
Statistical Properties of a VUV FEL

Christopher Gerth

Main contributions to the understanding of the SASE statistics:

Evgeni Saldin

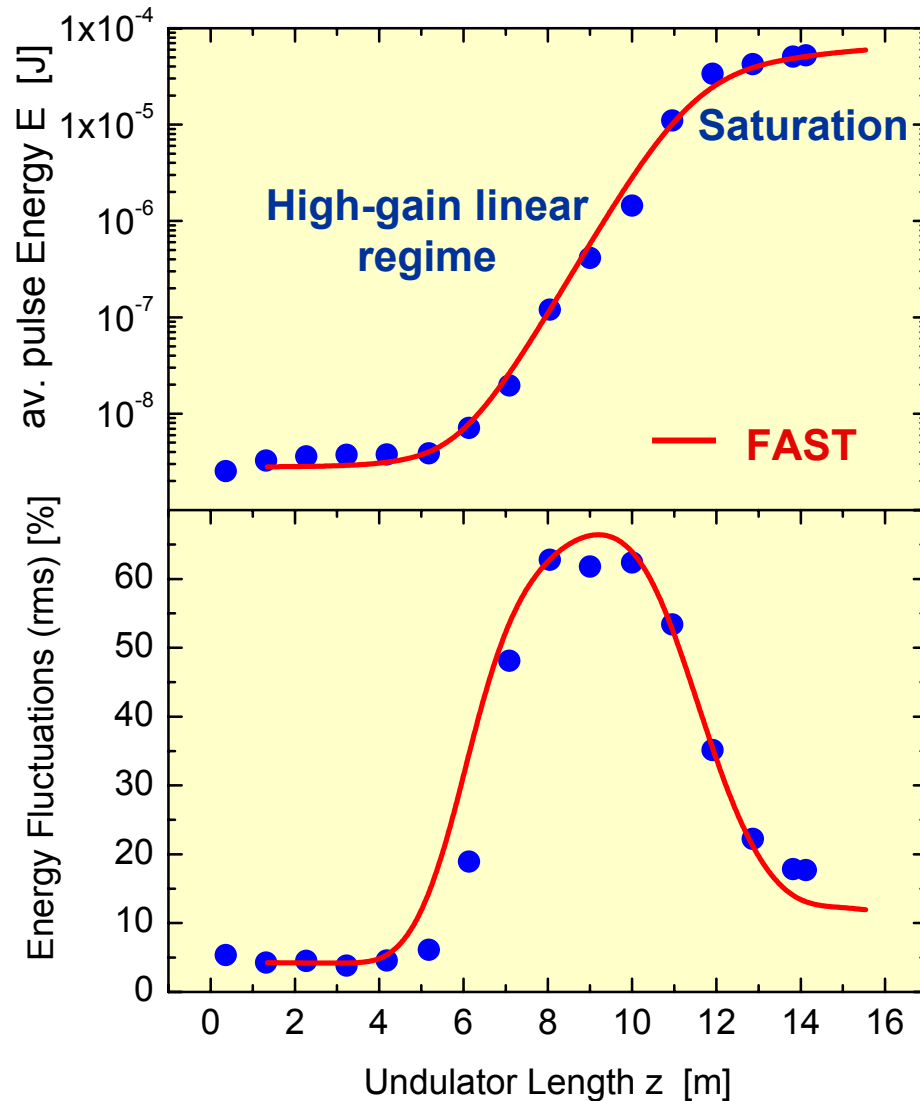
Evgeni Schneidmiller

Michael Yurkov

VUV Free-Electron Laser at the TESLA Test Facility at DESY

⇒ FR-O-03 J. Roßbach: General Overview

Amplification process vs. undulator length



Exponential growth:
 $P(z) = P_0 * \exp(z/L_g)$

Gain length: $L_g = 0.68$ m

Photon beam	Design values	Status 9/01
Pulse energy	330 -700 μ J	50 -100 μ J
Pulse duration	1.3 ps	?

No direct measurement of the pulse duration

(Power) Gain length L_g :

$$P(z) \approx P_0 \cdot \exp(z/L_g)$$

$$L_g \approx \frac{\lambda_u}{4\pi \cdot \rho}$$

$$\rho \approx 3 \cdot 10^{-3} \quad \text{FEL Parameter}$$

Information about electron beam parameters, e.g. I

$$\text{with } \lambda_u = 27.3 \text{ mm}$$

$$L_g = 68 \text{ cm}$$

Coherence length l_c :

$$l_c \approx \tau_c \cdot c$$

$$\text{with } \tau_c = 1/\omega\rho \quad \text{and} \quad c = \lambda \cdot \omega/2\pi$$

$$l_c \approx \frac{\lambda \cdot \omega}{\omega\rho \cdot 2\pi}$$

$$l_c \approx \frac{2L_g \cdot \lambda}{\lambda_u} = 5 \mu\text{m}$$

If the pulse is longer than l_c :
Several longitudinal modes

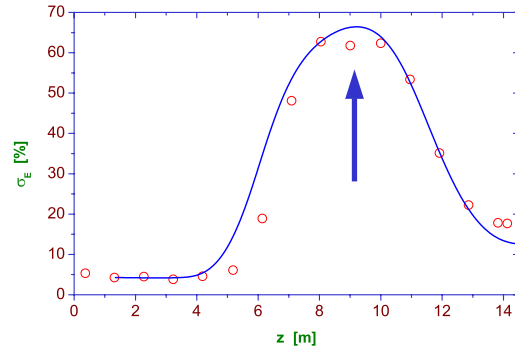
Coherence time τ_c :

$$\tau_c \approx \frac{l_c}{c} \approx \frac{T}{\omega\rho T} \approx \frac{T}{M} \approx 20 \text{ fs}$$

Pulse duration: $T \approx M \cdot \tau_c$
with M: No. of Modes

Linear regime

Probability distribution of the pulse energy



In the linear regime:
Pulse energy of chaotic polarized light
fluctuates according to Gamma-distribution

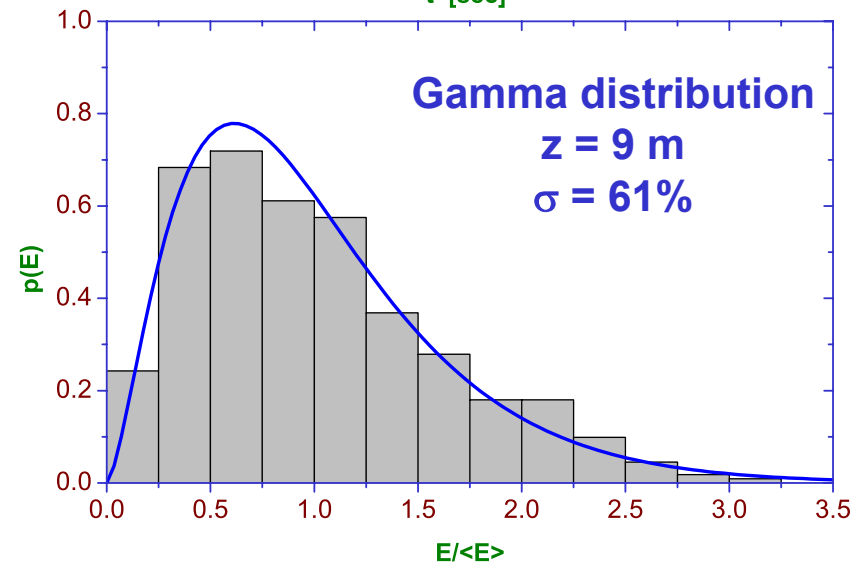
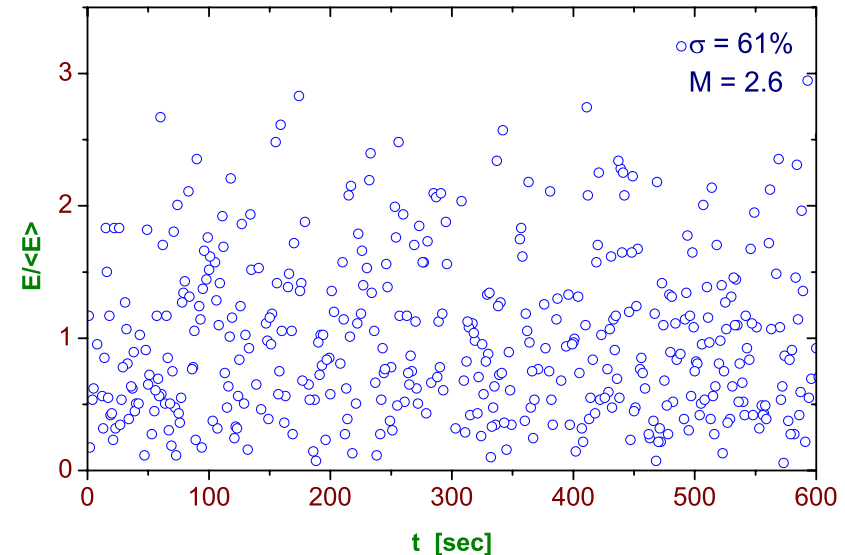
$$p(E) = \frac{M^M}{\Gamma(M)} \left(\frac{E}{\langle E \rangle} \right)^{M-1} \frac{1}{\langle E \rangle} \exp\left(-M \frac{E}{\langle E \rangle} \right)$$

Energy Fluctuations: $\sigma = 61\%$

No. of Modes: $M = 1/\sigma^2 = 2.6$

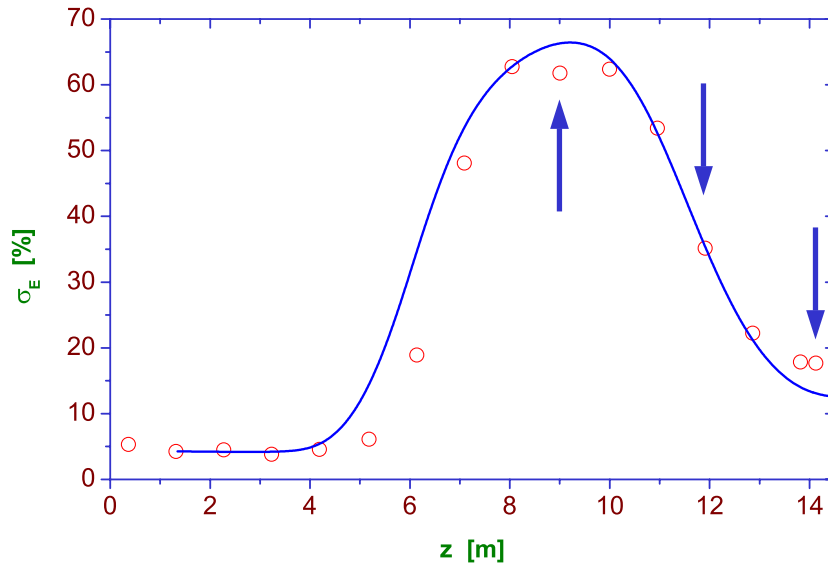
Pulse duration T

$T \cong M * 20 \text{ fs} \cong 50 \text{ fs}$

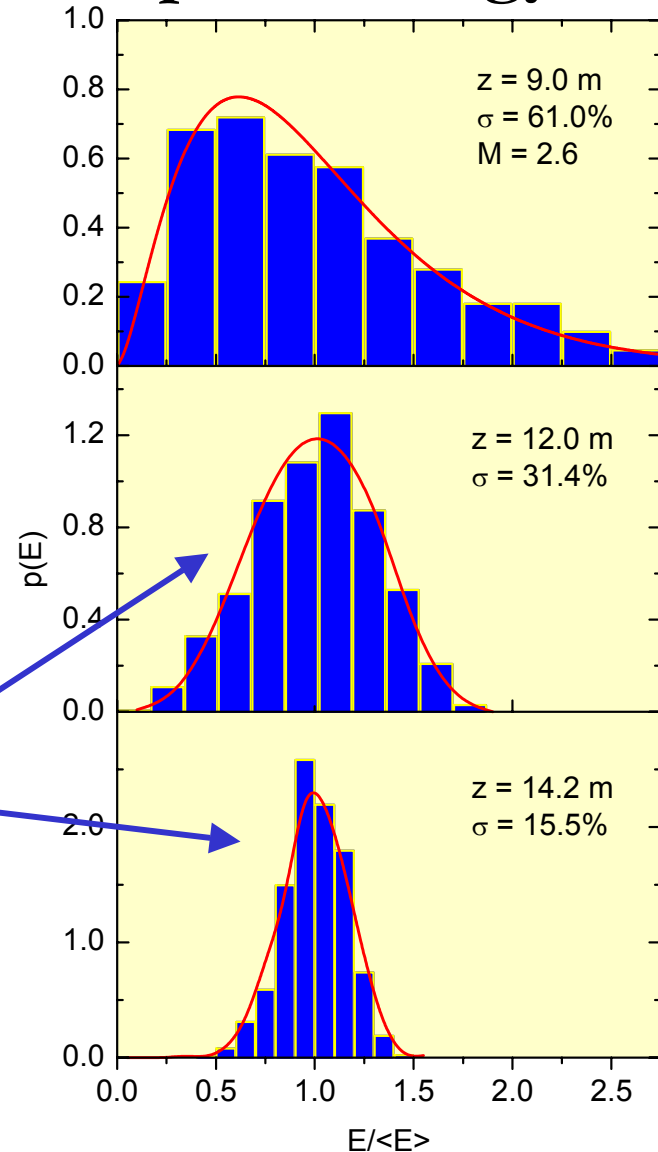


Nonlinear regime

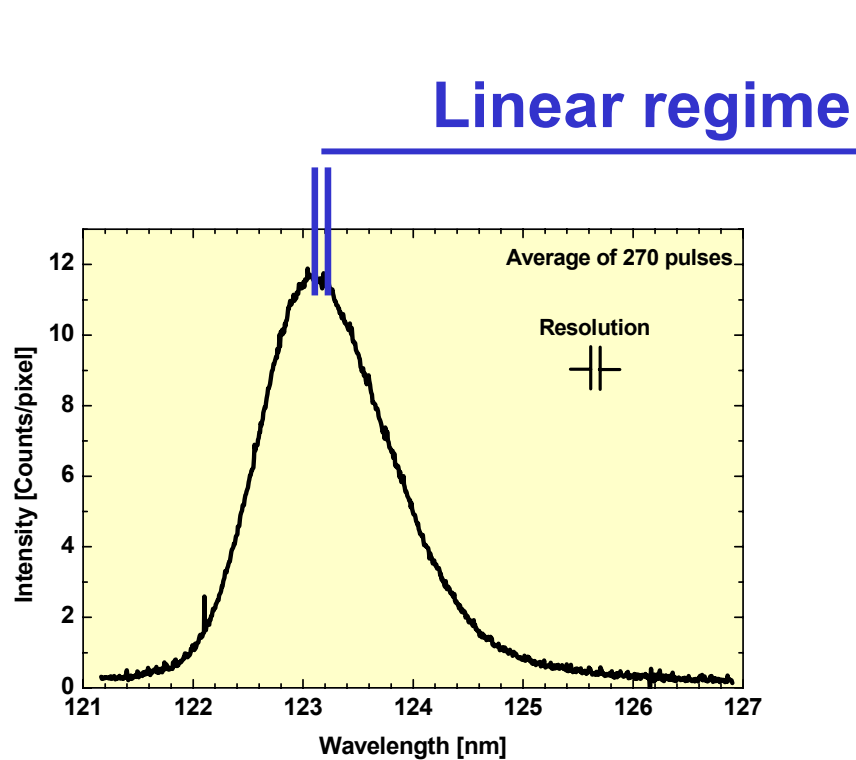
Probability distribution of the pulse energy



