2}}$$

V_p - compressional wave

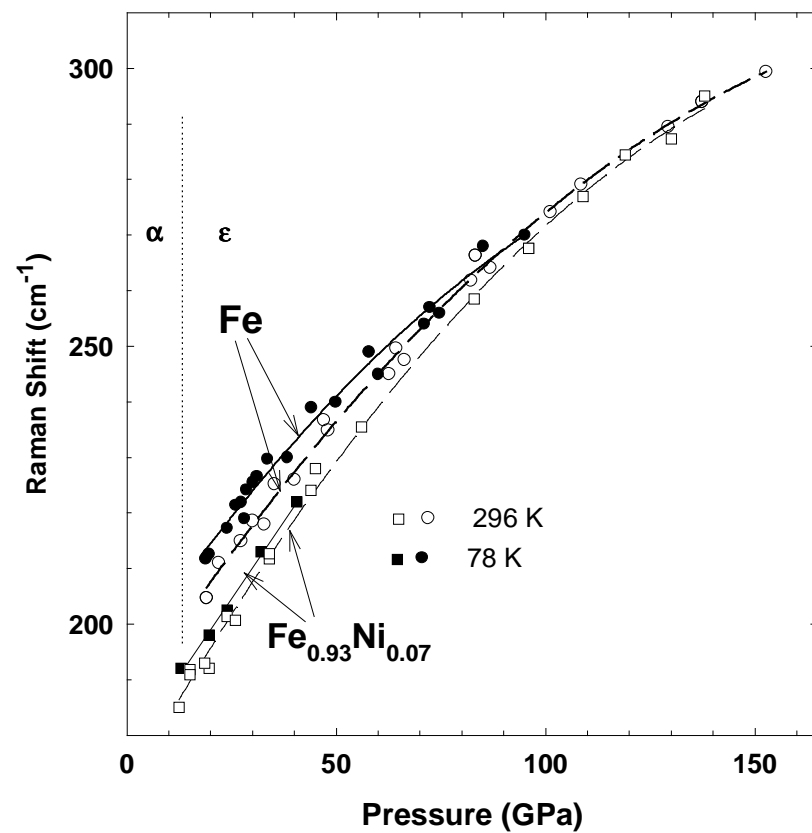
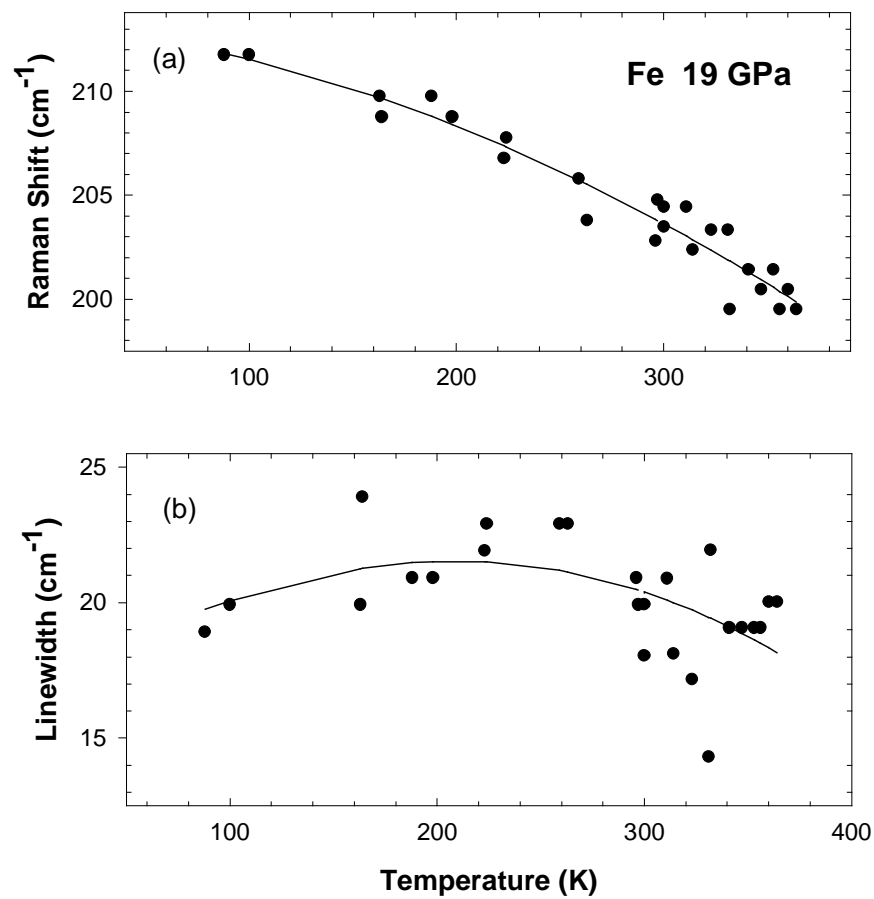
V_{s1} - pure shear wave

V_{s2} - quasi shear wave

Anharmonicity of shear wave in Fe: Raman results (Goncharov, Struzhkin, in JRS, 2003)



Anharmonicity of shear wave in Fe: Raman results



Conclusions: Fe, Fe-Ni

- Van-Hove singularities: dispersion branches in high symmetry directions may be used to estimate C_{ij} .
- Hydrostatic versus non-hydrostatic measurements (using preferred orientation) may provide additional C_{ij} .
- Fe-Ni(7%) alloy has shear-wave elastic properties very similar to pure Fe: with present data accuracy it is not possible to specify the content of Ni in the Earth's core.