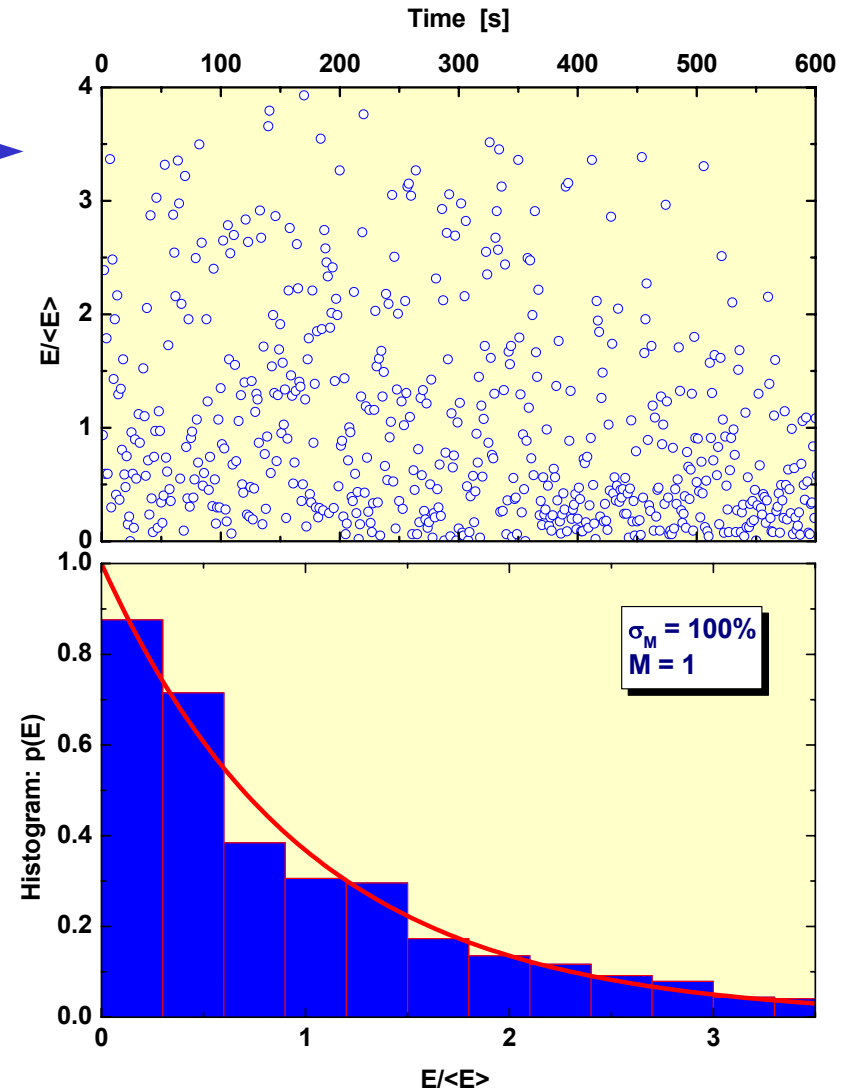
In the saturation regime:
Fluctuations of the pulse energy cannot
be described by a Gamma-distribution
 σ not connected to M anymore



Energy fluctuations behind a narrow-band monochromator

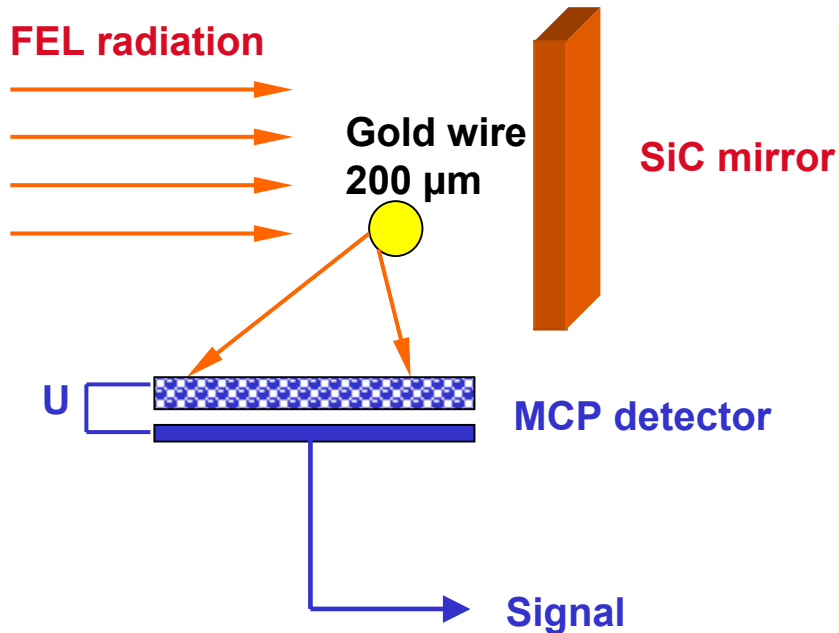


Negative exponential distribution
Intensity fluctuations: $\sigma = 100\%$



Pulse energy

Wire + Micro Channel Plate Detector



The determination of absolute pulse energies in the VUV is a challenging task.

- Large dynamic range: 10^7
(The MCP has been calibrated for different voltage settings U)
- Spont. Emission: gain = 1
 $E = \text{gain} \cdot Q \cdot f(\lambda)$
(f can be calculated precisely)
- Corroborated by independent detectors

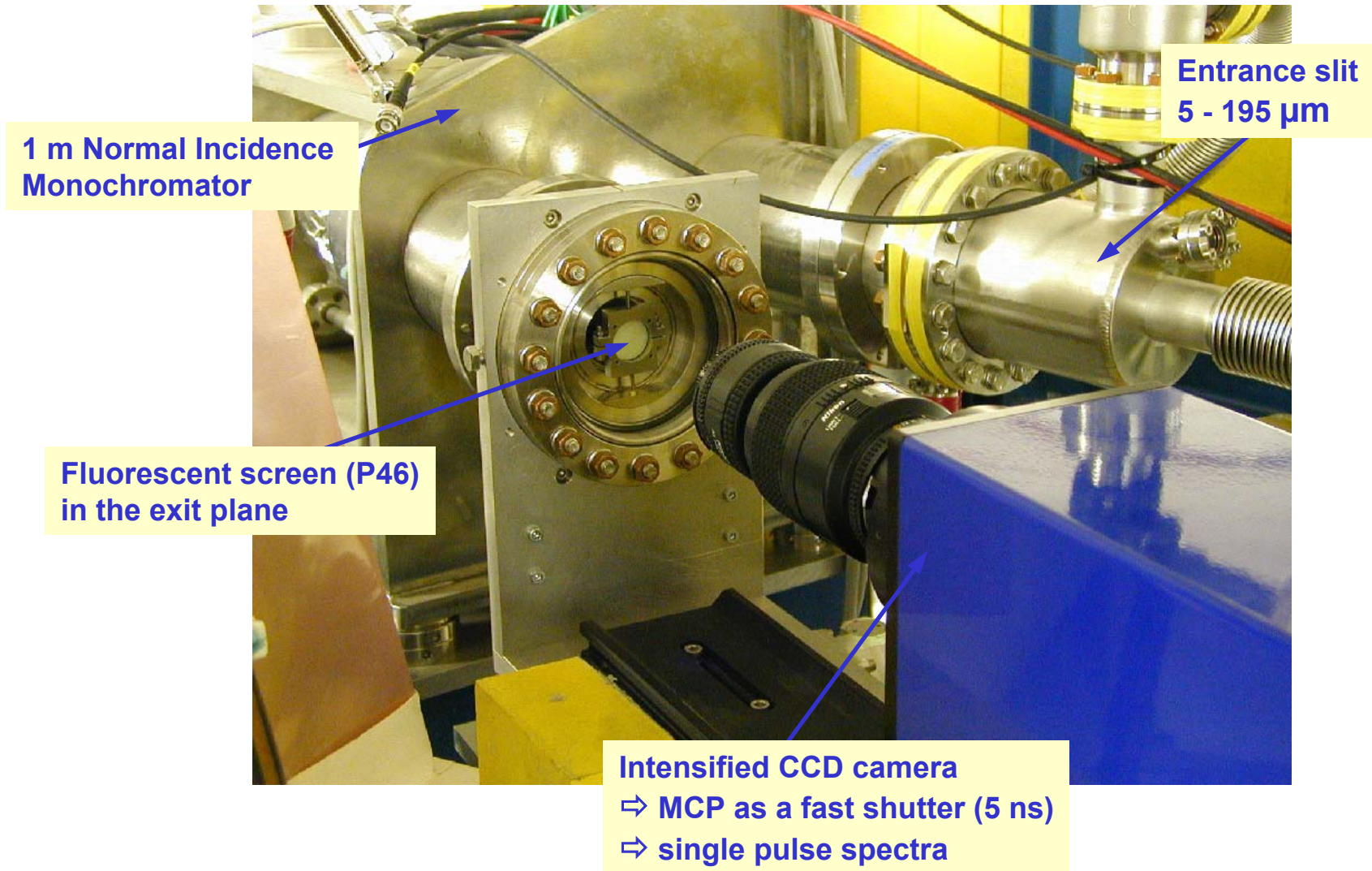
Data selection:

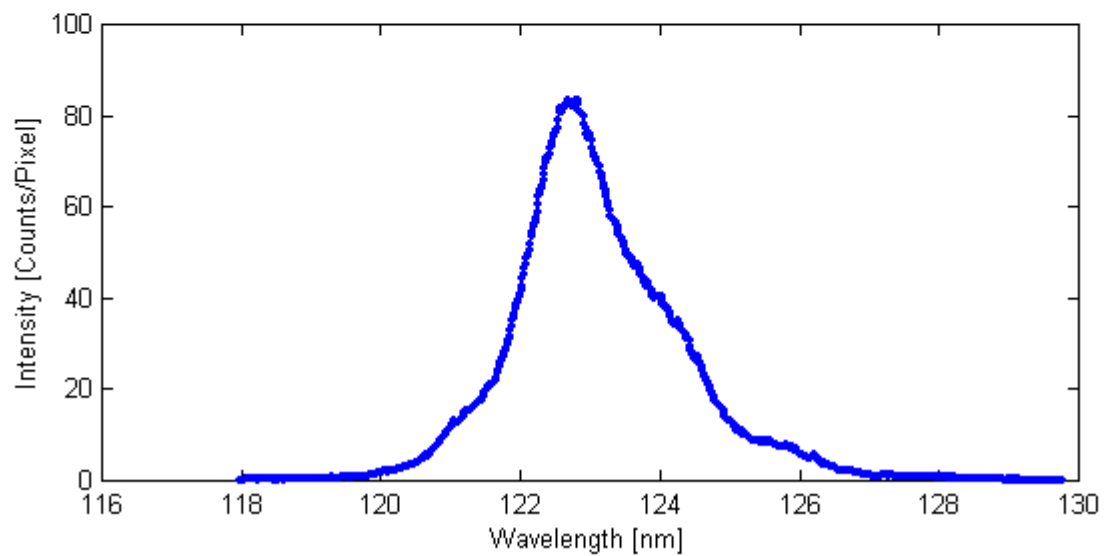
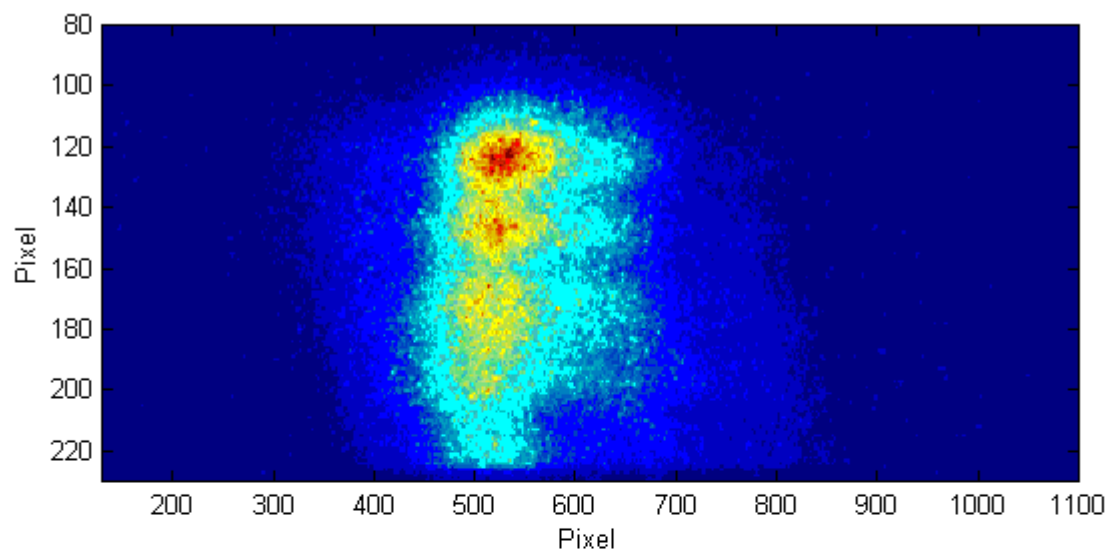
Charge fluctuations < 1% (rms)

Orbit deviation < 50 μm

Spectral distribution

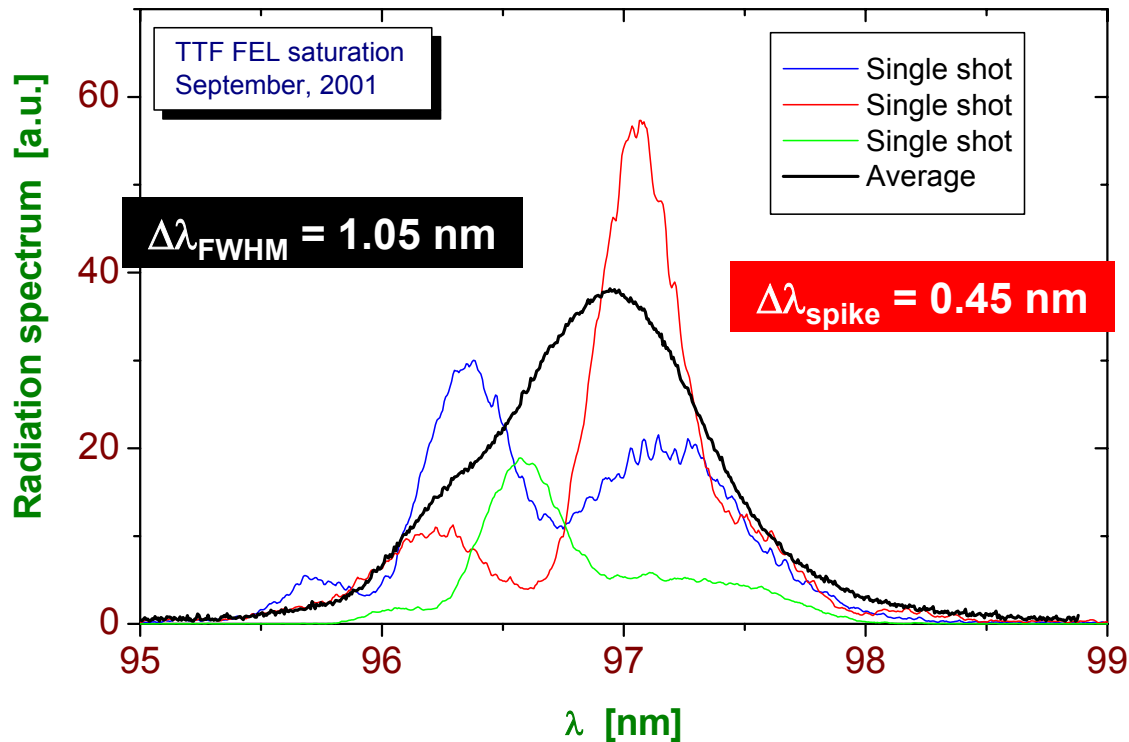
Measurement of the Spectral Distribution





Spectral distribution

Determination of the pulse duration



Spike: $T \cong 2\pi^{1/2}(\Delta\omega)_{spike} = 37 \text{ fs}$

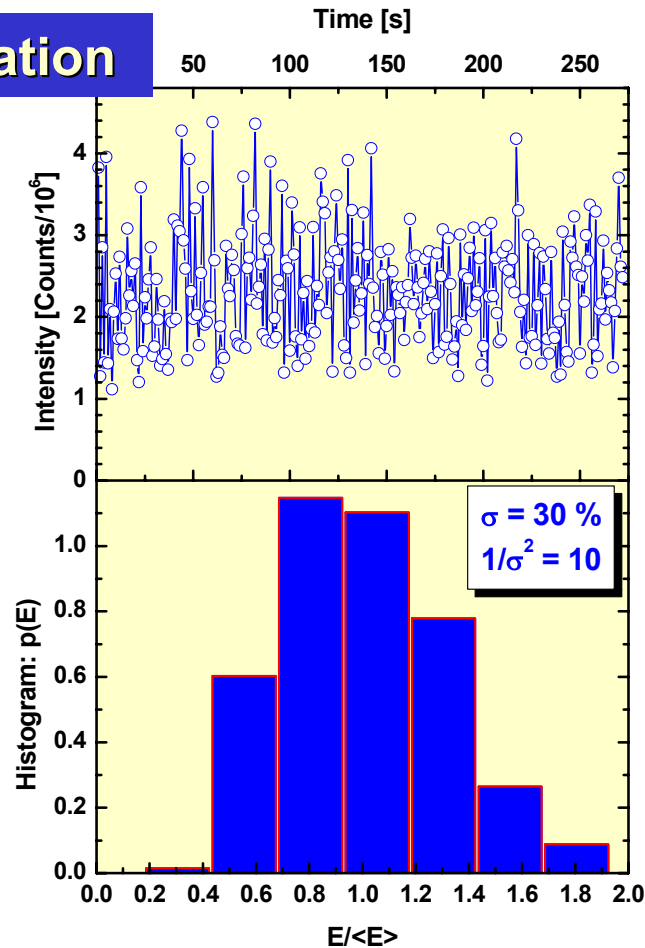
Average: $2\pi^{1/2}(\Delta\omega)_{FWHM} = 16 \text{ fs}$

$T \cong M * 2\pi^{1/2}/(\Delta\omega)_{FWHM} \cong 41 \text{ fs}$

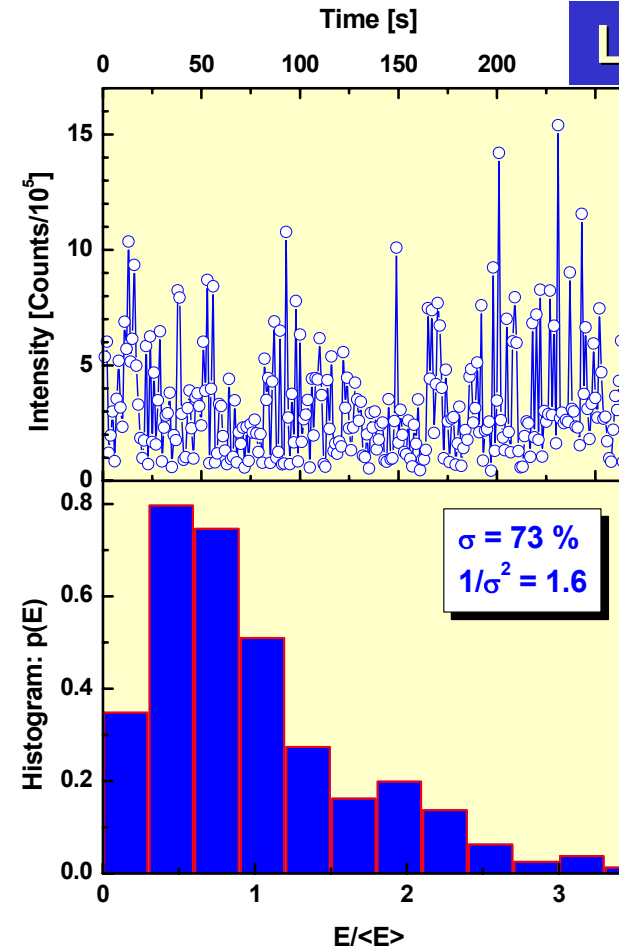
Spectral distribution

Fluctuations of integral intensity in the spectra

Saturation



Linear regime



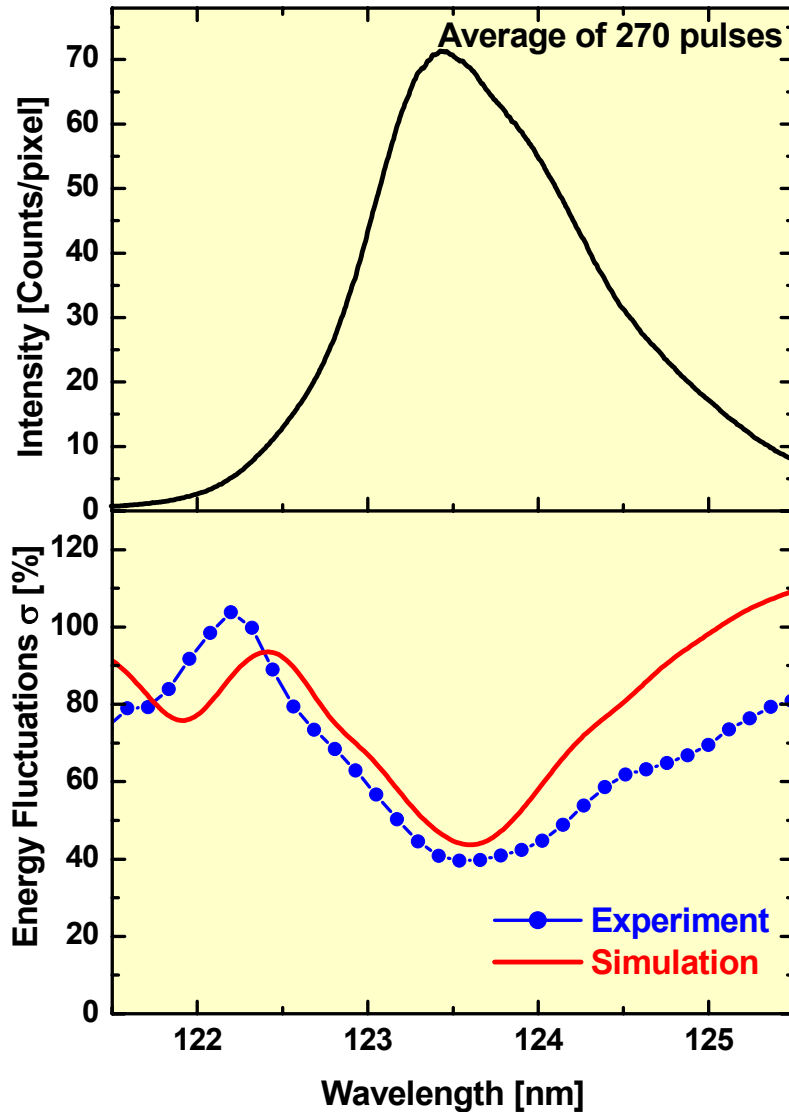
M = 1.6

Estimation of the radiation
pulse length τ_{rad} :

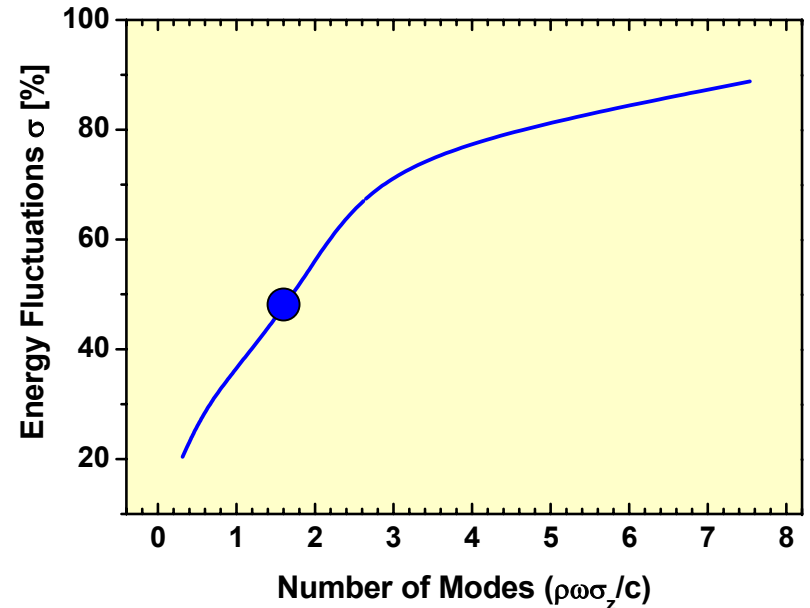
Modes: $M = 1/\sigma^2 = 1.6$
 $\tau_{\text{rad}} \cong 2M\pi^{1/2}/\Delta\omega \cong 40 \text{ fs}$

Spectral distribution

Fluctuations at saturation (spectrally resolved)

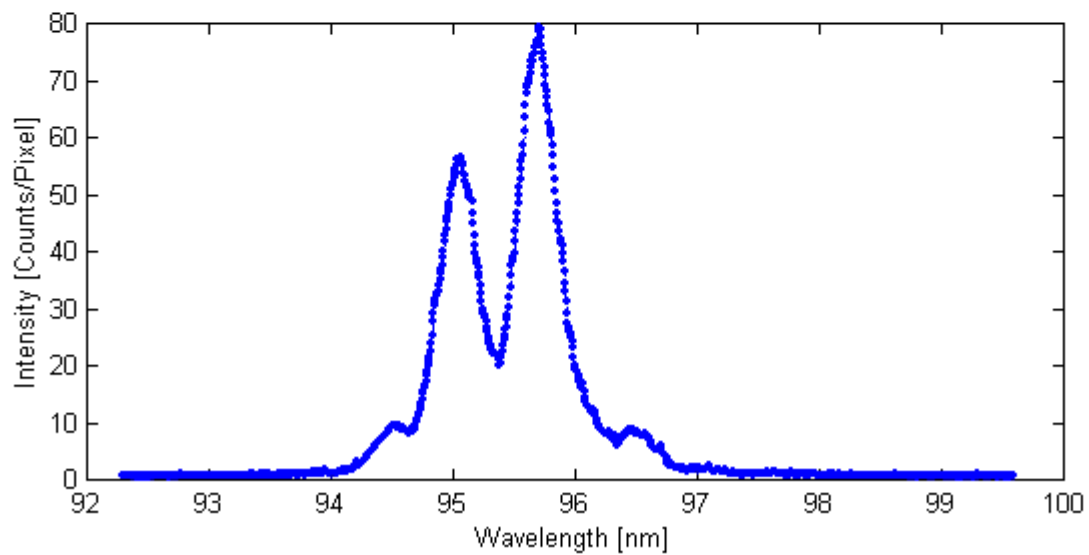
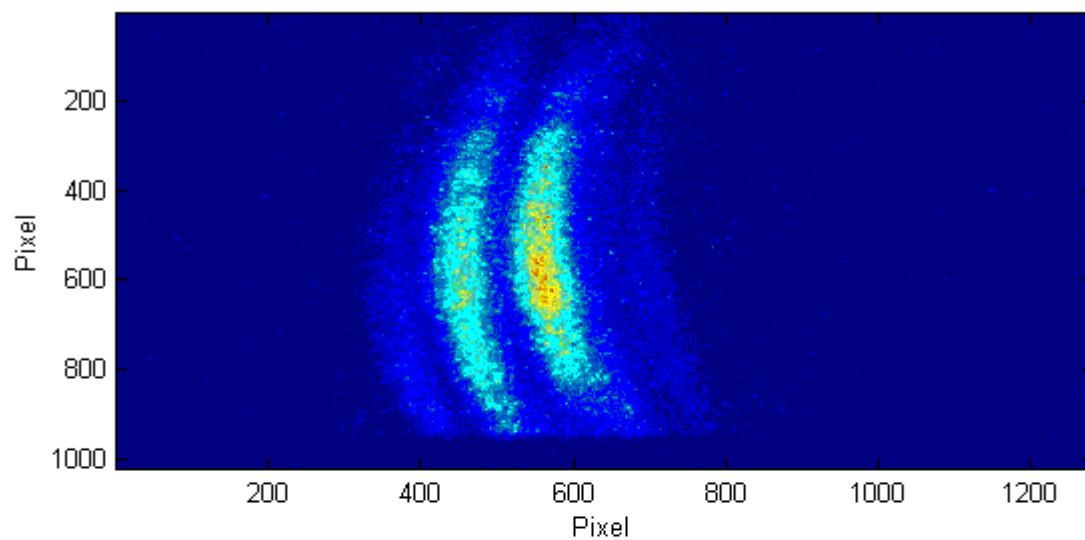


Energy fluctuations for a narrow bandwidth in the centre of the spectral distribution



- Few modes $M \Rightarrow$ fluctuations decrease
 - Many modes $M \Rightarrow$ 100 % fluctuations!
- Design value: $M \approx 20$**

$$M = 1.6 \Rightarrow \sigma = 46 \%$$

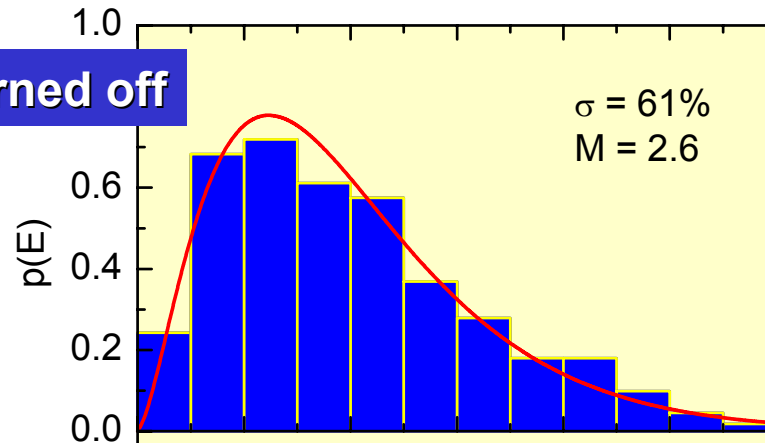
BC1 on

Pulse duration tailoring with Bunch Compressors

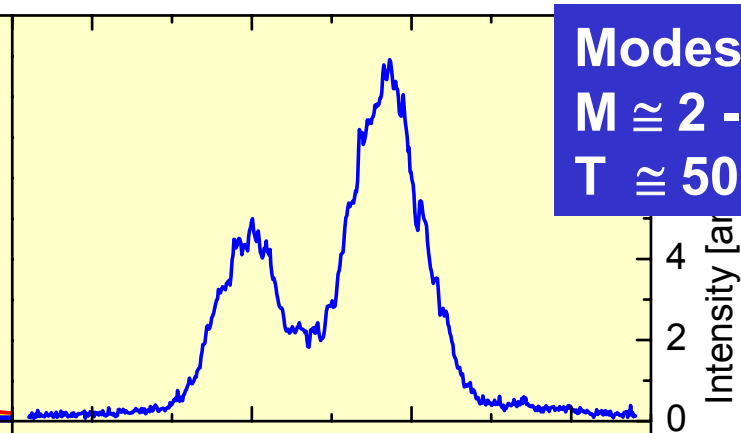
Linear regime

Saturation

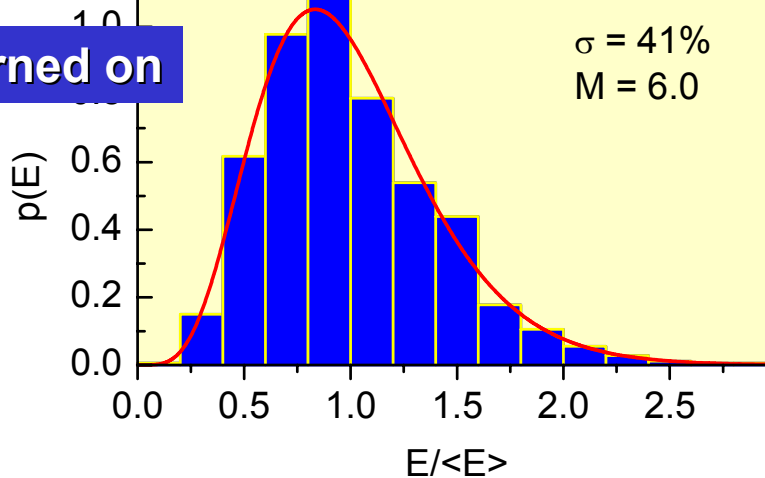
BC1 turned off



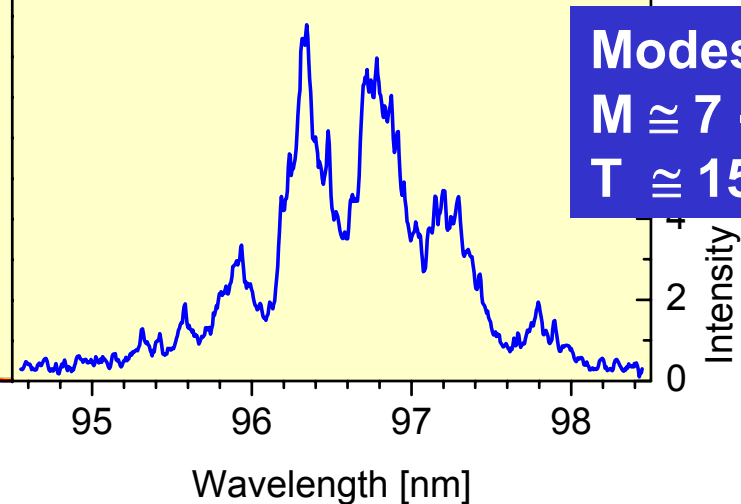
Modes:
 $M \approx 2 - 3$
 $T \approx 50 \text{ fs}$



BC1 turned on



Modes:
 $M \approx 7 - 10$
 $T \approx 150 \text{ fs}$



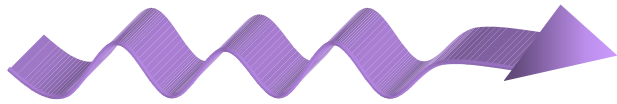
Summary

- Statistical properties of the SASE FEL are helpful for the determination of electron and photon beam properties.

- FEL parameters

Photon beam properties	Design values	Status
Pulse energy at saturation	330 -700 μJ	50 -100 μJ
Pulse duration (FWHM)	1.3 ps	30 -100 fs
Peak power	0.23-0.5 GW	1 GW
Energy fluctuations behind narrow-band mono at saturation	100%	40%

- Energy fluctuations behind a narrow-band monochromator decrease for short bunches.

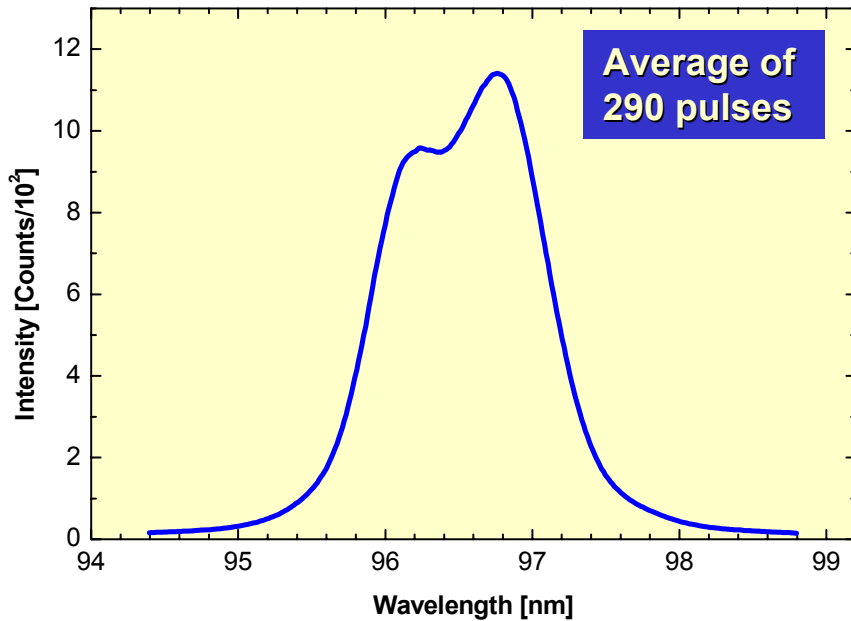


THE END

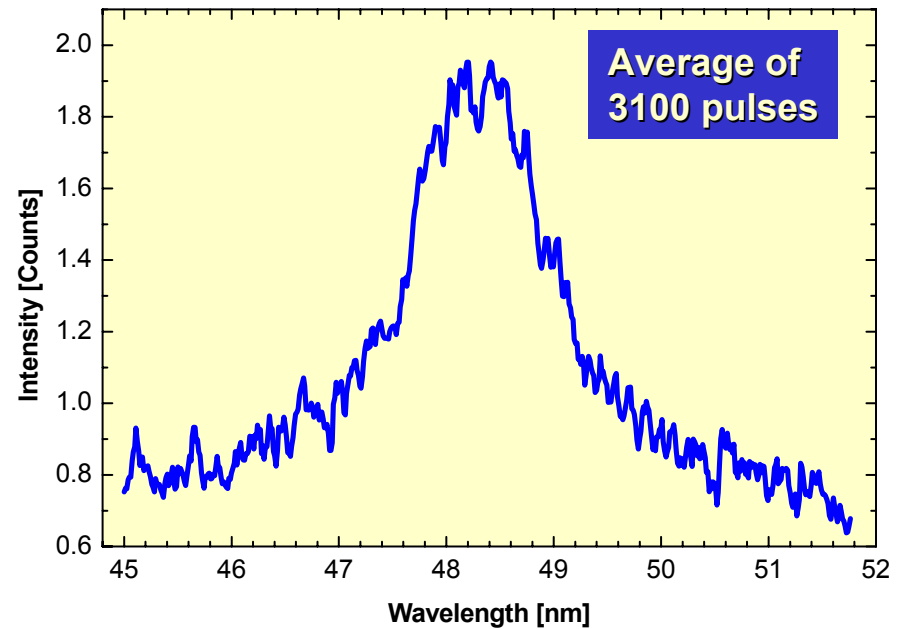
Spectral distribution

Higher Harmonics

Fundamental



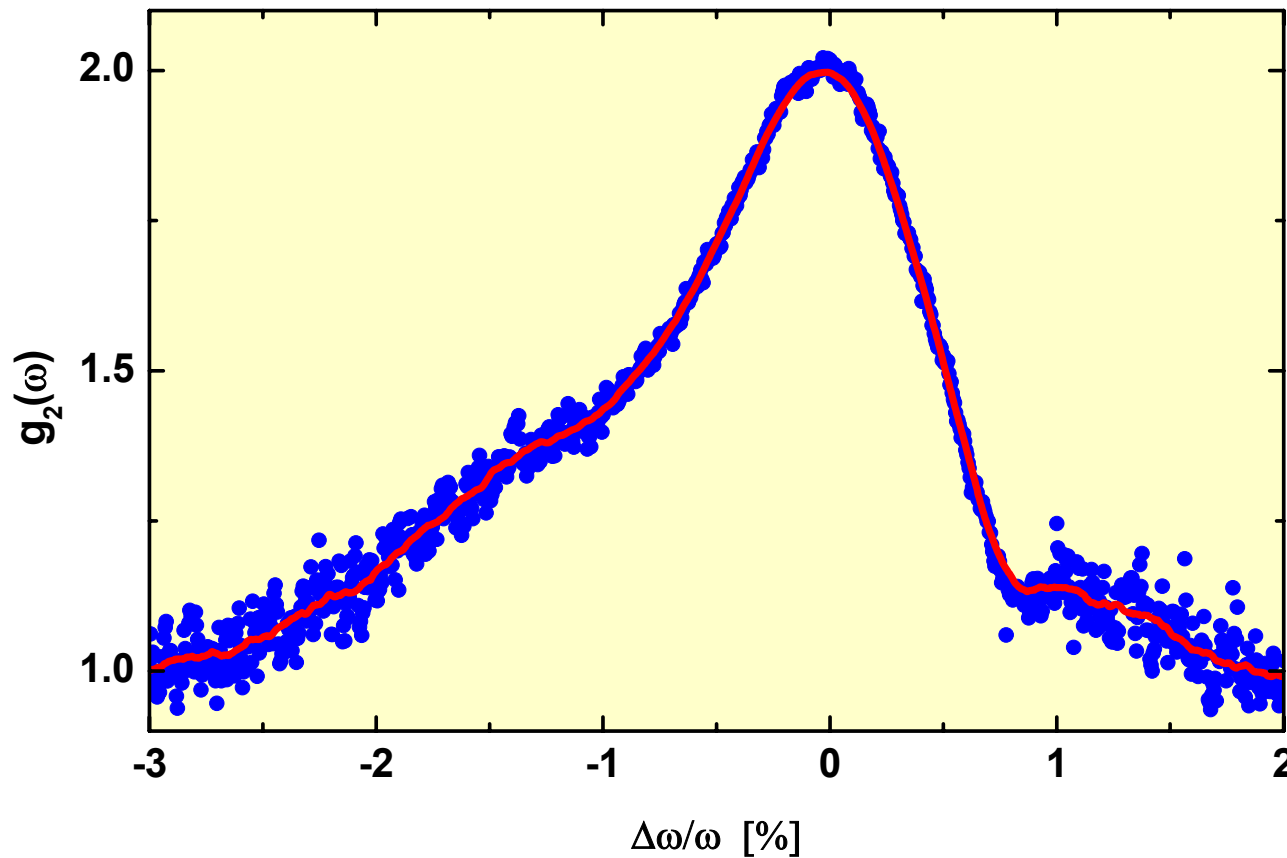
2nd Harmonic



⇒ Intensity of 2nd harmonic is about 1.0 - 0.1 % of the fundamental

Second Order Spectral Correlation

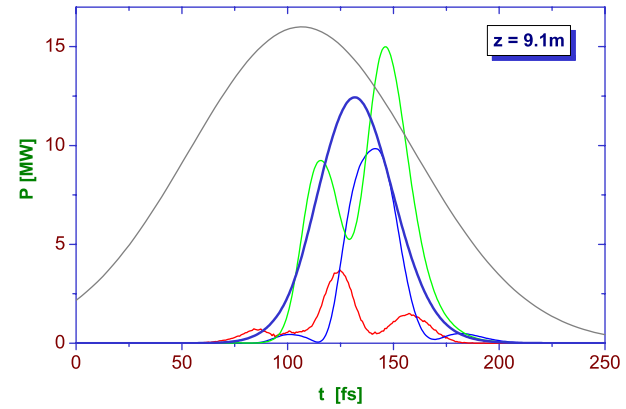
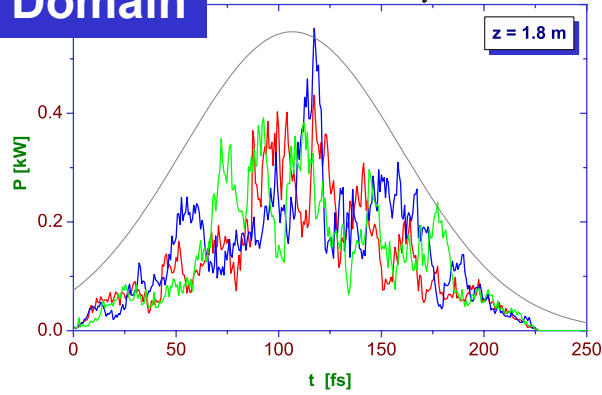
$$g_2(\omega, \omega') = \frac{\langle \bar{E}(\omega) \cdot E(\omega') \rangle}{\langle \bar{E}(\omega) \rangle \cdot \langle E(\omega') \rangle} = 1 + \frac{\sin^2((\omega - \omega')T/2)}{((\omega - \omega')T/2)^2}$$



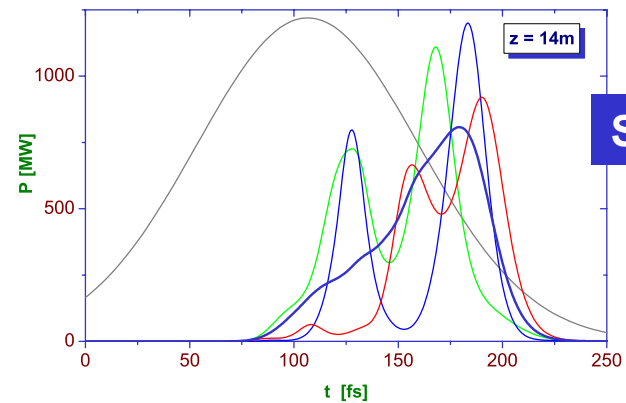
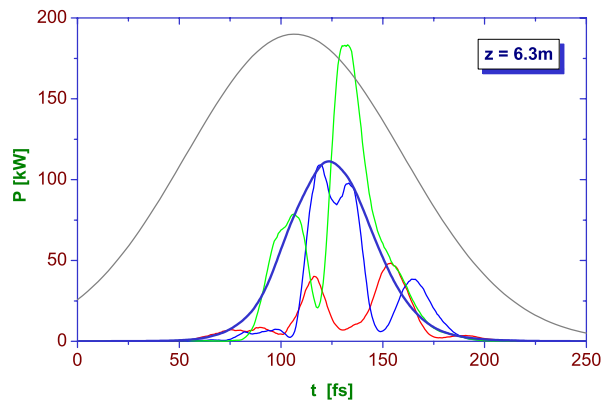
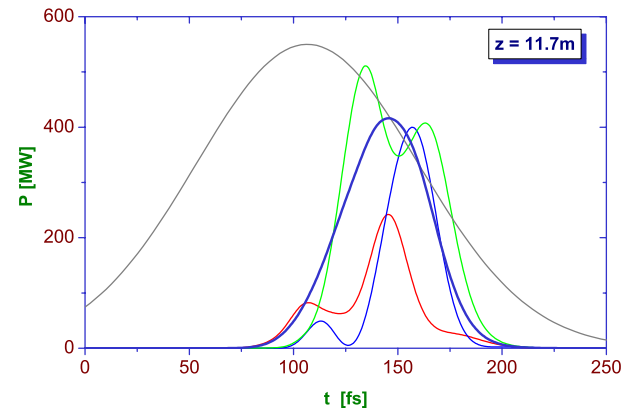
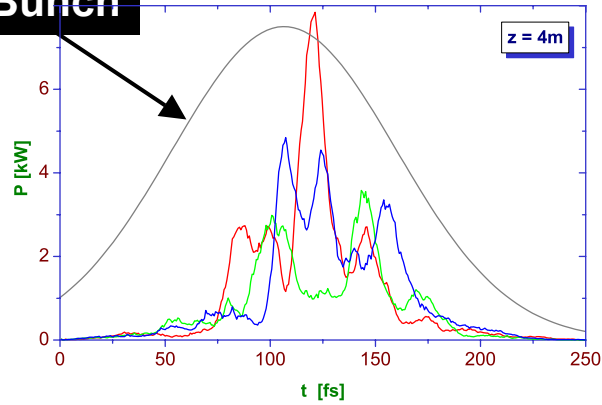
⇒ Method for the determination of the radiation pulse length T

Time Domain

Courtesy of M. Yurkov



Electron Bunch



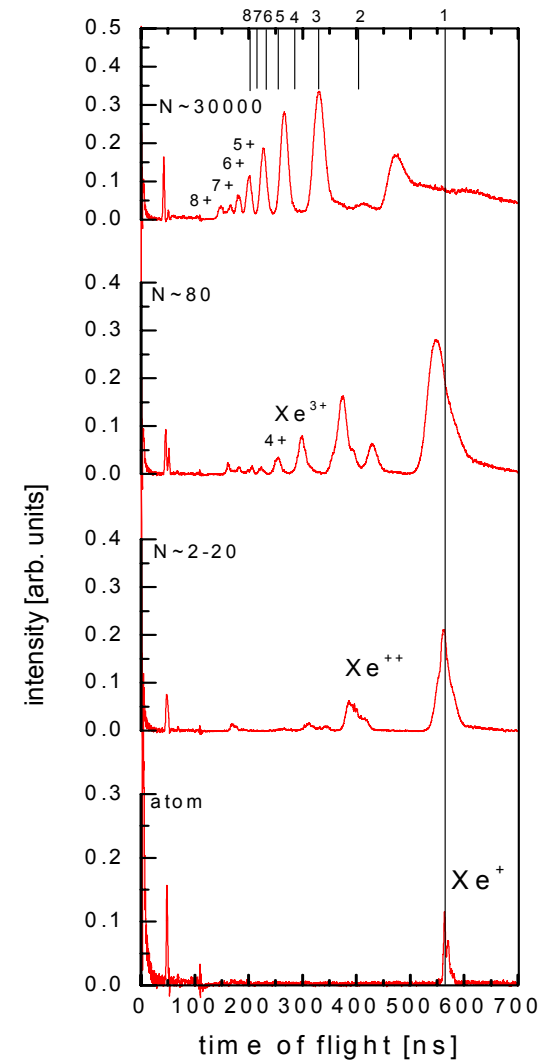
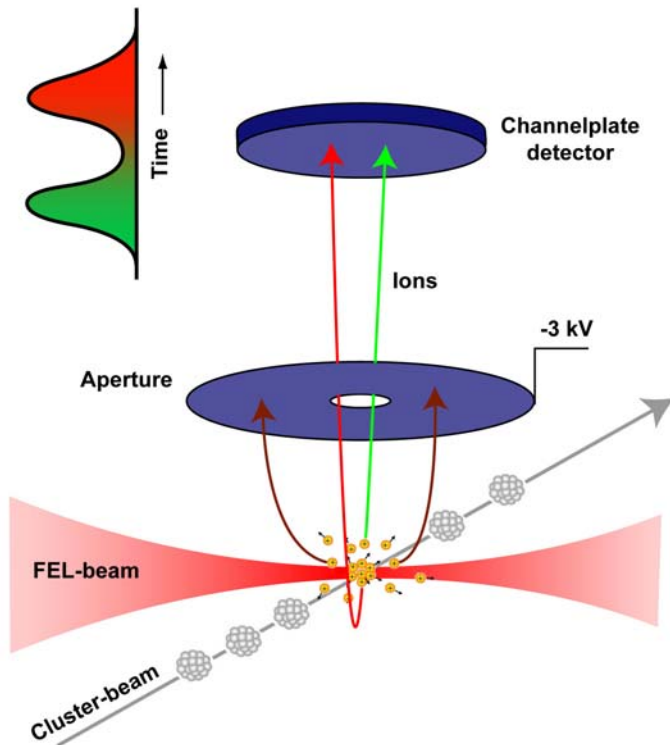
Slippage

Applications

Cluster Experiment

Hubertus Wabnitz, Thomas Möller *et al.*

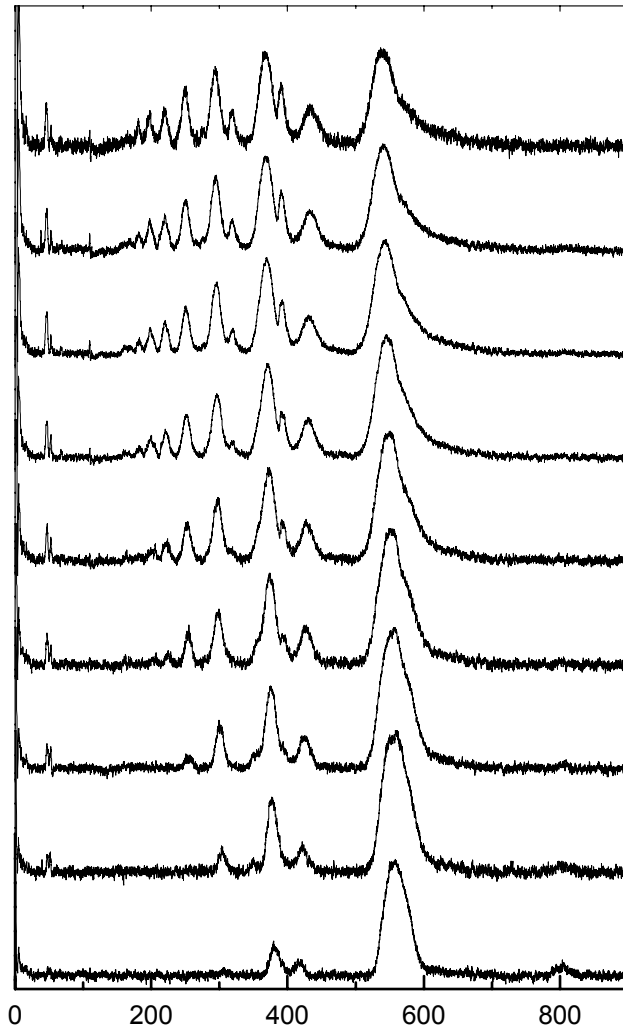
Cluster-Ion Detector



- emission of highly charged ions from clusters
- ions have high kinetic energies

Applications

Dependence on Cluster Size



Xenon clusters, 50 atoms
 10^{13} Watt/cm²

5×10^{11} Watt/cm²

Applications

Radiation Stability

FELIS Experiment:

(R. Sobierajski, J. Krzywinski, *et al.*)

wavelength: 98 nm

pulse length: 100 fs

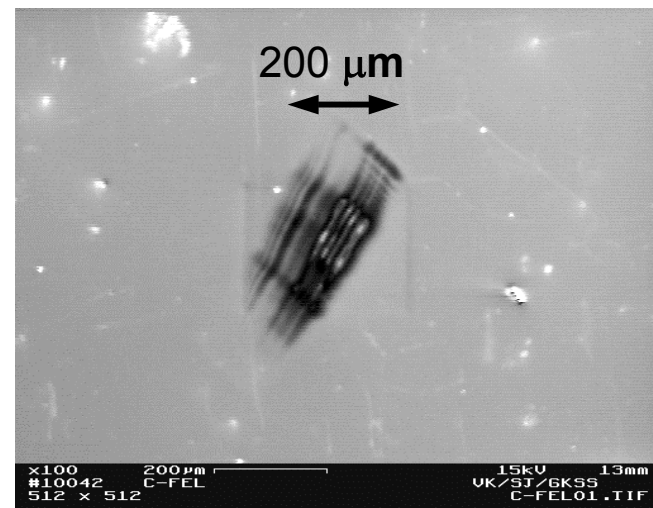
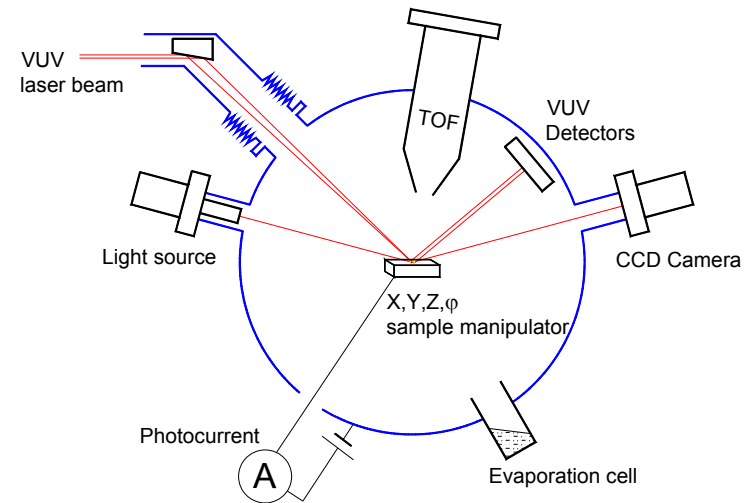
pulse energy : 40 μJ

damage threshold: 0.06 J/cm^2

Sample:

carbon mirror with 39 nm thickness

diffraction at intensity monitor
(gold wire)

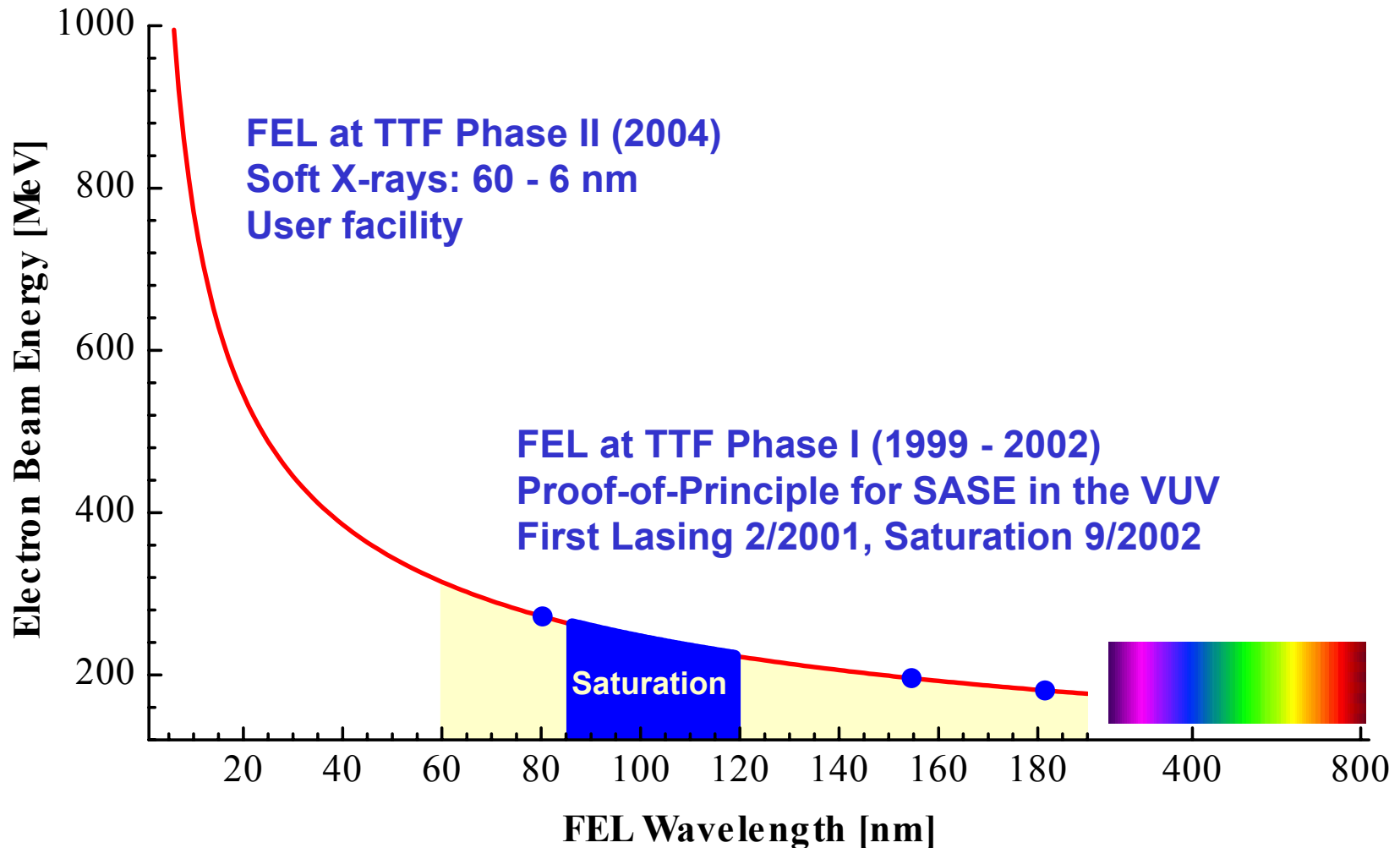


Summary

- **Free-Electron Laser at the TTF produces Gigawatt, femtosecond, laser-like radiation in the VUV**
- **Multiple Ionisation of Clusters**
- **Determination of Damage Thresholds**

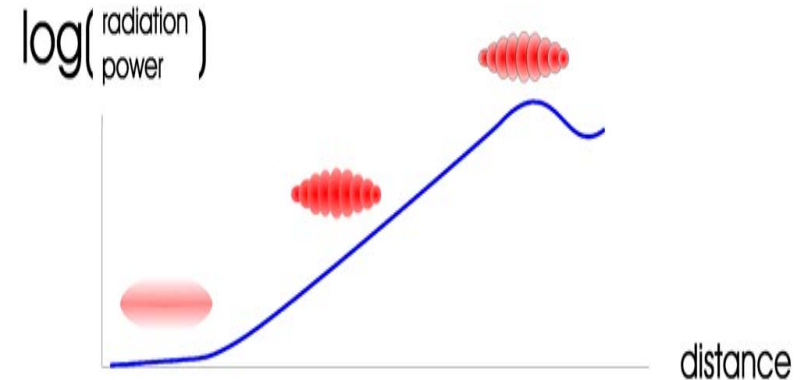
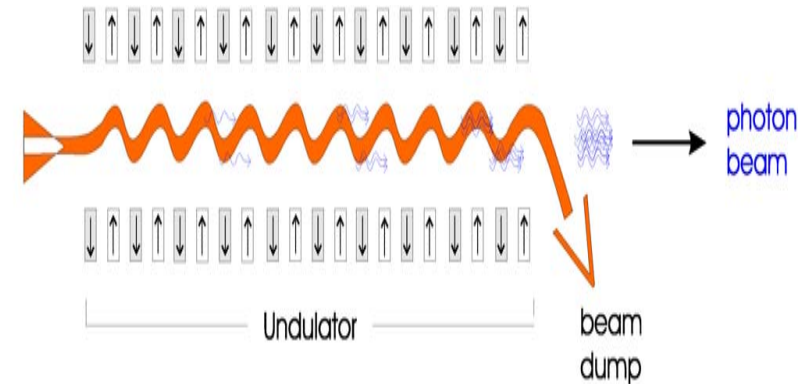
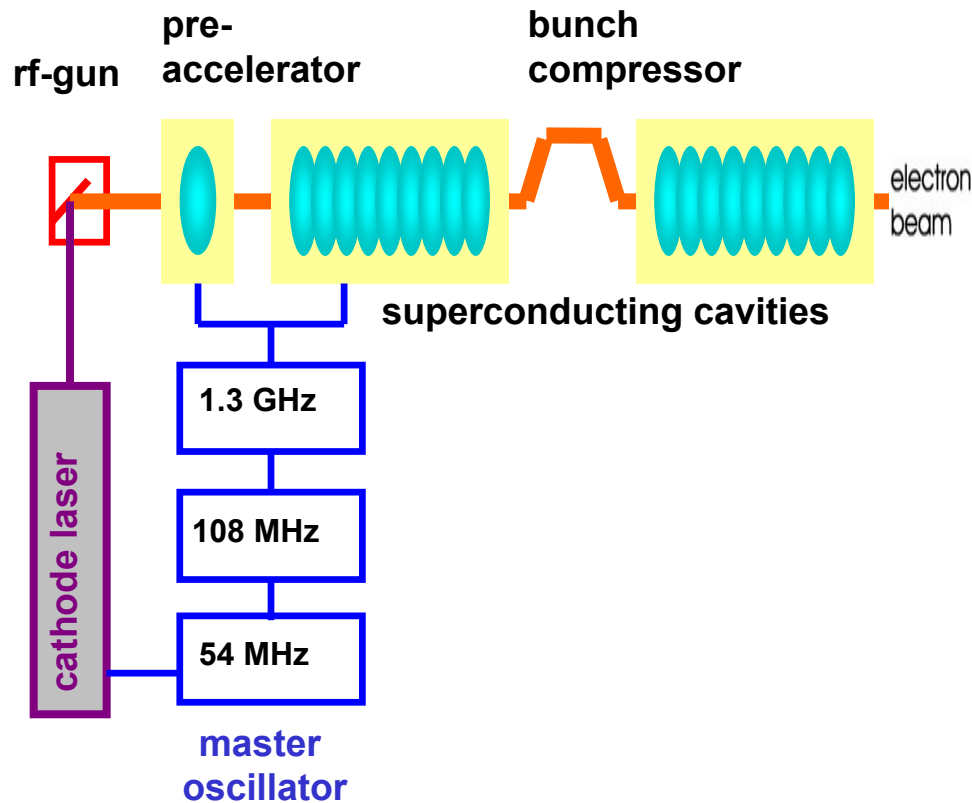
Experimental Setup

SASE in the Saturation Regime



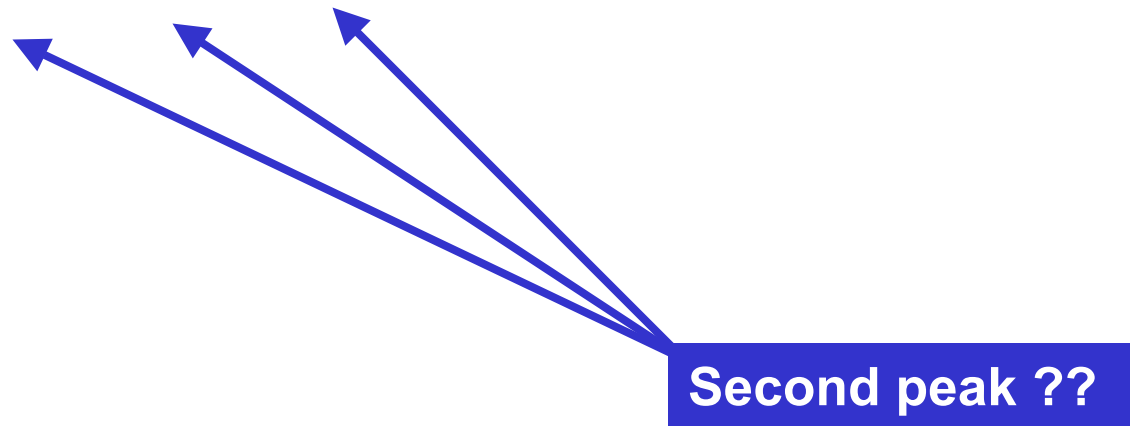
Experimental Setup

The Free-Electron Laser at TTF: Phase I

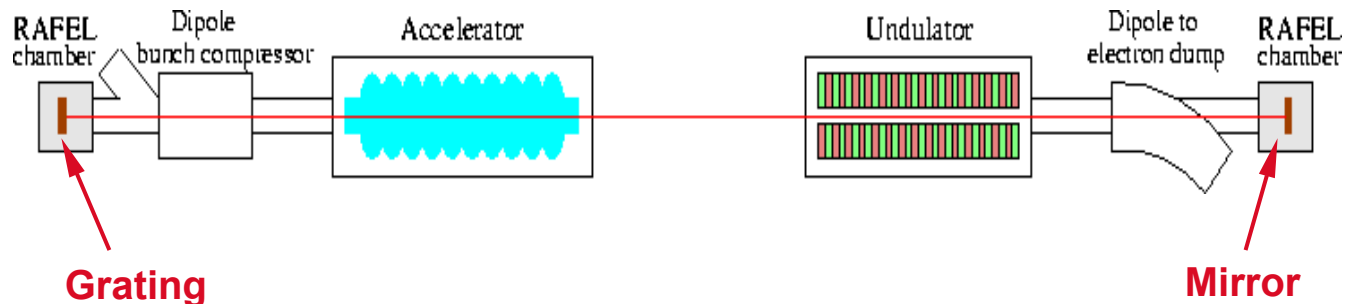


Idea: high gain \Rightarrow single pass \Rightarrow no mirrors !

Toroid reading

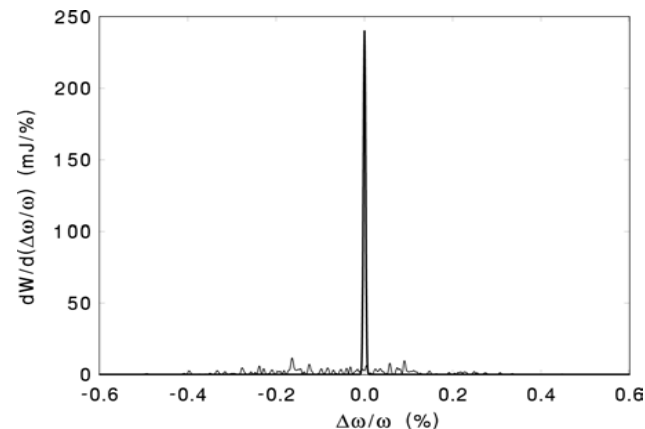
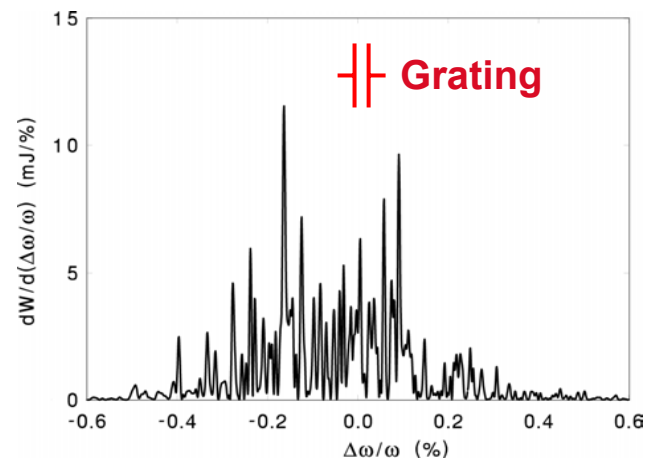


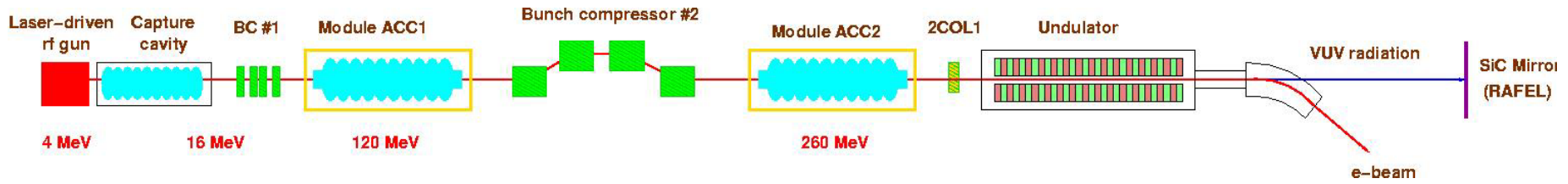
Regenerative FEL Amplifier (RAFEL)



Idea:
 to seed the SASE process of an electron bunch with a small bandwidth of the radiation emitted by the preceding electron bunch

- ⇒ small bandwidth
- ⇒ full longitudinal coherence
- ⇒ Seeding Option in Phase II

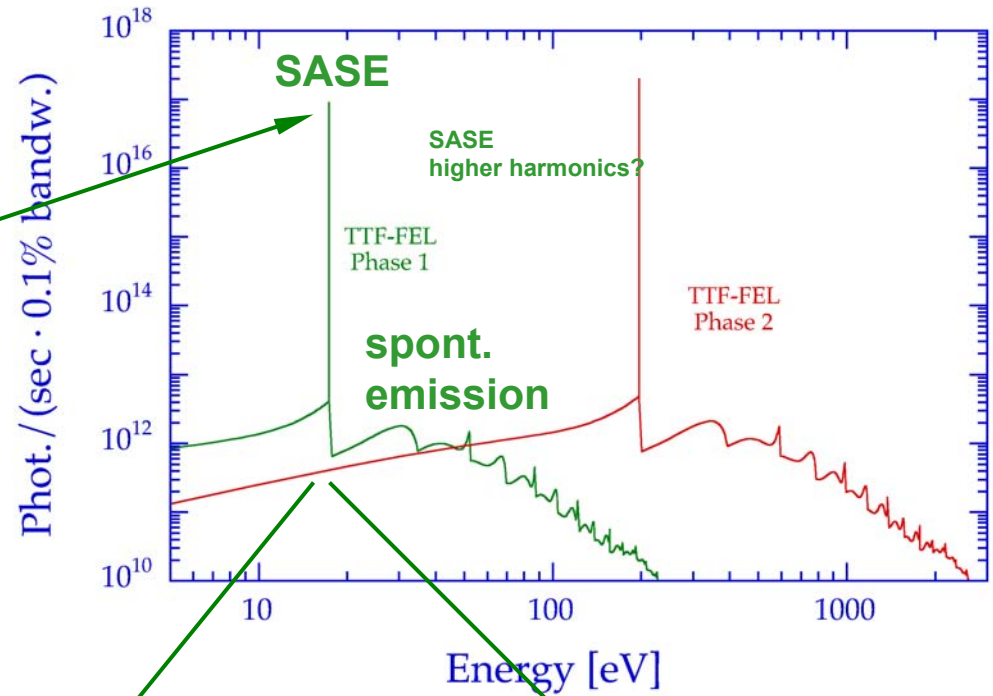




Courtesy of E. Schneidmiller

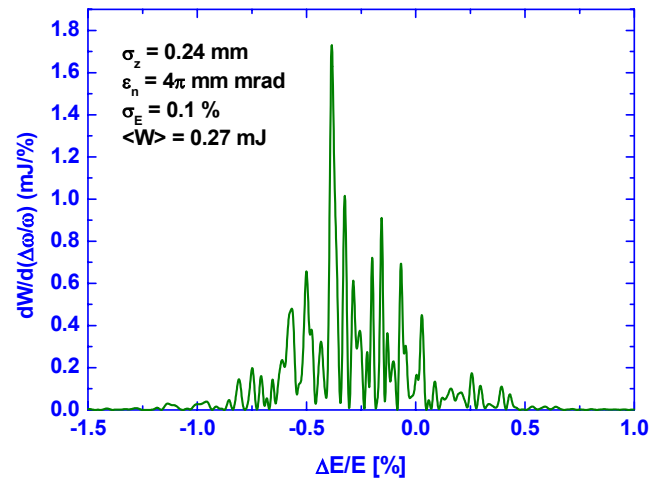
Full wavelength tunability
by electron energy variation

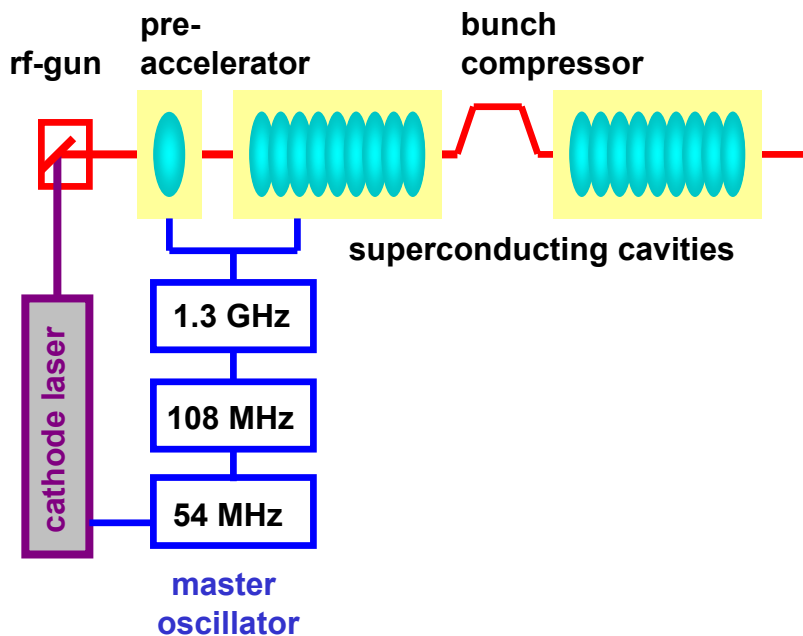
$$\lambda = \frac{\lambda_u}{2\gamma^2} \left(1 + \frac{K^2}{2} \right)$$



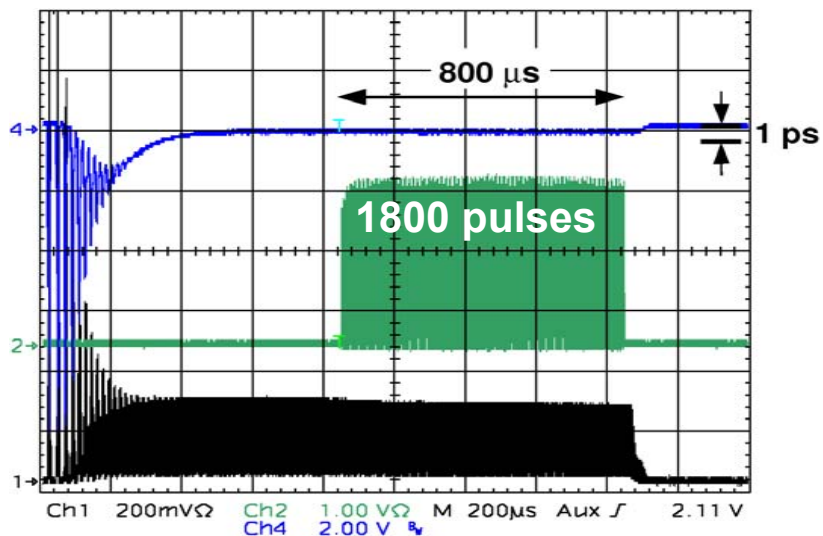
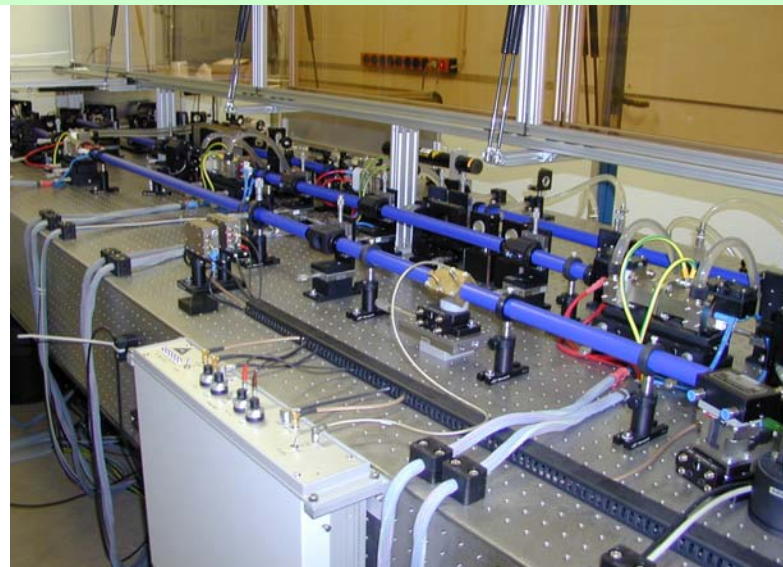
Full transverse coherence

BUT
not longitudinally coherent



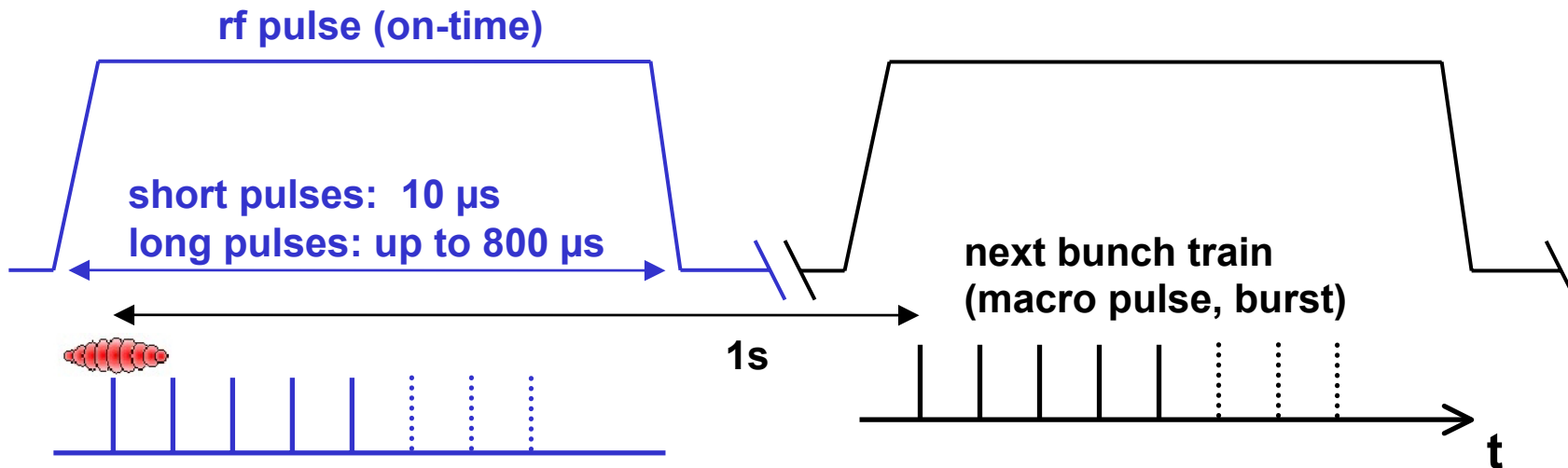


Frequency-quadrupled ND:YLF laser 1047 nm \Rightarrow 262 nm



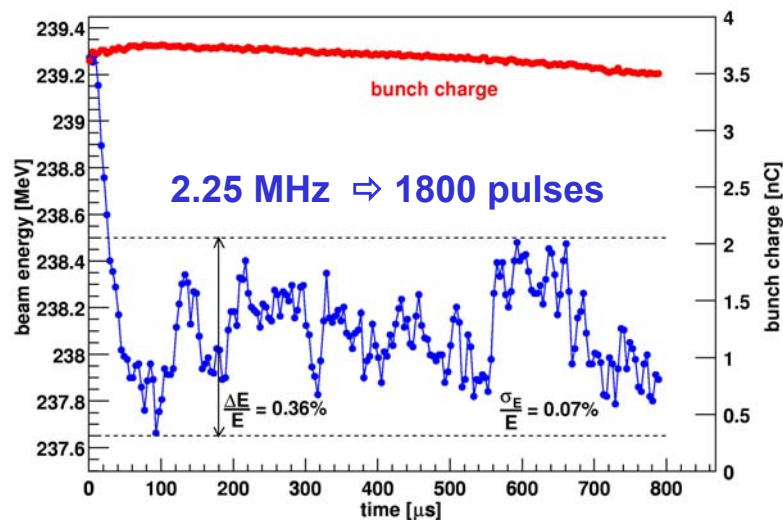
Pulse train 800 μ s
 Pulse energy 50 μ J
 Pulse duration (rms) 7 ps
 Energy variation:
 pulse to pulse < 5%
 Variable shape

Time structure of electron bunches



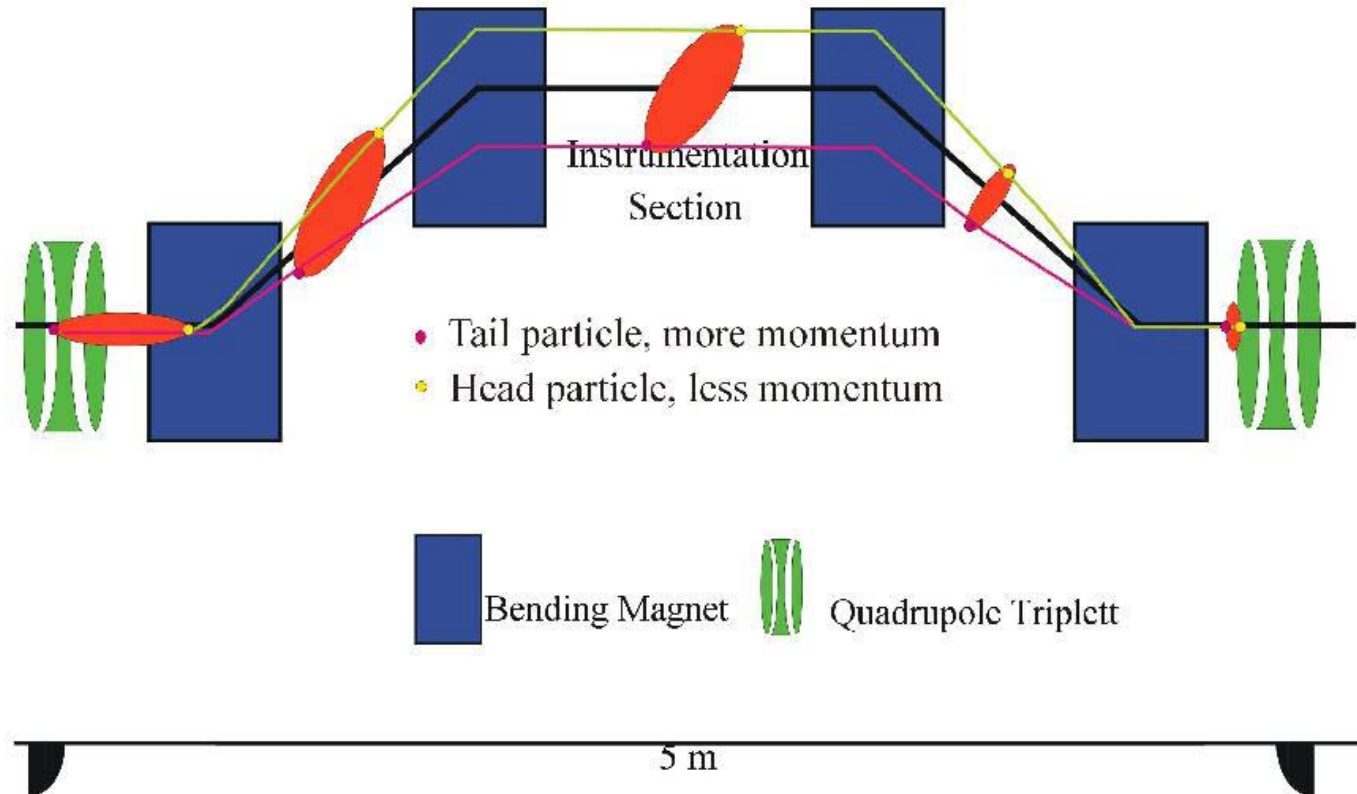
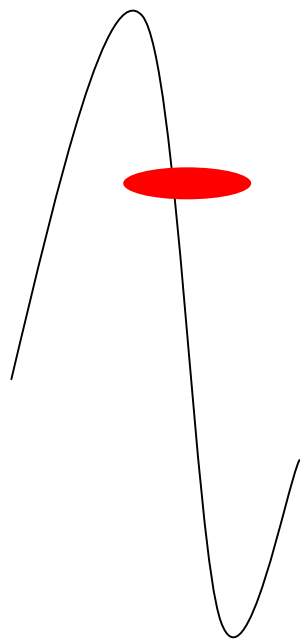
$10 \mu\text{s} = 100 \text{ kHz}$
 $1 \mu\text{s} = 1 \text{ MHz}$
 $444 \text{ ns} = 2.25 \text{ MHz}$

Number of pulses can be selected via control system



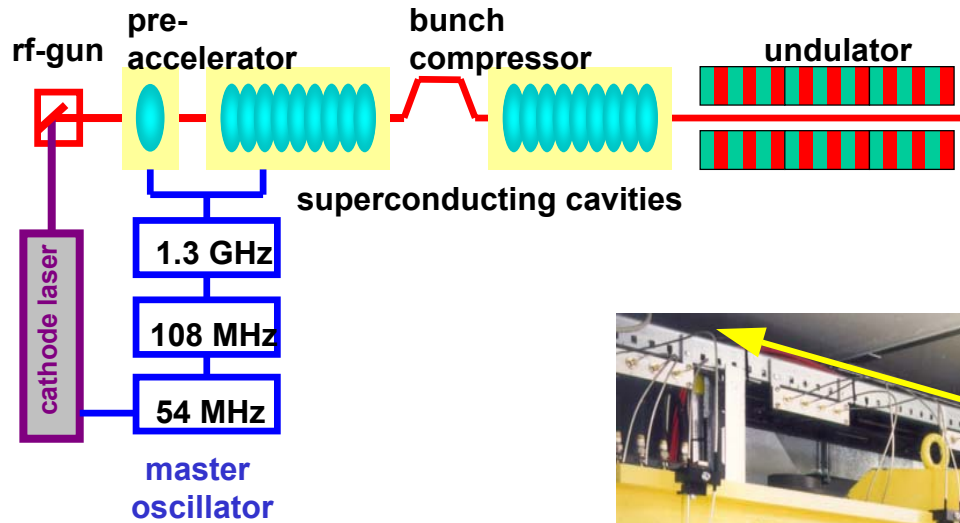
Bunch Compressor Scheme

Module 1



magnetic bunch compression

Phase of rf:
off crest \Rightarrow energy chirp



Period length: $\lambda_u = 27.3 \text{ mm}$
Magnetic peak field: $B = 0.46 \text{ T}$
Undulator parameter: $K = 1.17$



- Long undulator
3 modules of 4.5 m
- fixed gap
- Integrated focusing
- Corrector coils (steerers)

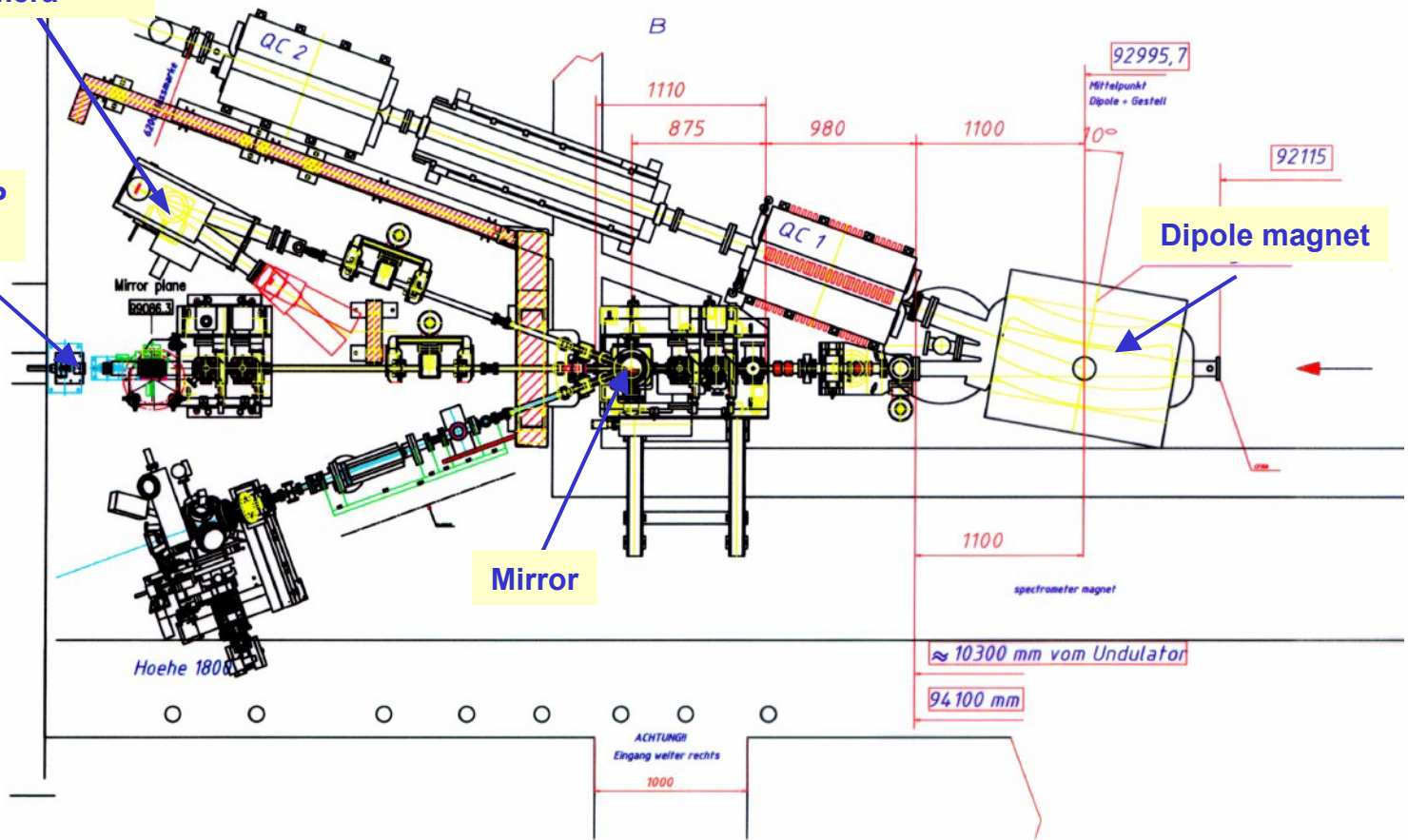
Photon Diagnostics Area

Spectral distribution

Monochromator +
ICCD camera

Intensity

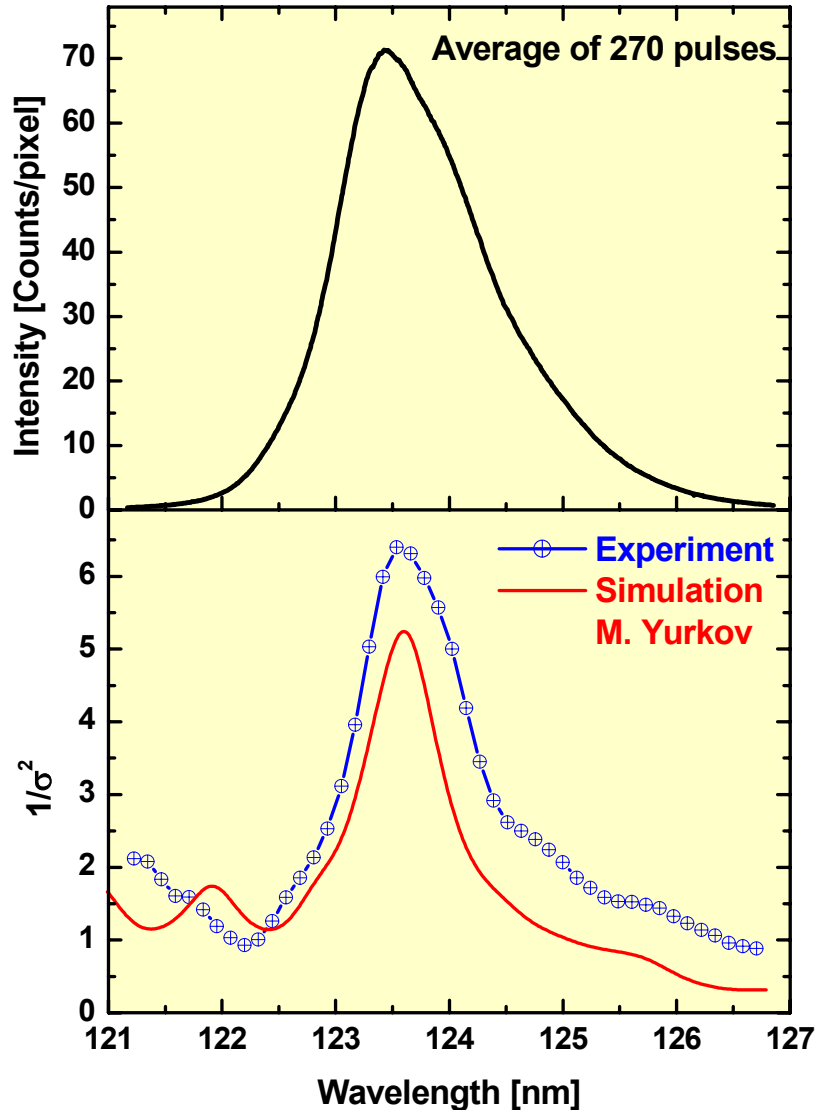
Wire + MCP
detector



≈ 10300 mm vom Undulator
94100 mm

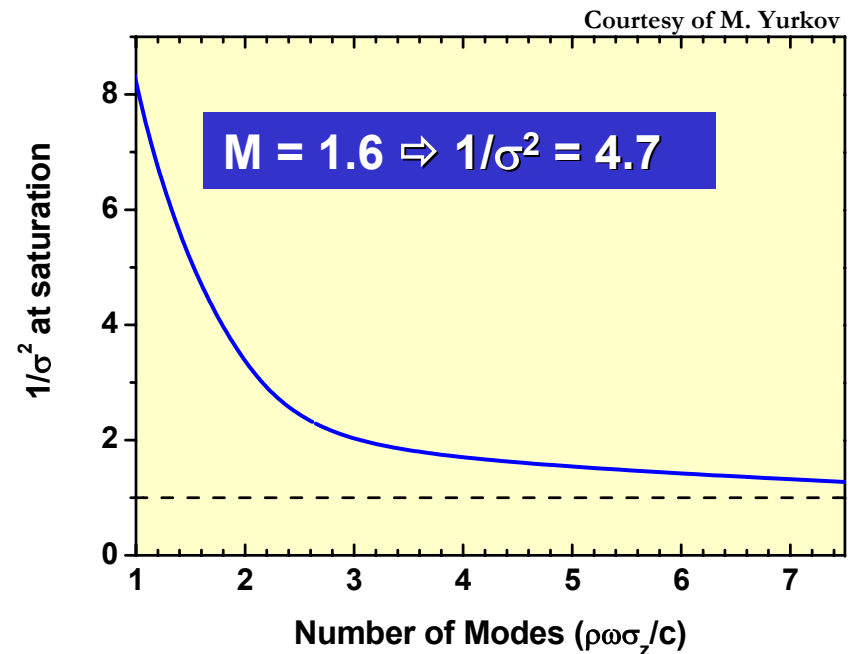
ACHTUNG!
Eingang weiter rechts
1000

Probability Distribution behind a narrow-band monochromator



At saturation:

- Probability distribution changes within the spectral distribution
- Asymmetric shape
- Many modes \Rightarrow 100 % fluctuations!



Cathode Laser

Wavelength	262 nm
Pulse energy	$\approx 50 \mu\text{J}$
No. of Photons	$\approx 5 \cdot 10^{13}$
Pulse duration	10 ps
Energy variation: pulse to pulse	< 5%

LINAC

Energy	245 MeV
No. of electrons	$\approx 10^{10}$
Pulse duration	10 ps
Energy variation: pulse to pulse	< 0.1%

FEL

Wavelength	90 nm
Pulse energy	$\approx 90 \mu\text{J}$
No. of Photons	$\approx 5 \cdot 10^{13}$
Pulse duration	50 fs
Energy variation:	$\approx 25\%$

Electrons Conversion Photons

**Current in the
flashlamps**



**Lasing in Nd:YLF oscillator
Frequency doubling**

**Photocathode
Acceleration
Undulator**



**spont. emission/SASE
Mirror
Monochromator
Ce:YAG fluorescence screen
Tandem optics**

**Photocathode
MCP**



**P46 fluorescence screen
Tandem optics**

**CCD
ADC
Computer
Monitor**



Eye ...